Hardware Description Languages

4.1 Introduction

Thus far, we have focused on designing combinational and sequential digital circuits at the schematic level. The process of finding an efficient set of logic gates to perform a given function is labor intensive and error prone, requiring manual simplification of truth tables or Boolean equations and manual translation of finite state machines (FSMs) into gates. In the 1990’s, designers discovered that they were far more productive if they worked at a higher level of abstraction, specifying just the logical function and allowing a computer-aided design (CAD) tool to produce the optimized gates. The specifications are generally given in a hardware description language (HDL). The two leading hardware description languages are Verilog and VHDL.

Verilog and VHDL are built on similar principles but have different syntax. Discussion of these languages in this chapter is divided into two columns for literal side-by-side comparison, with Verilog on the left and VHDL on the right. When you read the chapter for the first time, focus on one language or the other. Once you know one, you’ll quickly master the other if you need it.

Subsequent chapters show hardware in both schematic and HDL form. If you choose to skip this chapter and not learn one of the HDLs, you will still be able to master the principles of computer organization from the schematics. However, the vast majority of commercial systems are now built using HDLs rather than schematics. If you expect to do digital design at any point in your professional life, we urge you to learn one of the HDLs.

4.1.1 Modules

A block of hardware with inputs and outputs is called a module. An AND gate, a multiplexer, and a priority circuit are all examples of hardware modules. The two general styles for describing module functionality are...
behavioral and structural. Behavioral models describe what a module does. Structural models describe how a module is built from simpler pieces; it is an application of hierarchy. The Verilog and VHDL code in HDL Example 4.1 illustrate behavioral descriptions of a module that computes the Boolean function from Example 2.6, \( y = \overline{a}b\overline{c} + a\overline{b}c + abc \). In both languages, the module is named sillyfunction and has three inputs, \( a, b, \) and \( c \), and one output, \( y \).

### HDL Example 4.1 COMBINATIONAL LOGIC

<table>
<thead>
<tr>
<th>Verilog</th>
<th>VHDL</th>
</tr>
</thead>
<tbody>
<tr>
<td>module sillyfunction (input a, b, c, output y);</td>
<td>library IEEE; use IEEE.STD_LOGIC_1164.all;</td>
</tr>
<tr>
<td>assign y = !a &amp; !b &amp; !c</td>
<td>entity sillyfunction is</td>
</tr>
<tr>
<td>!a &amp; !b &amp; !c</td>
<td>port (a, b, c: in STD_LOGIC;</td>
</tr>
<tr>
<td>!a &amp; !b &amp; c;</td>
<td>y: out STD_LOGIC);</td>
</tr>
<tr>
<td>endmodule</td>
<td>architecture synth of sillyfunction is</td>
</tr>
<tr>
<td></td>
<td>begin</td>
</tr>
<tr>
<td></td>
<td>y &lt;= ((!a and !b and !c) or</td>
</tr>
<tr>
<td></td>
<td>(a and !b and !c) or</td>
</tr>
<tr>
<td></td>
<td>(a and !b and c);</td>
</tr>
<tr>
<td></td>
<td>end;</td>
</tr>
</tbody>
</table>

A Verilog module begins with the module name and a listing of the inputs and outputs. The assign statement describes combinational logic. \( \! \) indicates NOT, & indicates AND, and | indicates OR.

Verilog signals such as the inputs and outputs are Boolean variables (0 or 1). They may also have floating and undefined values, as discussed in Section 4.2.8.

VHDL code has three parts: the library use clause, the entity declaration, and the architecture body. The library use clause is required and will be discussed in Section 4.2.11. The entity declaration lists the module name and its inputs and outputs. The architecture body defines what the module does.

VHDL signals, such as inputs and outputs, must have a type declaration. Digital signals should be declared to be STD_LOGIC type. STD_LOGIC signals can have a value of '0' or '1', as well as floating and undefined values that will be described in Section 4.2.8. The STD_LOGIC type is defined in the IEEE.STD_LOGIC_1164 library, which is why the library must be used.

VHDL lacks a good default order of operations, so Boolean equations should be parenthesized.

A module, as you might expect, is a good application of modularity. It has a well defined interface, consisting of its inputs and outputs, and it performs a specific function. The particular way in which it is coded is unimportant to others that might use the module, as long as it performs its function.

### 4.1.2 Language Origins

Universities are almost evenly split on which of these languages is taught in a first course, and industry is similarly split on which language is preferred. Compared to Verilog, VHDL is more verbose and cumbersome,
as you might expect of a language developed by committee. U.S. military contractors, the European Space Agency, and telecommunications companies use VHDL extensively.

Both languages are fully capable of describing any hardware system, and both have their quirks. The best language to use is the one that is already being used at your site or the one that your customers demand. Most CAD tools today allow the two languages to be mixed, so that different modules can be described in different languages.

### 4.1.3 Simulation and Synthesis

The two major purposes of HDLs are logic *simulation* and *synthesis*. During simulation, inputs are applied to a module, and the outputs are checked to verify that the module operates correctly. During synthesis, the textual description of a module is transformed into logic gates.

**Simulation**

Humans routinely make mistakes. Such errors in hardware designs are called *bugs*. Eliminating the bugs from a digital system is obviously important, especially when customers are paying money and lives depend on the correct operation. Testing a system in the laboratory is time-consuming. Discovering the cause of errors in the lab can be extremely difficult, because only signals routed to the chip pins can be observed. There is no way to directly observe what is happening inside a chip. Correcting errors after the system is built can be devastatingly expensive. For example, correcting a mistake in a cutting-edge integrated circuit costs more than a million dollars and takes several months. Intel’s infamous FDIV (floating point division) bug in the Pentium processor forced the company to recall chips after they had shipped, at a total cost of $475 million. Logic simulation is essential to test a system before it is built.

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1 The Institute of Electrical and Electronics Engineers (IEEE) is a professional society responsible for many computing standards including WiFi (802.11), Ethernet (802.3), and floating-point numbers (754) (see Chapter 5).
Figure 4.1 shows waveforms from a simulation of the previous sillyfunction module demonstrating that the module works correctly. y is TRUE when a, b, and c are 000, 100, or 101, as specified by the Boolean equation.

Synthesis
Logic synthesis transforms HDL code into a netlist describing the hardware (e.g., the logic gates and the wires connecting them). The logic synthesizer might perform optimizations to reduce the amount of hardware required. The netlist may be a text file, or it may be drawn as a schematic to help visualize the circuit. Figure 4.2 shows the results of synthesizing the sillyfunction module. Notice how the three three-input AND gates are simplified into two two-input AND gates, as we discovered in Example 2.6 using Boolean algebra.

Circuit descriptions in HDL resemble code in a programming language. However, you must remember that the code is intended to represent hardware. Verilog and VHDL are rich languages with many commands. Not all of these commands can be synthesized into hardware. For example, a command to print results on the screen during simulation does not translate into hardware. Because our primary interest is

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2 The simulation was performed with the Xilinx ISE Simulator, which is part of the Xilinx ISE 8.2 software. The simulator was selected because it is used commercially, yet is freely available to universities.

3 Synthesis was performed with Synplify Pro from Synplicity. The tool was selected because it is the leading commercial tool for synthesizing HDL to field-programmable gate arrays (see Section 5.6.2) and because it is available inexpensively for universities.
to build hardware, we will emphasize a *synthesizable subset* of the languages. Specifically, we will divide HDL code into *synthesizable* modules and a *testbench*. The synthesizable modules describe the hardware. The testbench contains code to apply inputs to a module, check whether the output results are correct, and print discrepancies between expected and actual outputs. Testbench code is intended only for simulation and cannot be synthesized.

One of the most common mistakes for beginners is to think of HDL as a computer program rather than as a shorthand for describing digital hardware. If you don’t know approximately what hardware your HDL should synthesize into, you probably won’t like what you get. You might create far more hardware than is necessary, or you might write code that simulates correctly but cannot be implemented in hardware. Instead, think of your system in terms of blocks of combinational logic, registers, and finite state machines. Sketch these blocks on paper and show how they are connected before you start writing code.

In our experience, the best way to learn an HDL is by example. HDLs have specific ways of describing various classes of logic; these ways are called *idioms*. This chapter will teach you how to write the proper HDL idioms for each type of block and then how to put the blocks together to produce a working system. When you need to describe a particular kind of hardware, look for a similar example and adapt it to your purpose. We do not attempt to rigorously define all the syntax of the HDLs, because that is deathly boring and because it tends to encourage thinking of HDLs as programming languages, not shorthand for hardware. The IEEE Verilog and VHDL specifications, and numerous dry but exhaustive textbooks, contain all of the details, should you find yourself needing more information on a particular topic. (See Further Readings section at back of the book.)

### 4.2 COMBINATIONAL LOGIC

Recall that we are disciplining ourselves to design synchronous sequential circuits, which consist of combinational logic and registers. The outputs of combinational logic depend only on the current inputs. This section describes how to write behavioral models of combinational logic with HDLs.

#### 4.2.1 Bitwise Operators

*Bitwise* operators act on single-bit signals or on multi-bit busses. For example, the `inv` module in HDL Example 4.2 describes four inverters connected to 4-bit busses.
The endianness of a bus is purely arbitrary. (See the sidebar in Section 6.2.2 for the origin of the term.) Indeed, endianness is also irrelevant to this example, because a bank of inverters doesn’t care what the order of the bits are. Endianness matters only for operators, such as addition, where the sum of one column carries over into the next. Either ordering is acceptable, as long as it is used consistently. We will consistently use the little-endian order, \([N-1:0]\) in Verilog and \((N-1 \text{ downto } 0)\) in VHDL, for an \(N\)-bit bus.

After each code example in this chapter is a schematic produced from the Verilog code by the Synplify Pro synthesis tool. Figure 4.3 shows that the \texttt{inv} module synthesizes to a bank of four inverters, indicated by the inverter symbol labeled \(y[3:0]\). The bank of inverters connects to 4-bit input and output busses. Similar hardware is produced from the synthesized VHDL code.

The \texttt{gates} module in HDL Example 4.3 demonstrates bitwise operations acting on 4-bit busses for other basic logic functions.
4.2 Combinational Logic

**HDL Example 4.3 LOGIC GATES**

**Verilog**

```verilog
class gates(input [3:0] a, b, output [3:0] y1, y2, y3, y4, y5):
    /* Five different two-input logic gates acting on 4 bit busses */
    assign y1 = a & b; // AND
    assign y2 = a | b; // OR
    assign y3 = a ^ b; // XOR
    assign y4 = ~(a & b); // NAND
    assign y5 = ~(a | b); // NOR
endmodule
```

~, ^, and | are examples of Verilog operators, whereas a, b, and y1 are operands. A combination of operators and operands, such as a & b, or ~(a | b), is called an expression. A complete command such as `assign y4 = ~(a & b);` is called a statement.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity gates is
    port(a, b: in STD_LOGIC_VECTOR(3 downto 0);
y1, y2, y3, y4, y5:   out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture synth of gates is
begin
    -- Five different two-input logic gates acting on 4 bit busses
    y1 <= a and b;
y2 <= a or b;
y3 <= a xor b;
y4 <= a nand b;
y5 <= a nor b;
end;
```

not, xor, and or are examples of VHDL operators, whereas a, b, and y1 are operands. A combination of operators and operands, such as a and b, or a nor b, is called an expression. A complete command such as `y4 <= a nand b;` is called a statement.

**Figure 4.4 gates synthesized circuit**

A combination of operators and operands, such as a and b, or a nor b, is called an expression. A complete command such as `y4 <= a nand b;` is called a statement.

VHDL assignment statements end with a semicolon. Anytime the inputs on the right side of the `<=` in a concurrent signal assignment statement change, the output on the left side is recomputed. Thus, concurrent signal assignment statements describe combinational logic.
4.2.3 Reduction Operators

Reduction operators imply a multiple-input gate acting on a single bus. HDL Example 4.4 describes an eight-input AND gate with inputs \(a_7, a_6, \ldots, a_0\).

**HDL Example 4.4 EIGHT-INPUT AND**

**Verilog**

```verilog
module and8(input [7:0] a, output y);
assign y = &a;

// &a is much easier to write than
endmodule
```

As one would expect, |, ^, ¬, and ¬ | reduction operators are available for OR, XOR, NAND, and NOR as well. Recall that a multi-input XOR performs parity, returning TRUE if an odd number of inputs are TRUE.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity and8 is
  port(a: in std_logic_vector(7 downto 0); y: out std_logic);
end;

architecture synth of and8 is
begin
  y <= a(7) and a(6) and a(5) and a(4) and a(3) and a(2) and a(1) and a(0);
end;
```

VHDL does not have reduction operators. Instead, it provides the generate command (see Section 4.7). Alternatively, the operation can be written explicitly, as shown below.
4.2.4 Conditional Assignment

Conditional assignments select the output from among alternatives based on an input called the condition. HDL Example 4.5 illustrates a 2:1 multiplexer using conditional assignment.

**HDL Example 4.5 2:1 MULTIPLEXER**

**Verilog**

The conditional operator `?` chooses, based on a first expression, between a second and third expression. The first expression is called the condition. If the condition is 1, the operator chooses the second expression. If the condition is 0, the operator chooses the third expression.

`?` is especially useful for describing a multiplexer because, based on the first input, it selects between two others. The following code demonstrates the idiom for a 2:1 multiplexer with 4-bit inputs and outputs using the conditional operator.

```verilog
module mux2 (input [3:0] d0, d1, input s, output [3:0] y);
assign y = s ? d1 : d0;
endmodule
```

If `s` is 1, then `y = d1`. If `s` is 0, then `y = d0`.

`?` is also called a ternary operator, because it takes three inputs. It is used for the same purpose in the C and Java programming languages.

