

**UNIVERSITY CEU SAN PABLO  
SCHOOL OF PHARMACY  
DEPARTMENT OF CHEMISTRY AND BIOCHEMISTRY**

**COMPLEMENTARY PROBLEMS OF PHYSICAL CHEMISTRY**

**2018-19**

**LESSON 4**

**19.** An ideal solution is comprised of two components, A and B. The vapour pressure of pure A is 125 mmHg at 25 ° C and B is a non-volatile component. A mixture with 1 g B and 20 g A has a vapor pressure of 110 mmHg at 25 ° C. What is the relationship between the molecular weights of A and B?

**Solution:**  $M_A / M_B = 2.72$

**20.** An aerosol container\* contains an (ideal) liquid propellant mixture of A and B in equilibrium with its vapour. If the composition of the liquid is  $X_A^L = 0,7$  and  $X_B^L = 0,3$ . Determine:

- a) Vapour pressure at 25 ° C and 50 ° C inside the container
- b) The composition of the vapour in equilibrium at 25 ° C and 50 ° C.
- c) When the mixture of propellants go outside where the pressure is 1 atm, what phase was found at both temperatures?

**Data:**  $P_A^*(25) = 1.9 \cdot 10^5 \text{ N} \cdot \text{m}^{-2}$ ;  $T_{b(A)}^\circ = 276.8 \text{ K}$ ;  $\Delta H_{\text{vap}}(A) = 4863.12 \text{ cal} \cdot \text{mol}^{-1}$ ;  
 $P_B^*(25) = 5.85 \cdot 10^5 \text{ N} \cdot \text{m}^{-2}$ ;  $T_{b(B)}^\circ = 243.4 \text{ K}$ ;  $\Delta H_{\text{vap}}(B) = 4615.63 \text{ cal} \cdot \text{mol}^{-1}$ ;  
1 atm = 101300 N·m<sup>-2</sup>; R = 1.987 cal·K<sup>-1</sup>·mol<sup>-1</sup>

\* Fluorinated hydrocarbons as dichlorotetrafluoroethane (A) and chlorodifluoromethane (B) are used as propellants in aerosol pharmaceutical formulation (pressurized containers that contains the active component suspended in a propellant that can expel the product when the valve is opened)

**Solution:** a)  $P(25) = 308,500 \text{ N} \cdot \text{m}^{-2}$ ;  $P(50) = 569 510 \text{ N} \cdot \text{m}^{-2}$

b)  $X_A^V(25^\circ\text{C}) = 0.43$ ;  $X_B^V(25^\circ\text{C}) = 0.57$ ;  $X_A^V(50^\circ\text{C}) = 0.44$ ;  $X_B^V(50^\circ\text{C}) = 0.56$

c) Vapour

**21.** At 90 ° C, the vapour pressure of pure toluene and o-xylene are 400 mmHg and 150 mmHg, respectively. What is the composition of the mixture whose boiling point is 90 ° C under a pressure of 0.5 atm? What is the composition of the vapour in equilibrium?

Assume ideal behaviour.

**Solution:** a)  $X_{\text{o-xylene}}^L = 0.08$ ; b)  $X_{\text{o-xylene}}^V = 0,032$

22. The following data are the vapour pressure of water and the molality of sucrose in aqueous solutions measured at 25 ° C. Check if the solvent satisfies Raoult's law. If not calculate solvent activity and activity coefficient.

<b>m (sucrose) / (mol·Kg<sup>-1</sup>)</b>	0.000	0.200	2.000
<b>P / (mm Hg)</b>	23.75	23.66	22.75

**Solution:**  $m_{\text{suc}} = 0 \Rightarrow$  pure H<sub>2</sub>O;  $m_{\text{suc}} = 0.200 \text{ m} \Rightarrow$  It follows Raoult's law;  
 $m_{\text{suc}} = 2.000 \text{ m} \Rightarrow$  It does not follow Raoult's law ( $a_{\text{I, water}} = 0.9579$ ;  
 $\gamma_{\text{I, water}} = 0.9924$ )

23. At 23 °C, a mixture of two components A and B with 74% moles of A is prepared. The total pressure is 303 mmHg with 74% moles of A in the vapour. Determine:

- the activity and activity coefficient of each component according to convention I.
- the activity and activity coefficient of each component according to convention II, considering A the solvent.
- Describe the system.

**Data:**  $P^*_A(8^\circ\text{C}) = 112 \text{ mmHg}$ ;  $P^*_B(23^\circ\text{C}) = 203 \text{ mmHg}$ ;  $\Delta H_{\text{vap}}(A) = 330 \text{ cal}\cdot\text{mol}^{-1}$ ;  
 $K_B = 361 \text{ mmHg}$ ;  $R = 0.082 \text{ l}\cdot\text{atm}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 1.987 \text{ cal}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 8.314 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$

**Solución:** a)  $\gamma_{A,I} = 2.630$ ;  $\gamma_{B,I} = 1.493$ ; b)  $\gamma_{A,II} = 2.630$ ;  $\gamma_{B,II} = 0.839$

24. Two liquids A and B form non-ideal solutions. At 70 ° C, the vapour pressure of pure A is 280 mm Hg. and for pure B is 650 mm Hg at 30 °C. The total vapour pressure of a solution of 0.5 mole fraction is 500 mm Hg, at 30 ° C and the activity coefficient of B according convention I is 1.3; calculate:

- The activity coefficient of A in this solution
- The activity of both components
- Draw the diagram of vapour pressure versus composition at 30 ° C.

