

Degree in Biomedical Engineering

UNIT 4 Exercises: Optimal filtering

- 4.1 Given an 2nd order FIR filter:
 - a) Draw the block diagram of the filter.
 - b) Write the expression of y[0], y[1] and y[2] (y[n] is the output of the filter), given that the initial values for the delays are all zero. Provide the general expression and particularize for the following values of x[n]:
 - x(0)=0.1 x(1)=0.8
 - x(2)=0.2

4.2 Check that $\vec{w}^T \overrightarrow{R_{XD}} = \overrightarrow{R_{XD}}^T \vec{w}$ for M=3.

- **4.3.** Design a 2-coefficient optimal filter given the following statistics:
 - $R_{XX}(-2) = 0.24649$ $R_{XX}(-1) = 0.24671$ $R_{XX}(0) = 0.27136$ $R_{XX}(1) = 0.24671$ $R_{XX}(2) = 0.24649$ $R_{XD}(-2) = 0.24616$ $R_{XD}(-1) = 0.24634$ $R_{XD}(0) = 0.24634$ $R_{XD}(1) = 0.24634$ $R_{XD}(2) = 0.24616$
- **4.4.** Check that $\frac{d(\vec{w}^T \overrightarrow{R_{XD}})}{d\vec{w}} = \overrightarrow{R_{XD}}$ for M=3.
- **4.5.** Prove that $E[\vec{x}(n)d(n)] = E[d(n)\vec{x}(n)^T] = \overrightarrow{R_{XD}}$