**VHDL**

Conditional signal assignments perform different operations depending on some condition. They are especially useful for describing a multiplexer. For example, a 2:1 multiplexer can use conditional signal assignment to select one of two 4-bit inputs.

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mux2 is
port(d0, d1: in STD_LOGIC_VECTOR(3 downto 0); s: in STD_LOGIC; y: out STD_LOGIC_VECTOR(3 downto 0));
end;
architecture synth of mux2 is
begin
y <= d0 when s = '0' else d1;
end;
```

The conditional signal assignment sets `y` to `d0` if `s` is 0. Otherwise it sets `y` to `d1`.

**Figure 4.5** and 8 synthesized circuit

**Figure 4.6** `mux2` synthesized circuit
HDL Example 4.6 shows a 4:1 multiplexer based on the same principle as the 2:1 multiplexer in HDL Example 4.5.

Figure 4.7 shows the schematic for the 4:1 multiplexer produced by Synplify Pro. The software uses a different multiplexer symbol than this text has shown so far. The multiplexer has multiple data (\(d\)) and one-hot enable (\(e\)) inputs. When one of the enables is asserted, the associated data is passed to the output. For example, when \(s[1] = s[0] = 0\), the bottom AND gate, \(\text{un1_s_5}\), produces a 1, enabling the bottom input of the multiplexer and causing it to select \(d0[3:0]\).

### HDL Example 4.6 4:1 MULTIPLEXER

#### Verilog

A 4:1 multiplexer can select one of four inputs using nested conditional operators.

```verilog
module mux4(input [3:0] d0, d1, d2, d3,
            input [1:0] s,
            output [3:0] y);

assign y = s[1] ? (s[0] ? d3 : d2)
            : (s[0] ? d1 : d0);
endmodule
```

If \(s[1]\) is 1, then the multiplexer chooses the first expression, \((s[0] ? d3 : d2)\). This expression in turn chooses either \(d3\) or \(d2\) based on \(s[0]\) (\(y = d3\) if \(s[0] = 1\) and \(d2\) if \(s[0] = 0\)). If \(s[1]\) is 0, then the multiplexer similarly chooses the second expression, which gives either \(d1\) or \(d0\) based on \(s[0]\).

#### VHDL

A 4:1 multiplexer can select one of four inputs using multiple `else` clauses in the conditional signal assignment.

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mux4 is
port(d0, d1, d2, d3: in STD_LOGIC_VECTOR(3 downto 0);
    s: in STD_LOGIC_VECTOR(1 downto 0);
    y: out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture synthl of mux4 is
begin
    y <= d0 when s = "00" else
         d1 when s = "01" else
         d2 when s = "10" else
         d3;
end;
```

VHDL also supports `selected signal assignment statements` to provide a shorthand when selecting from one of several possibilities. This is analogous to using a `case` statement in place of multiple `if/else` statements in some programming languages. The 4:1 multiplexer can be rewritten with selected signal assignment as follows:

```vhdl
architecture synth2 of mux4 is
begin
    with a select y <=
        d0 when "00",
        d1 when "01",
        d2 when "10",
        d3 when others;
end;
```

### 4.2.5 Internal Variables

Often it is convenient to break a complex function into intermediate steps. For example, a full adder, which will be described in Section 5.2.1,
is a circuit with three inputs and two outputs defined by the following equations:

\[ S = A \oplus B \oplus C_{in} \]
\[ C_{out} = AB + AC_{in} + BC_{in} \]  

(4.1)

If we define intermediate signals, \( P \) and \( G \),

\[ P = A \oplus B \]
\[ G = AB \]  

(4.2)

we can rewrite the full adder as follows:

\[ S = P \oplus C_{in} \]
\[ C_{out} = G + PC_{in} \]  

(4.3)

\( P \) and \( G \) are called internal variables, because they are neither inputs nor outputs but are used only internal to the module. They are similar to local variables in programming languages. HDL Example 4.7 shows how they are used in HDLs.

HDL assignment statements (assign in Verilog and <= in VHDL) take place concurrently. This is different from conventional programming languages such as C or Java, in which statements are evaluated in the order in which they are written. In a conventional language, it is

Figure 4.7 mux4 synthesized circuit

Check this by filling out the truth table to convince yourself it is correct.
important that $S = P \oplus C_{in}$ comes after $P = A \oplus B$, because statements are executed sequentially. In an HDL, the order does not matter. Like hardware, HDL assignment statements are evaluated any time the inputs, signals on the right hand side, change their value, regardless of the order in which the assignment statements appear in a module.

### 4.2.6 Precedence

Notice that we parenthesized the $cout$ computation in HDL Example 4.7 to define the order of operations as $C_{out} = G + (P \cdot C_{in})$, rather than $C_{out} = (G + P) \cdot C_{in}$. If we had not used parentheses, the default operation order is defined by the language. HDL Example 4.8 specifies operator precedence from highest to lowest for each language. The tables include arithmetic, shift, and comparison operators that will be defined in Chapter 5.
**4.2 Combinational Logic**

### HDL Example 4.8 OPERATOR PRECEDENCE

#### Verilog

<table>
<thead>
<tr>
<th>Op</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>~</td>
<td>NOT</td>
</tr>
<tr>
<td>*, /, %</td>
<td>MUL, DIV, MOD</td>
</tr>
<tr>
<td>+, -</td>
<td>PLUS, MINUS</td>
</tr>
<tr>
<td>&lt;&lt;, &gt;&gt;</td>
<td>Logical Left/Right Shift</td>
</tr>
<tr>
<td>&lt;&lt;&lt;, &gt;&gt;&gt;</td>
<td>Arithmetic Left/Right Shift</td>
</tr>
<tr>
<td>&lt;=, &gt;=</td>
<td>Relative Comparison</td>
</tr>
<tr>
<td>==, !=</td>
<td>Equality Comparison</td>
</tr>
<tr>
<td>&amp; , ~&amp;</td>
<td>AND, NAND</td>
</tr>
<tr>
<td>^, ~^</td>
<td>XOR, XNOR</td>
</tr>
<tr>
<td></td>
<td>OR, NOR</td>
</tr>
<tr>
<td>?:</td>
<td>Conditional</td>
</tr>
</tbody>
</table>

The operator precedence for Verilog is much like you would expect in other programming languages. In particular, AND has precedence over OR. We could take advantage of this precedence to eliminate the parentheses.

```verilog
assign cout = g | p & cin;
```

---

#### VHDL

<table>
<thead>
<tr>
<th>Op</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>not</td>
<td>NOT</td>
</tr>
<tr>
<td>*, /, mod, rem</td>
<td>MUL, DIV, MOD, REM</td>
</tr>
<tr>
<td>+, -</td>
<td>PLUS, MINUS, CONCATENATE</td>
</tr>
<tr>
<td>&amp;</td>
<td>Rotate, Shift logical, Shift arithmetic</td>
</tr>
<tr>
<td>!</td>
<td>Comparison</td>
</tr>
<tr>
<td>and, or, and, nor, xor</td>
<td>Logical Operations</td>
</tr>
</tbody>
</table>

Multiplication has precedence over addition in VHDL, as you would expect. However, unlike Verilog, all of the logical operations (and, or, etc.) have equal precedence, unlike what one might expect in Boolean algebra. Thus, parentheses are necessary; otherwise `cout <= (g or p) and cin` would be interpreted from left to right as `cout <= g or p and cin`.

---

### 4.2.7 Numbers

Numbers can be specified in a variety of bases. Underscores in numbers are ignored and can be helpful in breaking long numbers into more readable chunks. HDL Example 4.9 explains how numbers are written in each language.

### 4.2.8 Z's and X's

HDLs use `z` to indicate a floating value. `z` is particularly useful for describing a tristate buffer, whose output floats when the enable is 0. Recall from Section 2.6 that a bus can be driven by several tristate buffers, exactly one of which should be enabled. HDL Example 4.10 shows the idiom for a tristate buffer. If the buffer is enabled, the output is the same as the input. If the buffer is disabled, the output is assigned a floating value (`z`).
Verilog

Verilog numbers can specify their base and size (the number of bits used to represent them). The format for declaring constants is \( N/b1032value \), where \( N \) is the size in bits, \( b \) is the base, and \( value \) gives the value. For example \( 9/h25 \) indicates a 9-bit number with a value of \( 25_{10} = 000100101_2 \). Verilog supports \('b\) for binary (base 2), \('o\) for octal (base 8), \('d\) for decimal (base 10), and \('h\) for hexadecimal (base 16). If the base is omitted, the base defaults to decimal.

If the size is not given, the number is assumed to have as many bits as the expression in which it is being used. Zeros are automatically padded on the front of the number to bring it up to full size. For example, if \( w \) is a 6-bit bus, assign \( w = 'b11 \) gives \( w \) the value \( 000011 \). It is better practice to explicitly give the size.

<table>
<thead>
<tr>
<th>Numbers</th>
<th>Bits</th>
<th>Base</th>
<th>Val</th>
<th>Stored</th>
</tr>
</thead>
<tbody>
<tr>
<td>'b101</td>
<td>3</td>
<td>2</td>
<td>5</td>
<td>101</td>
</tr>
<tr>
<td>'b11</td>
<td>?</td>
<td>2</td>
<td>3</td>
<td>000...0011</td>
</tr>
<tr>
<td>8'b11</td>
<td>8</td>
<td>2</td>
<td>3</td>
<td>00000011</td>
</tr>
<tr>
<td>8'b1010_1011</td>
<td>8</td>
<td>2</td>
<td>171</td>
<td>10101011</td>
</tr>
<tr>
<td>3'd6</td>
<td>3</td>
<td>10</td>
<td>6</td>
<td>110</td>
</tr>
<tr>
<td>6'42</td>
<td>6</td>
<td>8</td>
<td>34</td>
<td>100010</td>
</tr>
<tr>
<td>8'hAB</td>
<td>8</td>
<td>16</td>
<td>171</td>
<td>10101011</td>
</tr>
<tr>
<td>42</td>
<td>?</td>
<td>10</td>
<td>42</td>
<td>00...0101010</td>
</tr>
</tbody>
</table>

VHDL

In VHDL, STD_LOGIC numbers are written in binary and enclosed in single quotes: ‘0’ and ‘1’ indicate logic 0 and 1. STD_LOGIC_VECTOR numbers are written in binary or hexadecimal and enclosed in double quotation marks. The base is binary by default and can be explicitly defined with the prefix \( \times \) for hexadecimal or \( B \) for binary.

<table>
<thead>
<tr>
<th>Numbers</th>
<th>Bits</th>
<th>Base</th>
<th>Val</th>
<th>Stored</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot;101&quot;</td>
<td>3</td>
<td>2</td>
<td>5</td>
<td>101</td>
</tr>
<tr>
<td>B&quot;101&quot;</td>
<td>3</td>
<td>2</td>
<td>5</td>
<td>101</td>
</tr>
<tr>
<td>X&quot;AB&quot;</td>
<td>8</td>
<td>16</td>
<td>161</td>
<td>10101011</td>
</tr>
</tbody>
</table>

Verilog

module tristate(input [3:0] a, input en, output [3:0] y);

assign y = en ? a : 4'b11;
endmodule

VHDL

library IEEE; use IEEE.STD_LOGIC_1164.all;

declaration tristate is

port(a: in STD_LOGIC_VECTOR(3 downto 0);
en: in STD_LOGIC;
y: out STD_LOGIC_VECTOR(3 downto 0)));

architecture synth of tristate is

begin

y <= "ZZZZ" when en = '0' else a;
end;
Similarly, HDLs use \( x \) to indicate an invalid logic level. If a bus is simultaneously driven to 0 and 1 by two enabled tristate buffers (or other gates), the result is \( x \), indicating contention. If all the tristate buffers driving a bus are simultaneously OFF, the bus will float, indicated by \( z \).

At the start of simulation, state nodes such as flip-flop outputs are initialized to an unknown state (\( x \) in Verilog and \( u \) in VHDL). This is helpful to track errors caused by forgetting to reset a flip-flop before its output is used.

If a gate receives a floating input, it may produce an \( x \) output when it can’t determine the correct output value. Similarly, if it receives an illegal or uninitialized input, it may produce an \( x \) output. HDL Example 4.11 shows how Verilog and VHDL combine these different signal values in logic gates.

**HDL Example 4.11  TRUTH TABLES WITH UNDEFINED AND FLOATING INPUTS**

**Verilog**

Verilog signal values are 0, 1, z, and x. Verilog constants starting with z or x are padded with leading z’s or x’s (instead of 0’s) to reach their full length when necessary.

Table 4.5 shows a truth table for an AND gate using all four possible signal values. Note that the gate can sometimes determine the output despite some inputs being unknown. For example, 0 \& z returns 0 because the output of an AND gate is always 0 if either input is 0. Otherwise, floating or invalid inputs cause invalid outputs, displayed as x in Verilog.

**Table 4.5 Verilog AND gate truth table with z and x**

<table>
<thead>
<tr>
<th>A</th>
<th>0</th>
<th>1</th>
<th>z</th>
<th>x</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>z</td>
<td>0</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>x</td>
<td>0</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
</tbody>
</table>

**VHDL**

VHDL STD_LOGIC signals are ‘0’, ‘1’, ‘z’, ‘x’, and ‘u’.

Table 4.6 shows a truth table for an AND gate using all five possible signal values. Notice that the gate can sometimes determine the output despite some inputs being unknown. For example, ‘0’ and ‘z’ returns ‘0’ because the output of an AND gate is always ‘0’ if either input is ‘0’. Otherwise, floating or invalid inputs cause invalid outputs, displayed as ‘x’ in VHDL. Uninitialized inputs cause uninitialized outputs, displayed as ‘u’ in VHDL.

