5 Problem Set 4.ii

Advanced Financing

Problem 1

You make a deposit of 4250€ in a financial institution that uses compounding.

- 1. Calculate the balance after 2 years if the entity offers a 5% nominal APR with semestral compounding for the first 2 semester, and a 4% nominal APR with quarterly compounding thereafter.
- 2. Calculate the average effective rate of the transaction
- 3. Suppose the deposit includes the expenditures listed below. Compute the real effective return for the client and the real effective return for the bank. The expenditures are:
 - (a) The client pays initially $6\mathfrak{C}$ to the institution and at the end pays $4\mathfrak{C}$ to a third party
 - (b) The institution has an initial cost of 3€ payable to a third party

Problem 2

We wish to purchase a new car and its cash price is 16.500€. In order to ease the financing of the purchase the car dealer offers the following payment option:

- At the time of the sale we can hand in our used car, which is valued by the dealer at 4.500€
- You commit to making two equal payments, one due in 3 months and the other in 6 months

You know that the effective APR on the transaction is 6% and you are asked to:

- 1. The amount of the each of the two future payments
- 2. We are given a second payment option which involves giving up our used car (same value) and agreeing to a single future payment, due in 8 months. This second option involves two additional payments: an initial one of 35€ and a final one of 50€, both to the car dealer. The car dealer will also incur costs if you select this option: 25€ initially, payable to a third party. Knowing that the effective APR of the (pure) loan is 5.5%, you are asked to determine:
 - (a) The size of the payment, 8 months from today
 - (b) The cost and return of the transaction for the client and the dealer, respectively

Problem 3

Suppose you have 12,000€ in your bank account. The branch manager calls you to offer you several investment options. But, you are really not interested as you know you will be withdrawing the money in 3 months' time, and maybe even earlier. The manager then offers you the following: a 4% nominal APR with monthly capitalization and free access to the money. After 3 months you need to make a payment of 2,000€ so you take out all the money. Determine:

- The official effective interest rate (TAE) that the bank has to announce (for a one year deposit), and the effective APR
- The effective annual interest rate you have received if you have to pay an additional 0.5% fee (on balance)

Problem 4

You borrow 12000€ from the bank. You pay 10€ for a report on your credit status to another company (now). In 6 months you cancel the debt and you have to pay 450€ in interest and a cancellation fee of 120€—the loan is for one year (with no penalty at the end).

Determine:

- The official effective interest rate (TAE) that the bank has to announce (for a one year loan, without cancellation), and the effective APR (of the raw transaction)
- The effective annual interest rate you have paid

Past Exam Questions

Problem 5 (ex 2013)

Choose between the following two investment options for a three year investment (and explain your choice)

- 1. Growing deposit: 4% in the first year, 5% in the second year and 6% in the third year. All are nominal APR with monthly compounding
- 2. Constant deposit: 5% nominal APR with monthly compounding

Problem 6 (ex 2014)

In order to finance recently acquired machinery, your firm obtains quotes from three different financial institutions.

- 1. Bank A offers 4.45% nominal APR with payments every 6 months
- 2. Bank B offers monthly payments with a 4.42% nominal APR
- 3. Bank C offers yearly payments with a 4.60% nominal APR

None of these charge any commissions. Which offers the best effective APR?

Problem 7 (ex 2017/18)

You see an advertisement for a T.V. with a price of 600€. When you go to the store to buy the store owner offers two payment options

- Pay in cash now with a 2% cash discount
- Pay "without interest" in 3 months. To take this offer you also have to pay 10€ as a loan-processing fee

Determine the effective APR of taking the payment in 3 months instead of the cash discount

Problem 8 (ex 2014)

Determine the annual effective rate of a five year investment with

- 1. an 8% nominal APR with monthly capitalization and no commissions
- 2. an 8.3% nominal APR with monthly capitalization and no commissions
- 3. an 9% nominal APR with monthly capitalization and a 2% account opening fee

Problem 9 (ex 2014)

Marta has two IOUs from Mercanada S.A.: one with a face value of 1500€, due in 35 days. Another of 2100€ due in 65 days. El Cobrador del Pingüino, a financing firm, offers to discount them like a bank with a 4,5% interest and a study fee of 0,5% of the nominal amount, payable now.

- 1. Determine the amount of cash you would receive from this firm
- 2. Determine the effective APR of the (single) equivalent IOU