**Data:**  $\Delta \bar{H}_{\text{vap},A} = 4100 \text{ cal}\cdot\text{mol}^{-1}$   
 $R = 0.082 \text{ l}\cdot\text{atm}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 1.987 \text{ cal}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 8.314 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$

**Solution:** a)  $\gamma_{I,A} = 1.22$ ; b)  $a_{I,A} = 0.61$ ;  $a_{I,B} = 0.65$

25. The table below shows the total pressure and the composition of the solution and of the vapour at 25 °C:

$x_A^L$	P (torr)	$X_A^v$
1	500.0	1
0,985	499.6	0.9881
0,950	506.4	0.9615
0,925	517.4	0.9442
0.9	533.0	0.9287
0,875	552.7	0,9152
0.85	576.1	0.9037
0.75	696.9	0.8744

Determine the activity and the activity coefficient of A and B for a solution with  $x_A^L = 0.9$  according to the Convention I and II.

**Data:**  $P_B^*$  (25 °C) = 200 torr

**Solution:** a)  $a_{I,A} = 0.9899$ ;  $\gamma_{I,A} = 1.0999$ ;  $a_{I,B} = 0.1900$ ;  $\gamma_{I,B} = 1.9001$

b)  $a_{II,A} = 0.9899$ ;  $\gamma_{II,A} = 1.0999$ ;  $a_{II,B} = 0.0950$ ;  $\gamma_{II,B} = 0.9508$

26. At 35 °C, the vapour pressures of chloroform and ethanol are 295.1 torr and 102.8 torr. At 35 °C, a solution of chloroform and ethanol with  $X_{et}^l = 0,200$  has a vapour pressure of 304.2 torr and the vapour has a composition  $X_{et}^v = 0,138$ . Calculate:

a)  $\gamma_I$  and  $a_I$  of chloroform and ethanol in this solution.

b)  $\mu_i - \mu_i^*$ , for each component of this solution.

**Data:**  $R = 0.082 \text{ l}\cdot\text{atm}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 1.987 \text{ cal}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 8.314 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$

**Solution:** a)  $\gamma_{I, \text{chlor}} = 1.11$ ;  $\gamma_{I, \text{etha}} = 2.04$ ;  $a_{I, \text{chlor}} = 0.888$ ;  $a_{I, \text{etha}} = 0.408$

b)  $\mu_{\text{chlor}} - \mu_{\text{chlor}}^* = -72.3505 \text{ cal}\cdot\text{mol}^{-1}$ ;  $\mu_{\text{etha}} - \mu_{\text{etha}}^* = -548,1973 \text{ cal}\cdot\text{mol}^{-1}$

27. The following data refer to a mixture of equimolar amounts of two substances A and B, at 308.3 K:

$$P_A = 20,5 \text{ KN}\cdot\text{m}^{-2}$$

$$P_B = 15,5 \text{ KN}\cdot\text{m}^{-2}$$

Calculate:

a) Indicate what kind of deviations respect to Raoult's law present each compound.

b) Represent graphically the vapour pressures of A and B and the total vapour pressure as a function of the mole fraction of B. In the same graph represent the same magnitudes assuming ideal behaviour.

**Data:**  $R = 0.082 \text{ l}\cdot\text{atm}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 1.987 \text{ cal}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = 8.314 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$

$$P_A^*(308.3 \text{ K}) = 49.5 \text{ K}\cdot\text{N}\cdot\text{m}^{-2}; P_B^*(308.3 \text{ K}) = 39.1 \text{ K}\cdot\text{N}\cdot\text{m}^{-2}$$

**Solution:**  $\gamma_{I,A} = 0.8282$ ;  $\gamma_{I,B} = 0.7928 \Rightarrow$  negative deviations with respect to Raoult's law.

28. Given the following aqueous solution at 298 K:

- a) 0.01 M of  $\text{CaCl}_2$
- b) 0.10 M of  $\text{MgSO}_4$
- c) A mixture of  $(\text{NH}_4)_2\text{SO}_4$  0.5 M with Urea 0.5 M

Calculate:

- 1) The ionic strength of each of the solutions.
- 2) The mean ionic activity coefficient in all solutions where possible, using the limiting law of Debye-Huckel.
- 3) What other method could be used to determine the  $\gamma_{\pm}$ ?

**Data:**  $A = 0.51$

**Solution:**

$$\text{Im}(\text{CaCl}_2) = 0.03; \text{Im}(\text{MgSO}_4) = 0.4; \text{Im}((\text{NH}_4)_2\text{SO}_4) = 1.5$$

$$2) \gamma_{\pm}(\text{CaCl}_2) = 0.66$$