**Table 4.6 VHDL AND gate truth table with z, x, and u**

<table>
<thead>
<tr>
<th>AND</th>
<th>0</th>
<th>1</th>
<th>z</th>
<th>x</th>
<th>u</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
<td>x</td>
<td>x</td>
<td>x</td>
</tr>
<tr>
<td>z</td>
<td>0</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>u</td>
</tr>
<tr>
<td>x</td>
<td>0</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td>u</td>
</tr>
<tr>
<td>u</td>
<td>0</td>
<td>u</td>
<td>u</td>
<td>u</td>
<td>u</td>
</tr>
</tbody>
</table>
Seeing x or u values in simulation is almost always an indication of a bug or bad coding practice. In the synthesized circuit, this corresponds to a floating gate input, uninitialized state, or contention. The x or u may be interpreted randomly by the circuit as 0 or 1, leading to unpredictable behavior.

### 4.2.9 Bit Swizzling

Often it is necessary to operate on a subset of a bus or to concatenate (join together) signals to form busses. These operations are collectively known as *bit swizzling*. In HDL Example 4.12, y is given the 9-bit value c[2:1] d[0] d[0] d[0] c[0] 101 using bit swizzling operations.

### 4.2.10 Delays

HDL statements may be associated with delays specified in arbitrary units. They are helpful during simulation to predict how fast a circuit will work (if you specify meaningful delays) and also for debugging purposes to understand cause and effect (deducing the source of a bad output is tricky if all signals change simultaneously in the simulation results). These delays are ignored during synthesis; the delay of a gate produced by the synthesizer depends on its $t_{pd}$ and $t_{cd}$ specifications, not on numbers in HDL code.

HDL Example 4.13 adds delays to the original function from HDL Example 4.1, $y = \overline{a} \overline{b} c + a \overline{b} c + a \overline{b} c$. It assumes that inverters have a delay of 1 ns, three-input AND gates have a delay of 2 ns, and three-input OR gates have a delay of 4 ns. Figure 4.10 shows the simulation waveforms, with y lagging 7 ns after the inputs. Note that y is initially unknown at the beginning of the simulation.
4.2 Combinational Logic

4.2.11 VHDL Libraries and Types*

(This section may be skipped by Verilog users.) Unlike Verilog, VHDL enforces a strict data typing system that can protect the user from some errors but that is also clumsy at times.

Despite its fundamental importance, the STD_LOGIC type is not built into VHDL. Instead, it is part of the IEEE.STD_LOGIC_1164 library. Thus, every file must contain the library statements shown in the previous examples.

**HDL Example 4.13 LOGIC GATES WITH DELAYS**

<table>
<thead>
<tr>
<th><strong>Verilog</strong></th>
<th><strong>VHDL</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td><code>timescale 1ns/1ps</code></td>
<td>library IEEE; use IEEE.STD_LOGIC_1164.all;</td>
</tr>
<tr>
<td>module example (input a, b, c, output y);</td>
<td>entity example is</td>
</tr>
<tr>
<td>wire ab, bb, cb, n1, n2, n3;</td>
<td>port (a, b, c: in STD_LOGIC; y: out STD_LOGIC);</td>
</tr>
<tr>
<td>assign @1 (ab, bb, cb) = ~ (a, b, c);</td>
<td>architecture synth of example is</td>
</tr>
<tr>
<td>assign @2 n1 = ab &amp; bb &amp; cb;</td>
<td>signal ab, bb, cb, n1, n2, n3: STD_LOGIC;</td>
</tr>
<tr>
<td>assign @2 n2 = a &amp; bb &amp; cb;</td>
<td>begin</td>
</tr>
<tr>
<td>assign @2 n3 = a &amp; bb &amp; c;</td>
<td>ab &lt;= not a after 1 ns;</td>
</tr>
<tr>
<td>assign @4 y = n1</td>
<td>bb &lt;= not b after 1 ns;</td>
</tr>
<tr>
<td></td>
<td>cb &lt;= not c after 1 ns;</td>
</tr>
<tr>
<td></td>
<td>n1 &lt;= ab and bb and cb after 2 ns;</td>
</tr>
<tr>
<td></td>
<td>n2 &lt;= a and bb and cb after 2 ns;</td>
</tr>
<tr>
<td></td>
<td>n3 &lt;= a and bb and c after 2 ns;</td>
</tr>
<tr>
<td></td>
<td>y &lt;= n1 or n2 or n3 after 4 ns;</td>
</tr>
<tr>
<td>end;</td>
<td>end;</td>
</tr>
</tbody>
</table>

Verilog files can include a timescale directive that indicates the value of each time unit. The statement is of the form `timescale unit/precision`. In this file, each unit is 1 ns, and the simulation has 1 ps precision. If no timescale directive is given in the file, a default unit and precision (usually 1 ns for both) is used. In Verilog, a `#` symbol is used to indicate the number of units of delay. It can be placed in assignment statements, as well as non-blocking (`<=`) and blocking (`=`) assignments, which will be discussed in Section 4.5.4.

In VHDL, the after clause is used to indicate delay. The units, in this case, are specified as nanoseconds.

**Figure 4.10** Example simulation waveforms with delays (from the ModelSim simulator)
Moreover, IEEE.STD_LOGIC_1164 lacks basic operations such as addition, comparison, shifts, and conversion to integers for the STD_LOGIC_VECTOR data. Most CAD vendors have adopted yet more libraries containing these functions: IEEE.STD_LOGIC_UNSIGNED and IEEE.STD_LOGIC_SIGNED. See Section 1.4 for a discussion of unsigned and signed numbers and examples of these operations.

VHDL also has a BOOLEAN type with two values: true and false. BOOLEAN values are returned by comparisons (such as the equality comparison, \texttt{s = '0')} and are used in conditional statements such as \texttt{when}. Despite the temptation to believe a BOOLEAN true value should be equivalent to a STD_LOGIC ‘1’ and BOOLEAN false should mean STD_LOGIC ‘0’, these types are not interchangeable. Thus, the following code is illegal:

\begin{verbatim}
y <= d1 when s else d0;
q <= (state = S2);
\end{verbatim}

Instead, we must write

\begin{verbatim}
y <= d1 when (s = '1') else d0;
q <= '1' when (state = S2) else '0';
\end{verbatim}

Although we do not declare any signals to be BOOLEAN, they are automatically implied by comparisons and used by conditional statements.

Similarly, VHDL has an INTEGER type that represents both positive and negative integers. Signals of type INTEGER span at least the values \(-2^{31}\) to \(2^{31} - 1\). Integer values are used as indices of busses. For example, in the statement

\begin{verbatim}
y <= a(3) and a(2) and a(1) and a(0);
\end{verbatim}

0, 1, 2, and 3 are integers serving as an index to choose bits of the a signal. We cannot directly index a bus with a STD_LOGIC or STD_LOGIC_VECTOR signal. Instead, we must convert the signal to an INTEGER. This is demonstrated in HDL Example 4.14 for an 8:1 multiplexer that selects one bit from a vector using a 3-bit index. The 
\texttt{CONV_INTEGER} function is defined in the IEEE.STD_LOGIC_UNSIGNED library and performs the conversion from STD_LOGIC_VECTOR to INTEGER for positive (unsigned) values.

VHDL is also strict about \texttt{out} ports being exclusively for output. For example, the following code for two and three-input AND gates is illegal VHDL because \texttt{v} is an output and is also used to compute \texttt{w}.

\begin{verbatim}
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity and23 is
  port(a, b, c: in STD_LOGIC;
        v, w:    out STD_LOGIC);
end;
\end{verbatim}
architecture synth of and23 is
begin
  v <= a and b;
  w <= v and c;
end;

VHDL defines a special port type, buffer, to solve this problem. A signal connected to a buffer port behaves as an output but may also be used within the module. The corrected entity definition follows. Verilog does not have this limitation and does not require buffer ports.

entity and23 is
port(a, b, c: in STD_LOGIC;
     v: buffer STD_LOGIC;
     w: out STD_LOGIC);
end;

VHDL supports enumeration types as an abstract way of representing information without assigning specific binary encodings. For example, the divide-by-3 FSM described in Section 3.4.2 uses three states. We can give the states names using the enumeration type rather than referring to them by binary values. This is powerful because it allows VHDL to search for the best state encoding during synthesis, rather than depending on an arbitrary encoding specified by the user.

type statetype is (S0, S1, S2);
signal state, nextstate: statetype;

4.3 STRUCTURAL MODELING

The previous section discussed behavioral modeling, describing a module in terms of the relationships between inputs and outputs. This section
Figure 4.11 mux8 synthesized circuit
examines structural modeling, describing a module in terms of how it is composed of simpler modules.

For example, HDL Example 4.15 shows how to assemble a 4:1 multiplexer from three 2:1 multiplexers. Each copy of the 2:1 multiplexer
is called an *instance*. Multiple instances of the same module are distinguished by distinct names, in this case `lowmux`, `highmux`, and `finalmux`. This is an example of regularity, in which the 2:1 multiplexer is reused many times.

HDL Example 4.16 uses structural modeling to construct a 2:1 multiplexer from a pair of tristate buffers.

**HDL Example 4.16** **STRUCTURAL MODEL OF 2:1 MULTIPLEXER**

**Verilog**

```verilog
module mux2 (input [3:0] d0, d1, s, output [3:0] y);
    tristate t0 (d0, ~s, y);
    tristate t1 (d1, s, y);
endmodule
```

In Verilog, expressions such as `~s` are permitted in the port list for an instance. Arbitrarily complicated expressions are legal but discouraged because they make the code difficult to read.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mux2 is
    port (d0, d1: in STD_LOGIC_VECTOR(3 downto 0); s: in STD_LOGIC; y: out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture struct of mux2 is
    component tristate
        port(a: in STD_LOGIC_VECTOR(3 downto 0); en: in STD_LOGIC; y: out STD_LOGIC_VECTOR(3 downto 0));
    end component;
    signal sbar: STD_LOGIC;
    begin
        sbar <= not s;
        t0: tristate port map (d0, sbar, y);
        t1: tristate port map (d1, s, y);
    end;
```

In VHDL, expressions such as `not s` are not permitted in the port map for an instance. Thus, `sbar` must be defined as a separate signal.
4.3 Structural Modeling

HDL Example 4.17 shows how modules can access part of a bus. An 8-bit wide 2:1 multiplexer is built using two of the 4-bit 2:1 multiplexers already defined, operating on the low and high nibbles of the byte.

In general, complex systems are designed hierarchically. The overall system is described structurally by instantiating its major components. Each of these components is described structurally from its building blocks, and so forth recursively until the pieces are simple enough to describe behaviorally. It is good style to avoid (or at least to minimize) mixing structural and behavioral descriptions within a single module.

**HDL Example 4.17  ACCESSING PARTS OF BUSES**

**Verilog**

```verilog
module mux2_8 (input [7:0] d0, d1, input s, output [7:0] y);
mux2 lsbmux (d0[3:0], d1[3:0], s, y[3:0]);
mux2 msbmux (d0[7:4], d1[7:4], s, y[7:4]);
endmodule
```

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux2_8 is
port(d0, d1: in STD_LOGIC_VECTOR(7 downto 0); s: in STD_LOGIC; y: out STD_LOGIC_VECTOR(7 downto 0));
end;
architecture struct of mux2_8 is
component mux2
port(d0, d1: in STD_LOGIC_VECTOR(3 downto 0); s: in STD_LOGIC; y: out STD_LOGIC_VECTOR(3 downto 0));
end component;
begin
lsbmux: mux2
port map(d0(3 downto 0), d1(3 downto 0), s, y(3 downto 0));
msbmux: mux2
port map(d0(7 downto 4), d1(7 downto 4), s, y(7 downto 4));
end;
```
4.4 SEQUENTIAL LOGIC

HDL synthesizers recognize certain idioms and turn them into specific sequential circuits. Other coding styles may simulate correctly but synthesize into circuits with blatant or subtle errors. This section presents the proper idioms to describe registers and latches.

4.4.1 Registers

The vast majority of modern commercial systems are built with registers using positive edge-triggered D flip-flops. HDL Example 4.18 shows the idiom for such flip-flops.

In Verilog always statements and VHDL process statements, signals keep their old value until an event in the sensitivity list takes place that explicitly causes them to change. Hence, such code, with appropriate sensitivity lists, can be used to describe sequential circuits with memory. For example, the flip-flop includes only clk in the sensitive list. It remembers its old value of q until the next rising edge of the clk, even if d changes in the interim.

In contrast, Verilog continuous assignment statements (assign) and VHDL concurrent assignment statements (<=) are reevaluated anytime any of the inputs on the right hand side changes. Therefore, such code necessarily describes combinational logic.
A Verilog always statement is written in the form
always @ (sensitivity list) statement;

The statement is executed only when the event specified in the sensitivity list occurs. In this example, the statement is $q \leftarrow d$ (pronounced “q gets d”). Hence, the flip-flop copies $d$ to $q$ on the positive edge of the clock and otherwise remembers the old state of $q$.

$\leftarrow$ is called a nonblocking assignment. Think of it as a regular $=$ sign for now; we'll return to the more subtle points in Section 4.5.4. Note that $\leftarrow$ is used instead of assign inside an always statement.

All signals on the left hand side of $\leftarrow$ or $=$ in an always statement must be declared as reg. In this example, $q$ is both an output and a reg, so it is declared as output reg [3:0] $q$. Declaring a signal as reg does not mean the signal is actually the output of a register! All it means is that the signal appears on the left hand side of an assignment in an always statement. We will see later examples of always statements describing combinational logic in which the output is declared reg but does not come from a flip-flop.

