



**SECTION II: KINETICS AND BIOREACTOR DESIGN:**  
**LESSON 10.2. - Bioreactor design – Design Equations - Examples**



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## AIMS FOR TODAY'S LESSON

**10.1 Design equations**

**10.2 Exercises**

**10.3 Tank vs Tubular reactor: Comparing efficiency**

**10.4 Recycle, By-pass and Purge**

**10.5 Bioreactor association**



# WORKING ON BACTERIA

OK GERMS  
SHE'S SET UP  
ANOTHER  
EXPERIMENT



THIS IS  
WHAT WE  
DID LAST  
TIME —



THIS TIME  
WE'LL DO  
THIS



SHE WON'T  
KNOW WHICH  
IS RIGHT!

@twisteddoodler

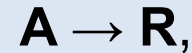
## What does a Greek cow say?



μ

**Example #1:**

An enzymatic process where the following reaction takes place



can be described using a first-order kinetic equation:

$$\mathbf{r \text{ (mole}\cdot\text{L}^{-1}\cdot\text{h}^{-1}) = 1.2\cdot[\text{A}]}$$

This reaction is carried out using a batch reactor where the working temperature is constantly 50°C. The reactant mixture presents an initial concentration of 12 moles/L in A.

What is the reaction time ( $t_R$ ) needed in order to reach an  $X_A$  of 0.80?

**Example #2:**

One current containing **3 moles/L of substrate** and **0.01 g/L of enzyme** is fed into a **Continuous Stirred Tank Reactor (CSTR)**. The kinetic parameters corresponding to the equation describing the process (Michaelis-Menten equation) are:

$$K_{\text{cat}} = 2 \text{ moles}/(\text{min.gE}) \text{ and } K_M = 0.1 \text{ (mole S)/L.}$$

Calculate the volume needed to treat a 30 L/min stream so that an output conversion of 99.5% is achieved.

**Example #3:**

The growth of an aerobic microorganism is carried out within a **3 L** bioreactor working as a **continuous stirred tank** fed with **0,15 L/h**.

If growth can adequately be described using the kinetic model proposed by **Monod**, and **nitrogenous substrate can be considered as limiting nutrient**, calculate both biomass and limiting substrate concentrations when steady state is achieved.

**Inlet substrate concentration** is 0.4 g/L.

**Kinetic parameters** for the biological system under the operating conditions are:

$$\mu^{\max} = 0.2 \text{ h}^{-1}, K_N = 0.06 \text{ g N/L}, Y_{X/N} = 4.6 \text{ gX / gN}.$$

**Example #4:**

**30 g/h** of a certain yeast need to be obtained. The kinetic model describing its growth has been obtained, taking into account that it is **limited by the amount of nitrogenous substrate** present in the fermentation broth.

Calculate the volume of the continuous tank reactor required for this production.

Kinetic model:

$$R_X \text{ (gX / L} \cdot \text{h)} = \mu_m \cdot [N] \cdot [X]$$

$$R_N \text{ (gN / L} \cdot \text{h)} = -Y_{N/X} \cdot R_X$$

where:  $\mu_m = 0.5 \text{ L / g N} \cdot \text{h}$ ;  $Y_{N/X} = 0.17 \text{ gN / gX}$ ;

And  $F = 12 \text{ L / h}$ ;  $[N]_0 = 0.8 \text{ gN / L}$

**Example #5:**

A 100 L bioreactor consisting in a continuous stirred tank is fed with a 10 L/h current containing 0,75 g/L of a growth limiting substrate.

The kinetic model describing the system has been previously obtained.

Calculate the amount of product generated per hour.

Data:

Kinetic model:

$$\left\{ \begin{array}{l} R_X \text{ (gX / L} \cdot \text{h)} = 0,46 \cdot [N] \cdot [X] \\ R_N \text{ (gN / L} \cdot \text{h)} = -0,15 \cdot R_X \\ R_P \text{ (gP / L} \cdot \text{h)} = 0,71 \cdot R_X \end{array} \right.$$



### Example #6:

A continuous tubular reactor is used in order to carry out the reaction



catalyzed by an enzyme. The fed stream contains "A" and "B" in an equimolecular ratio at a 500 L/min flow. The concentration of "A" at the entrance is 0.18 M

In order to achieve an output conversion of 85%, what volume of the reactor is needed?

Although the enzymatic process, the kinetics of the reaction taking place can be expressed as:

$$r = 10 \cdot [A] \cdot [B] \text{ (mole / L / min)}$$



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