A VHDL process is written in the form
process(sensitivity list) begin statement; end process;

The statement is executed when any of the variables in the sensitivity list change. In this example, the if statement is executed when $clk$ changes, indicated by $clk'$event. If the change is a rising edge ($clk = '1' after the event), then $q \leftarrow d$ (pronounced “q gets d”). Hence, the flip-flop copies $d$ to $q$ on the positive edge of the clock and otherwise remembers the old state of $q$.

An alternative VHDL idiom for a flip-flop is
process(clk) begin if RISING_EDGE(clk) then $q \leftarrow d$; end if; end process;

RISING_EDGE(clk) is synonymous with $clk'$event and $clk = 1$.

---

**4.4.2 Resettable Registers**

When simulation begins or power is first applied to a circuit, the output of a flop or register is unknown. This is indicated with $x$ in Verilog and ‘u’ in VHDL. Generally, it is good practice to use resettable registers so that on powerup you can put your system in a known state. The reset may be
either asynchronous or synchronous. Recall that asynchronous reset occurs immediately, whereas synchronous reset clears the output only on the next rising edge of the clock. HDL Example 4.19 demonstrates the idioms for flip-flops with asynchronous and synchronous resets. Note that distinguishing synchronous and asynchronous reset in a schematic can be difficult. The schematic produced by Synplify Pro places asynchronous reset at the bottom of a flip-flop and synchronous reset on the left side.

**HDL Example 4.19**  
RESETTABLE REGISTER

### Verilog

```verilog
module flopr(input clk,  
             input reset,  
             input [3:0] d,  
             output reg [3:0] q);

// asynchronous reset  
always @ (posedge clk, posedge reset)  
if(reset) q = 4'b0;  
else q = d;
endmodule

module flopr (input clk,  
              input reset,  
              input [3:0] d,  
              output reg [3:0] q);

// synchronous reset  
always @ (posedge clk)  
if (reset) q = 4'b0;  
else q = d;
endmodule
```

Multiple signals in an always statement sensitivity list are separated with a comma or the word or. Notice that posedge reset is in the sensitivity list on the asynchronously resettable flop, but not on the synchronously resettable flop. Thus, the asynchronously resettable flop immediately responds to a rising edge on reset, but the synchronously resettable flop responds to reset only on the rising edge of the clock.

Because the modules have the same name, `flopr`, you may include only one or the other in your design.

### VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity flopr is  
  port(clk,  
       reset: in STD_LOGIC;  
       d: in STD_LOGIC_VECTOR(3 downto 0);  
       q: out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture asynchronous of flopr is  
begin  
  process (clk, reset) begin  
    if reset = '1' then  
      q <= "0000";
    elsif clk'event and clk = '1' then  
      q <= d;
    end if;
  end process;
end;

architecture synchronous of flopr is  
begin  
  process (clk) begin  
    if clk'event and clk = '1' then  
      if reset = '1' then  
        q <= "0000";
      elsif clk'event and clk = '1' then  
        q <= d;
      end if;
    end if;
  end process;
end;
```

Multiple signals in a process sensitivity list are separated with a comma. Notice that reset is in the sensitivity list on the asynchronously resettable flop, but not on the synchronously resettable flop. Thus, the asynchronously resettable flop immediately responds to a rising edge on reset, but the synchronously resettable flop responds to reset only on the rising edge of the clock.

Recall that the state of a flop is initialized to 'u' at startup during VHDL simulation.

As mentioned earlier, the name of the architecture (asynchronous or synchronous, in this example) is ignored by the VHDL tools but may be helpful to the human reading the code. Because both architectures describe the entity `flopr`, you may include only one or the other in your design.
4.4.3 Enabled Registers

Enabled registers respond to the clock only when the enable is asserted. HDL Example 4.20 shows an asynchronously resettable enabled register that retains its old value if both reset and en are FALSE.

**HDL Example 4.20 RESETTABLE ENABLED REGISTER**

<table>
<thead>
<tr>
<th>Verilog</th>
<th>VHDL</th>
</tr>
</thead>
<tbody>
<tr>
<td>module flopr(input clk, input reset, input en, input [3:0] d, output reg [3:0] q); // asynchronous reset always @(posedge clk, posedge reset) if(reset) q &lt;= 4'b0; else if(en) q &lt;= d; endmodule</td>
<td>library IEEE; use IEEE.STD_LOGIC_1164.all; entity flopr is port(clk, reset, en: in STD_LOGIC; d: in STD_LOGIC_VECTOR(3 downto 0); q: out STD_LOGIC_VECTOR(3 downto 0)); end; architecture asynchronous of flopr is begin process(clk, reset)begin if reset = '1' then q &lt;= &quot;0000&quot;; elsif clk'event and clk = '1' then if en = '1' then q &lt;= d; end if; end if; end process; end;</td>
</tr>
</tbody>
</table>
4.4.4 Multiple Registers

A single always/process statement can be used to describe multiple pieces of hardware. For example, consider the synchronizer from Section 3.5.5 made of two back-to-back flip-flops, as shown in Figure 4.19. HDL Example 4.21 describes the synchronizer. On the rising edge of clk, d is copied to n1. At the same time, n1 is copied to q.

HDL Example 4.21 SYNCHRONIZER

Verilog

```verilog
module sync(input clk,
    input d,
    output reg q);

reg n1;
always @ (posedge clk)
begin
    n1 <= d;
    q <= n1;
end
endmodule
```

In Verilog, n1 must be declared as a reg because it is an internal signal used on the left hand side of <= in an always statement. Also notice that the begin/end construct is necessary because multiple statements appear in the always statement. This is analogous to { } in C or Java. The begin/end was not needed in the flopr example because if/else counts as a single statement.

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity sync is
port(clk: in STD_LOGIC;
    d: in STD_LOGIC;
    q: out STD_LOGIC);
end;

architecture good of sync is
signal n1: STD_LOGIC;
begin
process(clk) begin
    if clk'event and clk = '1' then
        n1 <= d;
        q <= n1;
    end if;
end process;
end;
```

In VHDL, n1 must be declared as a signal because it is an internal signal used in the module.
4.4.5 Latches

Recall from Section 3.2.2 that a D latch is transparent when the clock is HIGH, allowing data to flow from input to output. The latch becomes opaque when the clock is LOW, retaining its old state. HDL Example 4.22 shows the idiom for a D latch.

Not all synthesis tools support latches well. Unless you know that your tool does support latches and you have a good reason to use them, avoid them and use edge-triggered flip-flops instead. Furthermore, take care that your HDL does not imply any unintended latches, something that is easy to do if you aren’t attentive. Many synthesis tools warn you when a latch is created; if you didn’t expect one, track down the bug in your HDL.

4.5 MORE COMBINATIONAL LOGIC

In Section 4.2, we used assignment statements to describe combinational logic behaviorally. Verilog always statements and VHDL process statements are used to describe sequential circuits, because they remember the old state when no new state is prescribed. However, always/process

HDL Example 4.22 D LATCH

Verilog

module latch(input clk, input [3:0] d, output reg [3:0] q);
    always @ (clk, d)
        if (clk) q <= d;
    endmodule

The sensitivity list contains both clk and d, so the always statement evaluates any time clk or d changes. If clk is HIGH, d flows through to q.

q must be declared to be a reg because it appears on the left hand side of <= in an always statement. This does not always mean that q is the output of a register.

VHDL

library IEEE; use IEEE.STD_LOGIC_1164.all;

entity latch is
    port(clk: in STD_LOGIC;
         d: in STD_LOGIC_VECTOR(3 downto 0);
         q: out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture synth of latch is
begin
    process (clk, d) begin
        if clk = '1' then q <= d;
    end if;
end process;

end;

The sensitivity list contains both clk and d, so the process evaluates anytime clk or d changes. If clk is HIGH, d flows through to q.

Figure 4.21 latch synthesized circuit
Statements can also be used to describe combinational logic behaviorally if the sensitivity list is written to respond to changes in all of the inputs and the body prescribes the output value for every possible input combination. HDL Example 4.23 uses `always/process` statements to describe a bank of four inverters (see Figure 4.3 for the synthesized circuit).

HDLs support blocking and nonblocking assignments in an `always/process` statement. A group of blocking assignments are evaluated in the order in which they appear in the code, just as one would expect in a standard programming language. A group of nonblocking assignments are evaluated concurrently; all of the statements are evaluated before any of the signals on the left hand sides are updated.

HDL Example 4.24 defines a full adder using intermediate signals `p` and `g` to compute `s` and `cout`. It produces the same circuit from Figure 4.8, but uses `always/process` statements in place of assignment statements.

These two examples are poor applications of `always/process` statements for modeling combinational logic because they require more lines than the equivalent approach with assignment statements from Section 4.2.1. Moreover, they pose the risk of inadvertently implying sequential logic if the inputs are left out of the sensitivity list. However, `case` and `if` statements are convenient for modeling more complicated combinational logic. `case` and `if` statements must appear within `always/process` statements and are examined in the next sections.
In a Verilog always statement, = indicates a blocking assignment and <= indicates a nonblocking assignment (also called a concurrent assignment).

Do not confuse either type with continuous assignment using the assign statement. assign statements must be used outside always statements and are also evaluated concurrently.

In a VHDL process statement, := indicates a blocking assignment and = indicates a nonblocking assignment (also called a concurrent assignment). This is the first section where := is introduced.

Nonblocking assignments are made to outputs and to signals. Blocking assignments are made to variables, which are declared in process statements (see HDL Example 4.24).

<= can also appear outside process statements, where it is also evaluated concurrently.

**HDL Example 4.24 FULL ADDER USING always/process**

**Verilog**

```verilog
module fulladder(input a, b, cin, output reg s, cout);
    reg p, g;
    always @ (*)
    begin
        p = a ^ b; // blocking
        g = a & b; // blocking
        s = p ^ cin; // blocking
        cout = g | (p & cin); // blocking
    end
endmodule
```

In this case, an @ (a, b, cin) would have been equivalent to @ (*). However, @ (*) is better because it avoids common mistakes of missing signals in the stimulus list.

For reasons that will be discussed in Section 4.5.4, it is best to use blocking assignments for combinational logic. This example uses blocking assignments, first computing p, then g, then s, and finally cout.

Because p and g appear on the left hand side of an assignment in an always statement, they must be declared to be reg.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity fulladder is
    port(a, b, cin: in STD_LOGIC;
        s, cout: out STD_LOGIC);
end;
architecture synth of fulladder is
begin
    process(a, b, cin)
    variable p, g: STD_LOGIC;
    begin
        p := a xor b; -- blocking
        g := a and b; -- blocking
        s <= p xor cin;
        cout <= g or (p and cin);
    end process;
end;
```

The process sensitivity list must include a, b, and cin because combinational logic should respond to changes of any input.

For reasons that will be discussed in Section 4.5.4, it is best to use blocking assignments for intermediate variables in combinational logic. This example uses blocking assignments for p and g so that they get their new values before being used to compute s and cout that depend on them.

Because p and g appear on the left hand side of a blocking assignment (=) in a process statement, they must be declared to be variable rather than signal. The variable declaration appears before the begin in the process where the variable is used.
4.5.1 Case Statements

A better application of using the `always/process` statement for combinational logic is a seven-segment display decoder that takes advantage of the case statement that must appear inside an always/process statement.

As you might have noticed in Example 2.10, the design process for large blocks of combinational logic is tedious and prone to error. HDLs offer a great improvement, allowing you to specify the function at a higher level of abstraction, and then automatically synthesize the function into gates. HDL Example 4.25 uses case statements to describe a seven-segment display decoder based on its truth table. (See Example 2.10 for a description of the seven-segment display decoder.) The case

HDL Example 4.25 SEVEN-SEGMENT DISPLAY DECODER

Verilog

```verilog
module sevenseg(input [3:0] data, output reg [6:0] segments);
always @ (*)
case (data)
  // abc_defg
  // segments
  0: segments = 7'b111_1110;
  1: segments = 7'b011_0000;
  2: segments = 7'b110_1101;
  3: segments = 7'b111_1001;
  4: segments = 7'b011_0011;
  5: segments = 7'b101_1011;
  6: segments = 7'b101_1111;
  7: segments = 7'b111_0000;
  8: segments = 7'b111_1111;
  9: segments = 7'b111_1011;
  default: segments = 7'b000_0000;
endcase
endmodule
```

The case statement checks the value of data. When data is 0, the statement performs the action after the colon, setting segments to 1111110. The case statement similarly checks other data values up to 9 (note the use of the default base, base 10).

The **default** clause is a convenient way to define the output for all cases not explicitly listed, guaranteeing combinational logic.

In Verilog, case statements must appear inside always statements.

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity seven_seg_decoder is
  port(data: in STD_LOGIC_VECTOR(3 downto 0);
       segments: out STD_LOGIC_VECTOR(6 downto 0));
end;

architecture synth of seven_seg_decoder is
begin
  process (data) begin
    case data is
      // abc_defg
      // segments
      when X"0" => segments <= "1111110";
      when X"1" => segments <= "0110000";
      when X"2" => segments <= "1011011";
      when X"3" => segments <= "1111001";
      when X"4" => segments <= "0110011";
      when X"5" => segments <= "1011011";
      when X"6" => segments <= "1011111";
      when X"7" => segments <= "1110000";
      when X"8" => segments <= "1111111";
      when X"9" => segments <= "1111011";
      when others => segments <= "0000000";
    end case;
  end process;
end;
```

The case statement checks the value of data. When data is 0, the statement performs the action after the `=>`, setting segments to 1111110. The case statement similarly checks other data values up to 9 (note the use of X for hexadecimal numbers). The **others** clause is a convenient way to define the output for all cases not explicitly listed, guaranteeing combinational logic.

Unlike Verilog, VHDL supports selected signal assignment statements (see HDL Example 4.6), which are much like case statements but can appear outside processes. Thus, there is less reason to use processes to describe combinational logic.
A case statement performs different actions depending on the value of its input. A case statement implies combinational logic if all possible input combinations are defined; otherwise it implies sequential logic, because the output will keep its old value in the undefined cases.

Synplify Pro synthesizes the seven-segment display decoder into a read-only memory (ROM) containing the 7 outputs for each of the 16 possible inputs. ROMs are discussed further in Section 5.5.6.

If the default or others clause were left out of the case statement, the decoder would have remembered its previous output anytime data were in the range of 10–15. This is strange behavior for hardware.

Ordinary decoders are also commonly written with case statements. HDL Example 4.26 describes a 3:8 decoder.

4.5.2 If Statements

always/process statements may also contain if statements. The if statement may be followed by an else statement. If all possible input

**HDL Example 4.26 3:8 DECODER**

<table>
<thead>
<tr>
<th>Verilog</th>
<th>VHDL</th>
</tr>
</thead>
<tbody>
<tr>
<td>module decoder3_8(input [2:0] a, output reg [7:0] y);</td>
<td>library IEEE; use IEEE.STD_LOGIC_1164.all;</td>
</tr>
<tr>
<td>always @ (*)</td>
<td>entity decoder3_8 is</td>
</tr>
<tr>
<td>case (a)</td>
<td>port (a: in STD_LOGIC_VECTOR(2 downto 0));</td>
</tr>
<tr>
<td>3'b000: y = 8'b00000001;</td>
<td>y: out STD_LOGIC_VECTOR(7 downto 0));</td>
</tr>
<tr>
<td>3'b001: y = 8'b00000010;</td>
<td>end;</td>
</tr>
<tr>
<td>3'b010: y = 8'b00000100;</td>
<td>architecture synth of decoder3_8 is</td>
</tr>
<tr>
<td>3'b011: y = 8'b00001000;</td>
<td>begin</td>
</tr>
<tr>
<td>3'b100: y = 8'b00010000;</td>
<td>process (a) begin</td>
</tr>
<tr>
<td>3'b101: y = 8'b00100000;</td>
<td>case a is</td>
</tr>
<tr>
<td>3'b110: y = 8'b01000000;</td>
<td>when &quot;000&quot; =&gt; y &lt;= &quot;00000001&quot;;</td>
</tr>
<tr>
<td>3'b111: y = 8'b10000000;</td>
<td>when &quot;001&quot; =&gt; y &lt;= &quot;00000010&quot;;</td>
</tr>
<tr>
<td></td>
<td>when &quot;010&quot; =&gt; y &lt;= &quot;00000100&quot;;</td>
</tr>
<tr>
<td></td>
<td>when &quot;011&quot; =&gt; y &lt;= &quot;00010000&quot;;</td>
</tr>
<tr>
<td></td>
<td>when &quot;100&quot; =&gt; y &lt;= &quot;00100000&quot;;</td>
</tr>
<tr>
<td></td>
<td>when &quot;101&quot; =&gt; y &lt;= &quot;01000000&quot;;</td>
</tr>
<tr>
<td></td>
<td>when &quot;110&quot; =&gt; y &lt;= &quot;10000000&quot;;</td>
</tr>
<tr>
<td></td>
<td>end case</td>
</tr>
<tr>
<td></td>
<td>end case</td>
</tr>
<tr>
<td></td>
<td>end process</td>
</tr>
<tr>
<td></td>
<td>end;</td>
</tr>
<tr>
<td></td>
<td>No default statement is needed because all cases are covered.</td>
</tr>
</tbody>
</table>

No others clause is needed because all cases are covered.
Figure 4.23 decoder3_8 synthesized circuit
4.5 More Combinational Logic

More combinations are handled, the statement implies combinational logic; otherwise, it produces sequential logic (like the latch in Section 4.4.5).

HDL Example 4.27 uses if statements to describe a priority circuit, defined in Section 2.4. Recall that an N-input priority circuit sets the output TRUE that corresponds to the most significant input that is TRUE.

**4.5.3 Verilog casez**

(This section may be skipped by VHDL users.) Verilog also provides the casez statement to describe truth tables with don’t cares (indicated with ? in the casez statement). HDL Example 4.28 shows how to describe a priority circuit with casez.

Synplify Pro synthesizes a slightly different circuit for this module, shown in Figure 4.25, than it did for the priority circuit in Figure 4.24. However, the circuits are logically equivalent.

**4.5.4 Blocking and Nonblocking Assignments**

The guidelines on page 203 explain when and how to use each type of assignment. If these guidelines are not followed, it is possible to write
code that appears to work in simulation but synthesizes to incorrect hardware. The optional remainder of this section explains the principles behind the guidelines.

**Combinational Logic**

The full adder from HDL Example 4.24 is correctly modeled using blocking assignments. This section explores how it operates and how it would differ if nonblocking assignments had been used.

Imagine that a, b, and cin are all initially 0. p, g, s, and cout are thus 0 as well. At some time, a changes to 1, triggering the always/process statement. The four blocking assignments evaluate in
4.5 More Combinational Logic

Verilog

1. Use `always @ (posedge clk)` and nonblocking assignments to model synchronous sequential logic.

   ```verilog
   always @ (posedge clk)
   begin
       nl <= d; // nonblocking
       q <= nl; // nonblocking
   end
   ```

2. Use continuous assignments to model simple combinational logic.

   ```verilog
   assign y = s ? d1 : d0;
   ```

3. Use `always @ (*)` and blocking assignments to model more complicated combinational logic where the `always` statement is helpful.

   ```verilog
   always @ (*)
   begin
       p = a & b; // blocking
       g = a & b; // blocking
       s = p & cin;
       cout = g | (p & cin);
   end
   ```

4. Do not make assignments to the same signal in more than one `always` statement or continuous assignment statement.

VHDL

1. Use `process (clk)` and nonblocking assignments to model synchronous sequential logic.

   ```vhdl
   process (clk) begin
       if clk'event and clk = '1' then
           nl <= d; -- nonblocking
           q <= nl; -- nonblocking
       end if;
   end process;
   ```

2. Use concurrent assignments outside `process` statements to model simple combinational logic.

   ```vhdl
   y <= d0 when s = '0' else d1;
   ```

3. Use `process (in1, in2, ...)` to model more complicated combinational logic where the `process` is helpful. Use blocking assignments for internal variables.

   ```vhdl
   process (a, b, cin)
   variable p, g: STD_LOGIC;
   begin
       p := a xor b; -- blocking
       g := a and b; -- blocking
       s <= p xor cin;
       cout <= g or (p and cin);
   end process;
   ```

4. Do not make assignments to the same variable in more than one `process` or concurrent assignment statement.
In contrast, HDL Example 4.29 illustrates the use of nonblocking assignments.

Now consider the same case of a rising from 0 to 1 while b and cin are 0. The four nonblocking assignments evaluate concurrently:

\[
\begin{align*}
1. \quad & p \leftarrow 1 \oplus 0 = 1 \\
2. \quad & g \leftarrow 1 \cdot 0 = 0 \\
3. \quad & s \leftarrow 1 \oplus 0 = 1 \\
4. \quad & cout \leftarrow 0 + 1 \cdot 0 = 0
\end{align*}
\]

Observe that s is computed concurrently with p and hence uses the old value of p, not the new value. Therefore, s remains 0 rather than

HDL Example 4.29 | FULL ADDER USING NONBLOCKING ASSIGNMENTS

**Verilog**

```verilog
// nonblocking assignments (not recommended)
module fulladder (input a, b, cin, output reg s, cout);
  reg p, g;
  always @ (*)
  begin
    p <= a xor b; // nonblocking
    g <= a & b; // nonblocking
    s <= p ^ cin;
    cout <= g | (p & cin);
  end
endmodule
```

Because p and g appear on the left hand side of an assignment in an always statement, they must be declared to be reg.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity fulladder is
  port(a, b, cin: in STD_LOGIC;
       s, cout: out STD_LOGIC);
end;

architecture nonblocking of fulladder is
  signal p, g: STD_LOGIC;
  begin
    process(a, b, cin, p, g) begin
      p <= a xor b; -- nonblocking
      g <= a and b; -- nonblocking
      s <= p xor cin;
      cout <= g or (p and cin);
    end process;
  end;
```

Because p and g appear on the left hand side of a nonblocking assignment in a process statement, they must be declared to be signal rather than variable. The signal declaration appears before the begin in the architecture, not the process.
becoming 1. However, \( p \) does change from 0 to 1. This change triggers the `always/process` statement to evaluate a second time, as follows:

\[
p \leftarrow 1 \oplus 0 = 1 \quad g \leftarrow 1 \cdot 0 = 0 \quad s \leftarrow 1 \oplus 0 = 1 \quad \text{cout} \leftarrow 0 + 1 \cdot 0 = 0
\]

This time, \( p \) is already 1, so \( s \) correctly changes to 1. The nonblocking assignments eventually reach the right answer, but the `always/process` statement had to evaluate twice. This makes simulation slower, though it synthesizes to the same hardware.

Another drawback of nonblocking assignments in modeling combinational logic is that the HDL will produce the wrong result if you forget to include the intermediate variables in the sensitivity list.

<table>
<thead>
<tr>
<th>Verilog</th>
<th>VHDL</th>
</tr>
</thead>
<tbody>
<tr>
<td>If the sensitivity list of the <code>always</code> statement in HDL Example 4.29 were written as <code>always @ (a, b, cin)</code> rather than <code>always @ (*)</code>, then the statement would not reevaluate when ( p ) or ( g ) changes. In the previous example, ( s ) would be incorrectly left at 0, not 1.</td>
<td>If the sensitivity list of the <code>process</code> statement in HDL Example 4.29 were written as <code>process (a, b, cin)</code> rather than <code>process (a, b, cin, p, g)</code>, then the statement would not reevaluate when ( p ) or ( g ) changes. In the previous example, ( s ) would be incorrectly left at 0, not 1.</td>
</tr>
</tbody>
</table>

Worse yet, some synthesis tools will synthesize the correct hardware even when a faulty sensitivity list causes incorrect simulation. This leads to a mismatch between the simulation results and what the hardware actually does.

**Sequential Logic**

The synchronizer from HDL Example 4.21 is correctly modeled using nonblocking assignments. On the rising edge of the clock, \( d \) is copied to \( n1 \) at the same time that \( n1 \) is copied to \( q \), so the code properly describes two registers. For example, suppose initially that \( d = 0 \), \( n1 = 1 \), and \( q = 0 \). On the rising edge of the clock, the following two assignments occur concurrently, so that after the clock edge, \( n1 = 0 \) and \( q = 1 \).

\[
n1 \leftarrow d = 0 \quad q \leftarrow n1 = 1
\]

HDL Example 4.30 tries to describe the same module using blocking assignments. On the rising edge of \( clk \), \( d \) is copied to \( n1 \). Then this new value of \( n1 \) is copied to \( q \), resulting in \( d \) improperly appearing at both \( n1 \) and \( q \). The assignments occur one after the other so that after the clock edge, \( q = n1 = 0 \).

1. \( n1 \leftarrow d = 0 \)
2. \( q \leftarrow n1 = 0 \)
Because \( n_1 \) is invisible to the outside world and does not influence the behavior of \( q \), the synthesizer optimizes it away entirely, as shown in Figure 4.26.

The moral of this illustration is to exclusively use nonblocking assignment in always statements when modeling sequential logic. With sufficient cleverness, such as reversing the orders of the assignments, you could make blocking assignments work correctly, but blocking assignments offer no advantages and only introduce the risk of unintended behavior. Certain sequential circuits will not work with blocking assignments no matter what the order.

4.6 **FINITE STATE MACHINES**

Recall that a finite state machine (FSM) consists of a state register and two blocks of combinational logic to compute the next state and the output given the current state and the input, as was shown in Figure 3.22. HDL descriptions of state machines are correspondingly divided into three parts to model the state register, the next state logic, and the output logic.
4.6 Finite State Machines

HDL Example 4.31 DIVIDE-BY-3 FINITE STATE MACHINE

Verilog

```verilog
module divideby3FSM(input clk, input reset, output y);
reg [1:0] state, nextstate;
parameter S0 = 'b00;
parameter S1 = 'b01;
parameter S2 = 'b10;
// state register
always @(posedge clk, posedge reset)
if (reset)
  state = S0;
else
  state = nextstate;
// next state logic
always @(*)
case (state)
  S0: nextstate = S1;
  S1: nextstate = S2;
  S2: nextstate = S0;
  default: nextstate = S0;
endcase
// output logic
assign y = (state == S0);
endmodule
```

The parameter statement is used to define constants within a module. Naming the states with parameters is not required, but it makes changing state encodings much easier and makes the code more readable.

Notice how a case statement is used to define the state transition table. Because the next state logic should be combinational, a default is necessary even though the state 'b11 should never arise.

The output, y, is 1 when the state is S0. The equality comparison a == b evaluates to 1 if a equals b and 0 otherwise. The inequality comparison a != b does the inverse, evaluating to 1 if a does not equal b.

HDL Example 4.31 describes the divide-by-3 FSM from Section 3.4.2. It provides an asynchronous reset to initialize the FSM. The state register uses the ordinary idiom for flip-flops. The next state and output logic blocks are combinational.

The Synplify Pro Synthesis tool just produces a block diagram and state transition diagram for state machines; it does not show the logic gates or the inputs and outputs on the arcs and states. Therefore, be careful that you have specified the FSM correctly in your HDL code. The state transition diagram in Figure 4.27 for the divide-by-3 FSM is analogous to the diagram in Figure 3.28(b). The double circle indicates that

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity divideby3FSM is
  port(clk, reset: in STD_LOGIC;
       y: out STD_LOGIC);
end;
architecture synth of divideby3FSM is
  type statetype is (S0, S1, S2);
signal state, nextstate: statetype;
begin
  -- state register
  process (clk, reset) begin
    if reset = '1' then state <= S0;
    elsif clk'event and clk = '1' then
      state <= nextstate;
    end if;
  end process;
  -- next state logic
  if (reset = '1') then
    nextstate <= S0;
  elsif clk'event and clk = '1' then
    nextstate <= S1 when state = S0 else
                S2 when state = S1 else
                S0;
  end if;
  -- output logic
  y <= '1' when state = S0 else '0';
end;
```

This example defines a new enumeration data type, statetype, with three possibilities: S0, S1, and S2. state and nextstate are statetype signals. By using an enumeration instead of choosing the state encoding, VHDL frees the synthesizer to explore various state encodings to choose the best one.

The output, y, is 1 when the state is S0. The inequality-comparison uses /=. To produce an output of 1 when the state is anything but S0, change the comparison to state /= S0.

Notice that the synthesis tool uses a 3-bit encoding (Q[2:0]) instead of the 2-bit encoding suggested in the Verilog code.
S0 is the reset state. Gate-level implementations of the divide-by-3 FSM were shown in Section 3.4.2.

If, for some reason, we had wanted the output to be HIGH in states S0 and S1, the output logic would be modified as follows.

Verilog

```verilog
// Output Logic
assign y = (state == S0 | state == S1);
```

VHDL

```vhdl
-- output logic
y <= '1' when (state = S0 or state = S1) else '0';
```

The next two examples describe the snail pattern recognizer FSM from Section 3.4.3. The code shows how to use case and if statements to handle next state and output logic that depend on the inputs as well as the current state. We show both Moore and Mealy modules. In the Moore machine (HDL Example 4.32), the output depends only on the current state, whereas in the Mealy machine (HDL Example 4.33), the output logic depends on both the current state and inputs.
HDL Example 4.32  PATTERN RECOGNIZER MOORE FSM

Verilog

module patternMoore(input clk,
                      input reset,
                      input a,
                      output y);
  reg [2:0] state, nextstate;
  parameter S0 = 3'b000;
  parameter S1 = 3'b001;
  parameter S2 = 3'b010;
  parameter S3 = 3'b011;
  parameter S4 = 3'b100;

  // state register
  always @ (posedge clk, posedge reset)
    if (reset) state <= S0;
    else state <= nextstate;

  // next state logic
  always @ (*)
    case (state)
      S0: if (a) nextstate = S1;
         else nextstate = S0;
      S1: if (a) nextstate = S2;
         else nextstate = S0;
      S2: if (a) nextstate = S2;
         else nextstate = S3;
      S3: if (a) nextstate = S4;
         else nextstate = S0;
      S4: if (a) nextstate = S2;
         else nextstate = S0;
      default: nextstate = S0;
    endcase

  // output logic
  assign y = (state == S4);
endmodule

Note how nonblocking assignments (<=) are used in the state register to describe sequential logic, whereas blocking assignments (=) are used in the next state logic to describe combinational logic.

VHDL

library IEEE; use IEEE.STD_LOGIC_1164.all;

entity patternMoore is
  port(clk, reset: in STD_LOGIC;
       a: in STD_LOGIC;
       y: out STD_LOGIC);
end;

architecture synth of patternMoore is
  type statetype is (S0, S1, S2, S3, S4);
  signal state, nextstate: statetype;

  begin
    -- state register
    process (clk, reset) begin
      if reset = '1' then state <= S0;
      elsif clk'event and clk = '1' then
        state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(state, a) begin
    case state is
      when S0 => if a = '1' then
                 nextstate <= S1;
                 else nextstate <= S0;
                 end if;
      when S1 => if a = '1' then
                 nextstate <= S2;
                 else nextstate <= S0;
                 end if;
      when S2 => if a = '1' then
                 nextstate <= S2;
                 else nextstate <= S3;
                 end if;
      when S3 => if a = '1' then
                 nextstate <= S4;
                 else nextstate <= S0;
                 end if;
      when S4 => if a = '1' then
                 nextstate <= S2;
                 else nextstate <= S0;
                 end if;
      when others => nextstate <= S0;
    end case;
  end process;

  -- output logic
  y <= '1' when state = S4 else '0';
end;

Figure 4.28  patternMoore synthesized circuit
HDL Example 4.33  PATTERN RECOGNIZER MEALY FSM

**Verilog**

```verilog
module patternMealy(input clk, input reset, input a, output y);

reg [1:0] state, nextstate;

parameter S0 = 'b00;
parameter S1 = 'b01;
parameter S2 = 'b10;
parameter S3 = 'b11;

// state register
always @ (posedge clk, posedge reset)
if (reset) state <= S0;
else state <= nextstate;

// next state logic
always @ (*)
case (state)
S0: if (a) nextstate <= S1;
else nextstate <= S0;
S1: if (a) nextstate <= S2;
else nextstate <= S0;
S2: if (a) nextstate <= S2;
else nextstate <= S3;
S3: if (a) nextstate <= S1;
else nextstate <= S0;
default: nextstate <= S0;
endcase

// output logic
assign y = (a & state == S3);
endmodule
```

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity patternMealy is
port(clk, reset: in STD_LOGIC;
a: in STD_LOGIC;
y: out STD_LOGIC);
end;

architecture synth of patternMealy is

type statetype is (S0, S1, S2, S3);
signal state, nextstate: statetype;

begin

-- state register
process (clk, reset) begin
if reset = '1' then state <= S0;
else state <= nextstate;
end if;
end process;

-- next state logic
process(state, a) begin
case state is
when S0 => if a = '1' then
nextstate <= S1;
else nextstate <= S0;
end if;
when S1 => if a = '1' then
nextstate <= S2;
else nextstate <= S0;
end if;
when S2 => if a = '1' then
nextstate <= S2;
else nextstate <= S3;
end if;
when S3 => if a = '1' then
nextstate <= S1;
else nextstate <= S0;
end if;
when others => nextstate <= S0;
end case;
end process;

-- output logic
y <= '1' when (a = '1' and state = S3) else '0';
end;
```

*Figure 4.29* patternMealy synthesized circuit
4.7 PARAMETERIZED MODULES

So far all of our modules have had fixed-width inputs and outputs. For example, we had to define separate modules for 4- and 8-bit wide 2:1 multiplexers. HDLs permit variable bit widths using parameterized modules.

**HDL Example 4.34 PARAMETERIZED N-BIT MULTIPLEXERS**

**Verilog**

```verilog
module mux2
  # (parameter width = 8)
  input [width-1:0] d0, d1,
  input s,
  output [width-1:0] y;
  assign y = s ? d1 : d0;
endmodule
```

Verilog allows a `# (parameter ...)` statement before the inputs and outputs to define parameters. The parameter statement includes a default value (8) of the parameter, `width`. The number of bits in the inputs and outputs can depend on this parameter.

```verilog
modulemux4_8 (input [7:0] d0, d1, d2, d3,
  input [1:0] s,
  output [7:0] y);
wire [7:0] low, hi;
mux2 lowmux(d0, d1, s[0], low);
mux2 himux(d2, d3, s[1], hi);
mux2 outmux(low, hi, s[1], y);
endmodule
```

The 8-bit 4:1 multiplexer instantiates three 2:1 multiplexers using their default widths.

In contrast, a 12-bit 4:1 multiplexer, `mux4_12`, would need to override the default width using `#()` before the instance name, as shown below.

```verilog
module mux4_12 (input [11:0] d0, d1, d2, d3,
  input [1:0] s,
  output [11:0] y);
wire [11:0] low, hi;
mux2 # (12) lowmux(d0, d1, s[0], low);
mux2 # (12) himux(d2, d3, s[1], hi);
mux2 # (12) outmux(low, hi, s[1], y);
endmodule
```

Do not confuse the use of the `#` sign indicating delays with the use of `#( ... )` in defining and overriding parameters.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux2 is
  generic(width: integer := 8);
  port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0);
  s:  in STD_LOGIC;
  y:  out STD_LOGIC_VECTOR(width-1 downto 0));
end;
architecture synth of mux2 is
begin
  y <= d0 when s = '0' else d1;
end;
```

The `generic` statement includes a default value (8) of `width`. The value is an integer.

```vhdl
entity mux4_8 is
  port(d0, d1, d2, d3: in  STD_LOGIC_VECTOR(7 downto 0);
  s:  in STD_LOGIC_VECTOR(1 downto 0);
  y:  out STD_LOGIC_VECTOR(7 downto 0));
end;
architecture struct of mux4_8 is
  component mux2
    generic(width: integer);
    port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0) ;
    s:  in STD_LOGIC;
    y:  out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  signal low, hi: STD_LOGIC_VECTOR(7 downto 0);
begin
  lowmux: mux2 port map(d0, d1, s(0), low);
  himux:  mux2 port map(d2, d3, s(0), hi);
  outmux:  mux2 port map(low, hi, s(1), y);
end;
```

The 8-bit 4:1 multiplexer, `mux4_8`, instantiates three 2:1 multiplexers using their default widths.

In contrast, a 12-bit 4:1 multiplexer, `mux4_12`, would need to override the default width using `generic map`, as shown below.

```vhdl
lowmux:  mux2 generic map(12)
  port map(d0, d1, s(0), low);
himux:  mux2 generic map(12)
  port map(d2, d3, s(0), hi);
outmux:  mux2 generic map(12)
  port map(low, hi, s(1), y);
```
HDL Example 4.34 declares a parameterized 2:1 multiplexer with a default width of 8, then uses it to create 8- and 12-bit 4:1 multiplexers.

HDL Example 4.35 shows a decoder, which is an even better application of parameterized modules. A large $N:2^N$ decoder is cumbersome to

**HDL Example 4.35** PARAMETERIZED N:2$^N$ DECODER

**Verilog**

```verilog
module decoder #(parameter N = 3) (
    input [N-1:0] a,
    output reg [2**N-1:0] y);

always @ (*)
begin
    y[0] = 0;
    y[a] = 1;
end
endmodule
```

$2^N$ indicates $2^N$.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity decoder is
    generic(N: integer := 3);
    port(a: in STD_LOGIC_VECTOR(N-1 downto 0);
        y: out STD_LOGIC_VECTOR(2**N-1 downto 0));
end;

architecture synth of decoder is
begin
    process (a)
    variable tmp: STD_LOGIC_VECTOR(2**N-1 downto 0);
    begin
        tmp := CONV_STD_LOGIC_VECTOR(0, 2**N);
        tmp(CONV_INTEGER(a)) := '1';
        y <= tmp;
    end process;
end;
```

$2^N$ indicates $2^N$.

**CONV_STD_LOGIC_VECTOR(0, 2**N)** produces a **STD_LOGIC_VECTOR** of length $2^N$ containing all 0’s. It requires the **STD_LOGIC_ARITH** library. The function is useful in other parameterized functions, such as resettable flip-flops that need to be able to produce constants with a parameterized number of bits. The bit index in VHDL must be an integer, so the **CONV_INTEGER** function is used to convert a from a **STD_LOGIC_VECTOR** to an integer.
specify with case statements, but easy using parameterized code that simply sets the appropriate output bit to 1. Specifically, the decoder uses blocking assignments to set all the bits to 0, then changes the appropriate bit to 1.

HDLs also provide generate statements to produce a variable amount of hardware depending on the value of a parameter. generate supports for loops and if statements to determine how many of what types of hardware to produce. HDL Example 4.36 demonstrates how to use generate statements to produce an \( N \)-input AND function from a cascade of two-input AND gates.

Use generate statements with caution; it is easy to produce a large amount of hardware unintentionally!

**HDL Example 4.36 PARAMETERIZED \( N \)-INPUT AND GATE**

**Verilog**
```verilog
module andN
  (#(parameter width = 8))
  (input [width-1:0] a,
   output y);

genvar i;
wire[width-1:1] x;

generate
  for (i=1; i<width; i=i+1) begin:forloop
    if (i == 1)
      assign x[1] = a[0] & a[1];
    else
      assign x[i] = a[i] & x[i-1];
  end
endgenerate
assign y = x[width-1];
endmodule
```

The for statement loops through \( i = 1, 2, \ldots, width-1 \) to produce many consecutive AND gates. The begin in a generate for loop must be followed by a : and an arbitrary label (forloop, in this case).

Of course, writing assign \( y = \& a \) would be much easier!

**VHDL**
```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity andN is
  generic(width: integer := 8);
  port(a: in STD_LOGIC_VECTOR(width-1 downto 0);
       y: out STD_LOGIC);
end;

architecture synth of andN is
  signal i: integer;
  signal x: STD_LOGIC_VECTOR(width-1 downto 1);

  begin
  AllBits: for i in 1 to width-1 generate
    LowBit: if i = 1 generate
      A1: x(1) <= a(0) and a(1);
    end generate;
    OtherBits: if i /= 1 generate
      A1: x(i) <= a(i) and x(i-1);
    end generate;
  end generate;
  assign y = x(width-1);
end;
```

**Figure 4.31 andN synthesized circuit**
4.8 TESTBENCHES

A testbench is an HDL module that is used to test another module, called the device under test (DUT). The testbench contains statements to apply inputs to the DUT and, ideally, to check that the correct outputs are produced. The input and desired output patterns are called test vectors.

Consider testing the sillyfunction module from Section 4.1.1 that computes \( y = \overline{a \overline{b}c} + a \overline{b} \overline{c} + ab \overline{c} \). This is a simple module, so we can perform exhaustive testing by applying all eight possible test vectors.

HDL Example 4.37 demonstrates a simple testbench. It instantiates the DUT, then applies the inputs. Blocking assignments and delays are used to apply the inputs in the appropriate order. The user must view the results of the simulation and verify by inspection that the correct outputs are produced. Testbenches are simulated the same as other HDL modules. However, they are not synthesizeable.

HDL Example 4.37 TESTBENCH

**Verilog**

```verilog
module testbench1();
    reg a, b, c;
    wire y;
    // instantiate device under test
    sillyfunction dut(a, b, c, y);
    // apply inputs one at a time
    initial begin
        a = 0; b = 0; c = 0; #10;
        c = 1; #10;
        b = 1; c = 0; #10;
        c = 1; #10;
        a = 1; b = 0; c = 0; #10;
        c = 1; #10;
        b = 1; c = 0; #10;
        c = 1; #10;
    end
endmodule
```

The *initial* statement executes the statements in its body at the start of simulation. In this case, it first applies the input pattern 000 and waits for 10 time units. It then applies 001 and waits 10 more units, and so forth until all eight possible inputs have been applied. *initial* statements should be used only in testbenches for simulation, not in modules intended to be synthesized into actual hardware. Hardware has no way of magically executing a sequence of special steps when it is first turned on.

Like signals in *always* statements, signals in *initial* statements must be declared to be *reg*.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity testbench1 is -- no inputs or outputs
end;

architecture sim of testbench1 is
    component sillyfunction
        port(a, b, c: in STD_LOGIC;
             y: out STD_LOGIC);
    end component;
    signal a, b, c, y: STD_LOGIC;
    begin
        -- instantiate device under test
        dut: sillyfunction port map(a, b, c, y);
        -- apply inputs one at a time
        process begin
            a <= '0'; b <= '0'; c <= '0'; wait for 10 ns;
            c <= '1'; wait for 10 ns;
            b <= '1'; c <= '0'; wait for 10 ns;
            c <= '1'; wait for 10 ns;
            a <= '1'; b <= '0'; c <= '0'; wait for 10 ns;
            c <= '1'; wait for 10 ns;
            b <= '1'; c <= '0'; wait for 10 ns;
            c <= '1'; wait for 10 ns;
            wait; -- wait forever
        end process;
    end;
```

The *process* statement first applies the input pattern 000 and waits for 10 ns. It then applies 001 and waits 10 more ns, and so forth until all eight possible inputs have been applied. At the end, the process waits indefinitely; otherwise, the process would begin again, repeatedly applying the pattern of test vectors.
Checking for correct outputs is tedious and error-prone. Moreover, determining the correct outputs is much easier when the design is fresh in your mind; if you make minor changes and need to retest weeks later, determining the correct outputs becomes a hassle. A much better approach is to write a self-checking testbench, shown in HDL Example 4.38.

**HDL Example 4.38 SELF-CHECKING TESTBENCH**

**Verilog**

```verilog
module testbench2();
    reg a, b, c;
    wire y;
    // instantiate device under test
    sillyfunction dut(a, b, c, y);
    // apply inputs one at a time
    // checking results
    initial begin
        a = '0'; b = '0'; c = '0'; #10;
        if (y !== 1)$display("000 failed.");
        c = '1'; #10;
        if (y !== 0)$display("001 failed.");
        b = '1'; c = '0'; #10;
        if (y !== 0)$display("010 failed.");
        c = '1'; #10;
        if (y !== 1)$display("011 failed.");
        a = '1'; b = '0'; c = '0'; #10;
        if (y !== 1)$display("100 failed.");
        c = '1'; #10;
        if (y !== 1)$display("101 failed.");
        c = '1'; #10;
        if (y !== 0)$display("111 failed.");
    end
endmodule
```

This module checks `y` against expectations after each input test vector is applied. In Verilog, comparison using `==` or `!=` is effective between signals that do not take on the values of `x` and `z`. Testbenches use the `==` and `!=` operators for comparisons of equality and inequality, respectively, because these operators work correctly with operands that could be `x` or `z`. It uses the `$display system task to print a message on the simulator console if an error occurs. `$display is meaningful only in simulation, not in synthesis.

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity testbench2 is -- no inputs or outputs
    end;

architecture sim of testbench2 is

    component sillyfunction
        port(a, b, c: in  STD_LOGIC;
        y: out STD_LOGIC);
    end component;

    signal a, b, c, y: STD_LOGIC;

    begin
        // instantiate device under test
        dut: sillyfunction port map(a, b, c, y);

        // apply inputs one at a time
        // checking results
        process begin
            a <= '0'; b <= '0'; c <= '0'; wait for 10 ns;
            assert y = '1' report "000 failed.";
            c <= '1'; wait for 10 ns;
            assert y = '0' report "001 failed.";
            b <= '1'; c <= '0'; wait for 10 ns;
            assert y = '0' report "010 failed.";
            c <= '1'; wait for 10 ns;
            assert y = '0' report "011 failed.";
            a <= '1'; b <= '0'; c <= '0'; wait for 10 ns;
            assert y = '1' report "100 failed.";
            c <= '1'; wait for 10 ns;
            assert y = '0' report "101 failed.";
            b <= '1'; c <= '0'; wait for 10 ns;
            assert y = '0' report "110 failed.";
            c <= '1'; wait for 10 ns;
            assert y = '0' report "111 failed.";
        end process;
end;
```

The `assert` statement checks a condition and prints the message given in the `report` clause if the condition is not satisfied. `assert` is meaningful only in simulation, not in synthesis.

Writing code for each test vector also becomes tedious, especially for modules that require a large number of vectors. An even better approach is to place the test vectors in a separate file. The testbench simply reads the test vectors from the file, applies the input test vector to the DUT, waits, checks that the output values from the DUT match the output vector, and repeats until reaching the end of the test vectors file.
HDL Example 4.39 demonstrates such a testbench. The testbench generates a clock using an always/process statement with no stimulus list, so that it is continuously reevaluated. At the beginning of the simulation, it reads the test vectors from a text file and pulses reset for two cycles. example.tv is a text file containing the inputs and expected output written in binary:

000_1
001_0
010_0
011_0
100_1
101_1
110_0
111_0

HDL Example 4.39  TESTBENCH WITH TEST VECTOR FILE

**Verilog**

```verilog
module testbench3();
reg clk, reset;
reg a, b, c, yexpected;
wire y;
reg[31:0] vectornum, errors;
reg[3:0] testvectors[10000:0];

// instantiate device under test
sillyfunction dut(a, b, c, y);

// generate clock
always begin
  clk = 1; #5; clk = 0; #5;
end

// at start of test, load vectors
// and pulse reset
initial begin
  $readmemb("example.tv", testvectors);
  vectornum = 0; errors = 0;
  reset = 1; #27; reset = 0;
end

// apply test vectors on rising edge of clk
always @(posedge clk)
begin
  #1; a, b, c, yexpected = testvectors[vectornum];
end

// check results on falling edge of clk
always @(negedge clk)
begin
  if(!reset) begin // skip during reset
    if(y !== yexpected) begin
```
$display ("Error: inputs = %b", {a, b, c});
$display(" outputs = %b (y expected) ", y, yexpected);
errors = errors + 1;
end
vectornum = vectornum + 1;
if (testvectors(vectornum) === 4'b1) begin
$display("%d tests completed with %d errors", vectornum, errors);
$finish;
end
endmodule

$readmemb reads a file of binary numbers into the testvectors array. $readmemh is similar but reads a file of hexadecimal numbers.

The next block of code waits one time unit after the rising edge of the clock (to avoid any confusion if clock and data change simultaneously), then sets the three inputs and the expected output based on the four bits in the current test vector. The next block of code checks the output of the DUT at the negative edge of the clock, after the inputs have had time to propagate through the DUT to produce the output, y. The testbench compares the generated output, y, with the expected output, yexpected, and prints an error if they don't match. %b and %d indicate to print the values in binary and decimal, respectively. For example, $display ("%b %b", y, yexpected): prints the two values, y and yexpected, in binary. $h prints a value in hexadecimal.

This process repeats until there are no more valid test vectors in the testvectors array. $finish terminates the simulation.

Note that even though the Verilog module supports up to 10,001 test vectors, it will terminate the simulation after executing the eight vectors in the file.

The VHDL code is rather ungainly and uses file reading commands beyond the scope of this chapter, but it gives the sense of what a self-checking testbench looks like.
New inputs are applied on the rising edge of the clock, and the output is checked on the falling edge of the clock. This clock (and reset) would also be provided to the DUT if sequential logic were being tested. Errors are reported as they occur. At the end of the simulation, the testbench prints the total number of test vectors applied and the number of errors detected.

The testbench in HDL Example 4.39 is overkill for such a simple circuit. However, it can easily be modified to test more complex circuits by changing the example.tv file, instantiating the new DUT, and changing a few lines of code to set the inputs and check the outputs.

4.9 SUMMARY

Hardware description languages (HDLs) are extremely important tools for modern digital designers. Once you have learned Verilog or VHDL, you will be able to specify digital systems much faster than if you had to draw the complete schematics. The debug cycle is also often much faster, because modifications require code changes instead of tedious schematic rewiring. However, the debug cycle can be much longer using HDLs if you don’t have a good idea of the hardware your code implies.

HDLs are used for both simulation and synthesis. Logic simulation is a powerful way to test a system on a computer before it is turned into hardware. Simulators let you check the values of signals inside your system that might be impossible to measure on a physical piece of hardware. Logic synthesis converts the HDL code into digital logic circuits.

The most important thing to remember when you are writing HDL code is that you are describing real hardware, not writing a computer program. The most common beginner’s mistake is to write HDL code without thinking about the hardware you intend to produce. If you don’t know what hardware you are implying, you are almost certain not to get what you want. Instead, begin by sketching a block diagram of your system, identifying which portions are combinational logic, which portions are sequential circuits or finite state machines, and so forth. Then write HDL code for each portion, using the correct idioms to imply the kind of hardware you need.
Exercises

The following exercises may be done using your favorite HDL. If you have a simulator available, test your design. Print the waveforms and explain how they prove that it works. If you have a synthesizer available, synthesize your code. Print the generated circuit diagram, and explain why it matches your expectations.

Exercise 4.1 Sketch a schematic of the circuit described by the following HDL code. Simplify the schematic so that it shows a minimum number of gates.

Verilog

module exercise1(input a, b, c, output y, z);

assign y = a & b & c | a & b & ~c | a & ~b & c;
assign z = a & b | ~a & ~b;
endmodule

VHDL

library IEEE; use IEEE.STD_LOGIC_1164.all;

entity exercise1 is
port(a, b, c: in STD_LOGIC;
    y, z: out STD_LOGIC);
end;

architecture synth of exercise1 is
begin
    y <= (a and b and c)or(a and b and (not c))or
        (a and(not b) and c);
    z <= (a and b)or ((not a) and (not b));
end;

Exercise 4.2 Sketch a schematic of the circuit described by the following HDL code. Simplify the schematic so that it shows a minimum number of gates.

Verilog

module exercise2(input [3:0] a, output reg [1:0] y);

always @(*)
    if (a[0]) y = 2'b11;
    else if(a[1]) y = 2'b10;
    else if(a[2]) y = 2'b01;
    else if(a[3]) y = 2'b00;
    else y = a[1:0];
endmodule

VHDL

library IEEE; use IEEE.STD_LOGIC_1164.all;

entity exercise2 is
port(a: in STD_LOGIC_VECTOR(3 downto 0);
    y: out STD_LOGIC_VECTOR(1 downto 0));
end;

architecture synth of exercise2 is
begin
    process (a) begin
        if a(0) = '1' then y <= "11";
        elsif a(1) = '1' then y <= "10";
        elsif a(2) = '1' then y <= "01";
        elsif a(3) = '1' then y <= "00";
        else y <= a(1 downto 0);
    end if;
    end process;
end;

Exercise 4.3 Write an HDL module that computes a four-input XOR function. The input is a[3:0], and the output is y.
Exercise 4.4  Write a self-checking testbench for Exercise 4.3. Create a test vector file containing all 16 test cases. Simulate the circuit and show that it works. Introduce an error in the test vector file and show that the testbench reports a mismatch.

Exercise 4.5  Write an HDL module called minority. It receives three inputs, a, b, and c. It produces one output, y, that is TRUE if at least two of the inputs are FALSE.

Exercise 4.6  Write an HDL module for a hexadecimal seven-segment display decoder. The decoder should handle the digits A, B, C, D, E, and F as well as 0–9.

Exercise 4.7  Write a self-checking testbench for Exercise 4.6. Create a test vector file containing all 16 test cases. Simulate the circuit and show that it works. Introduce an error in the test vector file and show that the testbench reports a mismatch.

Exercise 4.8  Write an 8:1 multiplexer module called mux8 with inputs s2:s0, d0, d1, d2, d3, d4, d5, d6, d7, and output y.

Exercise 4.9  Write a structural module to compute the logic function, y = \overline{a}b + \overline{b}c + \overline{a}bc, using multiplexer logic. Use the 8:1 multiplexer from Exercise 4.8.

Exercise 4.10  Repeat Exercise 4.9 using a 4:1 multiplexer and as many NOT gates as you need.

Exercise 4.11  Section 4.5.4 pointed out that a synchronizer could be correctly described with blocking assignments if the assignments were given in the proper order. Think of a simple sequential circuit that cannot be correctly described with blocking assignments, regardless of order.

Exercise 4.12  Write an HDL module for an eight-input priority circuit.

Exercise 4.13  Write an HDL module for a 2:4 decoder.

Exercise 4.14  Write an HDL module for a 6:64 decoder using three instances of the 2:4 decoders from Exercise 4.13 and a bunch of three-input AND gates.

Exercise 4.15  Write HDL modules that implement the Boolean equations from Exercise 2.7.

Exercise 4.16  Write an HDL module that implements the circuit from Exercise 2.18.

Exercise 4.17  Write an HDL module that implements the logic function from Exercise 2.19. Pay careful attention to how you handle don’t cares.
Exercise 4.18  Write an HDL module that implements the functions from Exercise 2.24.

Exercise 4.19  Write an HDL module that implements the priority encoder from Exercise 2.25.

Exercise 4.20  Write an HDL module that implements the binary-to-thermometer code converter from Exercise 2.27.

Exercise 4.21  Write an HDL module implementing the days-in-month function from Question 2.2.

Exercise 4.22  Sketch the state transition diagram for the FSM described by the following HDL code.

Verilog

```verilog
module fsm2(input clk, reset, 
            input a, b, 
            output y); 
reg [1:0] state, nextstate; 
parameter S0 = 2'd00; 
parameter S1 = 2'd01; 
parameter S2 = 2'd10; 
parameter S3 = 2'd11; 
always @ (posedge clk, posedge reset) 
if (reset) state <= S0; 
else state <= nextstate; 
always @ (*) 
case (state) 
  S0: if (a ^ b) nextstate = S1; 
  else nextstate = S0; 
  S1: if (a & b) nextstate = S2; 
  else nextstate = S0; 
  S2: if (a | b) nextstate = S3; 
  else nextstate = S0; 
  S3: if (a | b) nextstate = S3; 
  else nextstate = S0; 
endcase 
assign y = (state == S1) | (state == S2); 
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity fsm2 is
  port(clk, reset: in STD_LOGIC; 
       a, b: in STD_LOGIC; 
       y: out STD_LOGIC);
end;

architecture synth of fsm2 is 
type statetype is (S0, S1, S2, S3); 
signal state, nextstate: statetype; 
bEGIN 
process(clk, reset) begin 
if reset = '1' then state <= S0; 
elsif clk'event and clk = '1' then 
  state <= nextstate;
end if;
end process;
process(state, a, b) begin 
case state is 
  when S0 => if (a xor b) = '1' then 
    nextstate <= S1; 
  else nextstate <= S0; 
  when S1 => if (a and b) = '1' then 
    nextstate <= S2; 
  else nextstate <= S0; 
  when S2 => if (a or b) = '1' then 
    nextstate <= S3; 
  else nextstate <= S0; 
  when S3 => if (a or b) = '1' then 
    nextstate <= S3; 
  else nextstate <= S0; 
end case;
end process;
y <= '1' when ((state = S1) or (state = S2)) 
  else '0'; 
end;
```
Exercise 4.23 Sketch the state transition diagram for the FSM described by the following HDL code. An FSM of this nature is used in a branch predictor on some microprocessors.

**Verilog**

```verilog
module fsm1(input clk, reset, 
             input taken, back, 
             output predicttaken);
reg [4:0] state, nextstate;
parameter S0 = 5'b00001;
parameter S1 = 5'b00010;
parameter S2 = 5'b00100;
parameter S3 = 5'b01000;
parameter S4 = 5'b10000;
always @ (posedge clk, posedge reset)
if (reset) state = S2;
else state = nextstate;
always @ (*)
case (state)
  S0: if (taken) nextstate = S1;
      else nextstate = S0;
  S1: if (taken) nextstate = S2;
      else nextstate = S0;
  S2: if (taken) nextstate = S3;
      else nextstate = S1;
  S3: if (taken) nextstate = S4;
      else nextstate = S2;
  S4: if (taken) nextstate = S4;
      else nextstate = S3;
  default: nextstate = S2;
endcase
assign predicttaken = (state == S4) ||
                      (state == S3) ||
                      (state == S2 && back);
endmodule
```

**VHDL**

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity fsm1 is 
  port(clk, reset: in STD_LOGIC; 
       taken, back: in STD_LOGIC; 
       predicttaken: out STD_LOGIC);
end;

architecture synth of fsm1 is
  type statetype is (S0, S1, S2, S3, S4);
signal state, nextstate: statetype;
begin
  process (clk, reset) begin
    if reset = '1' then state <= S2;
    elsif clk'event and clk = '1' then
      state <= nextstate;
    end if;
  end process;
  process(state, taken) begin
    case state is
      when S0 => if taken = '1' then
        nextstate <= S1;
      else
        nextstate <= S0;
      end if;
      when S1 => if taken = '1' then
        nextstate <= S2;
      else
        nextstate <= S0;
      end if;
      when S2 => if taken = '1' then
        nextstate <= S3;
      else
        nextstate <= S1;
      end if;
      when S3 => if taken = '1' then
        nextstate <= S4;
      else
        nextstate <= S2;
      end if;
      when S4 => if taken = '1' then
        nextstate <= S4;
      else
        nextstate <= S3;
      end if;
      when others => nextstate <= S2;
    end case;
  end process;
  -- output logic
  predicttaken <= '1' when
    ((state = S4) or (state = S3) or
     (state = S2 and back = '1'))
  else '0';
end;
```
Exercises

**Exercise 4.24** Write an HDL module for an SR latch.

**Exercise 4.25** Write an HDL module for a JK flip-flop. The flip-flop has inputs, \( clk \), \( J \), and \( K \), and output \( Q \). On the rising edge of the clock, \( Q \) keeps its old value if \( J = K = 0 \). It sets \( Q \) to 1 if \( J = 1 \), resets \( Q \) to 0 if \( K = 1 \), and inverts \( Q \) if \( J = K = 1 \).

**Exercise 4.26** Write an HDL module for the latch from Figure 3.18. Use one assignment statement for each gate. Specify delays of 1 unit or 1 ns to each gate. Simulate the latch and show that it operates correctly. Then increase the inverter delay. How long does the delay have to be before a race condition causes the latch to malfunction?

**Exercise 4.27** Write an HDL module for the traffic light controller from Section 3.4.1.

**Exercise 4.28** Write three HDL modules for the factored parade mode traffic light controller from Example 3.8. The modules should be called *controller*, *mode*, and *lights*, and they should have the inputs and outputs shown in Figure 3.33(b).

**Exercise 4.29** Write an HDL module describing the circuit in Figure 3.40.

**Exercise 4.30** Write an HDL module for the FSM with the state transition diagram given in Figure 3.65 from Exercise 3.19.

**Exercise 4.31** Write an HDL module for the FSM with the state transition diagram given in Figure 3.66 from Exercise 3.20.

**Exercise 4.32** Write an HDL module for the improved traffic light controller from Exercise 3.21.

**Exercise 4.33** Write an HDL module for the daughter snail from Exercise 3.22.

**Exercise 4.34** Write an HDL module for the soda machine dispenser from Exercise 3.23.

**Exercise 4.35** Write an HDL module for the Gray code counter from Exercise 3.24.

**Exercise 4.36** Write an HDL module for the UP/DOWN Gray code counter from Exercise 3.25.

**Exercise 4.37** Write an HDL module for the FSM from Exercise 3.26.
Exercise 4.38 Write an HDL module for the FSM from Exercise 3.27.

Exercise 4.39 Write an HDL module for the serial two's complementer from Question 3.2.

Exercise 4.40 Write an HDL module for the circuit in Exercise 3.28.

Exercise 4.41 Write an HDL module for the circuit in Exercise 3.29.

Exercise 4.42 Write an HDL module for the circuit in Exercise 3.30.

Exercise 4.43 Write an HDL module for the circuit in Exercise 3.31. You may use the full adder from Section 4.2.5.

Verilog Exercises
The following exercises are specific to Verilog.

Exercise 4.44 What does it mean for a signal to be declared reg in Verilog?

Exercise 4.45 Rewrite the syncbad module from HDL Example 4.30. Use nonblocking assignments, but change the code to produce a correct synchronizer with two flip-flops.

Exercise 4.46 Consider the following two Verilog modules. Do they have the same function? Sketch the hardware each one implies.

module code1(input clk, a, b, c, output reg y);
  reg x;
  always @ (posedge clk) begin
    x <= a & b;
    y <= x | c;
  end
endmodule

module code2(input a, b, c, clk, output reg y);
  reg x;
  always @ (posedge clk) begin
    y <= x | c;
    x <= a & b;
  end
endmodule

Exercise 4.47 Repeat Exercise 4.46 if the <= is replaced by = in every assignment.
Exercise 4.48 The following Verilog modules show errors that the authors have seen students make in the laboratory. Explain the error in each module and show how to fix it.

(a) module latch (input clk, input [3:0] d, output reg [3:0] q):
    always @(clk)
        if(clk) q <= d;
endmodule

(b) module gates (input [3:0] a, b, output reg [3:0] y1, y2, y3, y4, y5):
    always @(a)
        begin
            y1 = a & b;
            y2 = a | b;
            y3 = a ^ b;
            y4 = ~(a & b);
            y5 = ~(a | b);
        end
endmodule

(c) module mux2 (input [3:0] d0, d1, input s, output reg [3:0] y):
    always @(posedge s)
        if(s) y <= d1;
        else y <= d0;
endmodule

(d) module twoflops (input clk, input d0, d1, output reg q0, q1):
    always @(posedge clk)
        q1 = d1;
        q0 = d0;
endmodule
(e) module FSM(input clk, 
    input a, 
    output reg out1, out2):

    reg state;

    // next state logic and register (sequential)
    always @ (posedge clk)
        if(state == 0) begin
            if(a) state <= 1;
            else begin
                if(~a) state <= 0;
            end
        end

    always @ (*) // output logic (combinational)
        if(state == 0) out1 = 1;
    else out2 = 1;
endmodule

(f) module priority (input [3:0] a, 
    output reg [3:0] y):

    always @ (*)
        if (a[3]) y = 4'b1000;
    else if(a[2]) y = 4'b0100;
    else if(a[1]) y = 4'b0010;
    else if(a[0]) y = 4'b0001;
endmodule

(g) module divideby3FSM (input clk, 
    input reset, 
    output out):

    reg [1:0] state, nextstate;

    parameter S0 = 2'b00;
    parameter S1 = 2'b01;
    parameter S2 = 2'b10;

    // State Register
    always @ (posedge clk, posedge reset)
        if(reset) state <= S0;
    else state <= nextstate;

    // Next State Logic
    always @ (state)
        case (state)
            S0: nextstate = S1;
            S1: nextstate = S2;
            2: nextstate = S0;
        endcase

    // Output Logic
    assign out = (state == S2);
endmodule
(h) module mux2tri (input [3:0] d0, d1,
 input s,
 output [3:0] y);
     tristate t0(d0, s, y);
     tristate t1(d1, s, y);
 endmodule

(i) module floprsen (input clk,
 input reset,
 input set,
 input [3:0] d,
 output reg [3:0] q);

 always @ (posedge clk, posedge reset)
     if(reset) q <= 0;
     else q <= d;

 always @ (set)
     if(set) q <= 1;
 endmodule

(j) module and3 (input a, b, c,
 output reg y);

 reg tmp;

 always @ (a, b, c)
 begin
     tmp <= a & b;
     y <= tmp & c;
 end
 endmodule

**VHDL Exercises**

The following exercises are specific to VHDL.

**Exercise 4.49** In VHDL, why is it necessary to write

q <= '1' when state = S0 else '0';

rather than simply

q <= (state = S0);
Exercise 4.50 Each of the following VHDL modules contains an error. For brevity, only the architecture is shown; assume that the library use clause and entity declaration are correct. Explain the error and show how to fix it.

(a) architecture synth of latch is
    begin
        process(clk)
        begin
            if clk = '1' then
                q <= d;
            end if;
        end process;
    end;

(b) architecture proc of gates is
    begin
        process(a)
        begin
            y1 <= a and b;
            y2 <= a or b;
            y3 <= a xor b;
            y4 <= a nand b;
            y5 <= a nor b;
        end process;
    end;

(c) architecture synth of flop is
    begin
        process(clk)
        begin
            if clk'event and clk = '1' then
                q <= d;
            end if;
        end process;
    end;

(d) architecture synth of priority is
    begin
        process(a)
        begin
            if a(3) = '1' then y <= "1000";
            elsif a(2) = '1' then y <= "0100";
            elsif a(1) = '1' then y <= "0010";
            elsif a(0) = '1' then y <= "0001";
        end if;
    end process;

(e) architecture synth of divideby3FSM is
    type statetype is (S0, S1, S2);
    signal state, nextstate: statetype;
    begin
        process(clk, reset)
        begin
            if reset = '1' then state <= S0;
            elsif clk'event and clk = '1' then
                state <= nextstate;
            end if;
        end process;
    end;
process (state) begin
    case state is
        when S0 => nextstate <= S1;
        when S1 => nextstate <= S2;
        when S2 => nextstate <= S0;
    end case;
end process;

q <= '1' when state = S0 else '0';
end;

(f) architecture struct of mux2 is
    component tristate
        port(a: in STD_LOGIC_VECTOR(3 downto 0);
            en: in  STD_LOGIC;
            y:  out STD_LOGIC_VECTOR(3 downto 0));
    end component;
    begin
        t0: tristate port map(d0, s, y);
        t1: tristate port map(d1, s, y);
    end;

(g) architecture asynchronous of flopr is
    begin
        process(clk, reset) begin
            if reset = '1' then
                q <= '0';
            elsif clk'event and clk = '1' then
                q <= d;
            end if;
        end process;
        process(set) begin
            if set = '1' then
                q <= '1';
            end if;
        end process;
    end;

(h) architecture synth of mux3 is
    begin
        y <= d2 when s(1) else
            d1 when s(0) else d0;
    end;
Interview Questions

The following exercises present questions that have been asked at interviews for digital design jobs.

**Question 4.1** Write a line of HDL code that gates a 32-bit bus called `data` with another signal called `sel` to produce a 32-bit `result`. If `sel` is TRUE, `result = data`. Otherwise, `result` should be all 0's.

**Question 4.2** Explain the difference between blocking and nonblocking assignments in Verilog. Give examples.

**Question 4.3** What does the following Verilog statement do?

```
result = | (data[15:0] & 16'hC820);
```