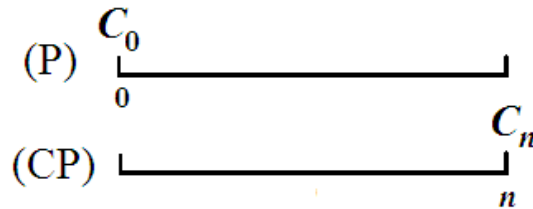


Compound Interest Law



The final capital obtained at the end of every period can be determined by means of the capital available at the beginning of the period

$$\left\{ \begin{array}{l} C_1 = C_0 + C_0 i = C_0 (1 + i) \\ C_2 = C_1 + C_1 i = C_1 (1 + i) = C_0 (1 + i)^2 \\ C_3 = C_2 + C_2 i = C_2 (1 + i) = C_0 (1 + i)^3 \\ C_4 = C_3 + C_3 i = C_3 (1 + i) = C_0 (1 + i)^4 \\ C_n = C_0 (1 + i)^n \end{array} \right.$$

The Final Capital is calculated using the **Compound Interest Law**

Cartagena99

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP: 689 45 44 70

Financial mathematics

Effective Interest Rate

$$\left\{ \begin{array}{l} C_1 = C_0(1+i) \Rightarrow i = \frac{C_1 - C_0}{C_0} \\ C_2 = C_1(1+i) \Rightarrow i = \frac{C_2 - C_1}{C_1} \\ \dots \\ C_n = C_{n-1}(1+i) \Rightarrow i = \frac{C_n - C_{n-1}}{C_{n-1}} \end{array} \right.$$

The EAIR reflects the total Interest produced at the end of every period by every monetary unit available at the beginning of the period

“*i*” is called **Effective Interest Rate** of the financial operation

The Effective Interest rate is a measurement of :

Profitability, if my financial operation is an investment.

Cartagena99

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVIA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70

Financial mathematics

Total Interest in Compound

$$\left. \begin{aligned} C_{n+1} &= C_n (1+i) \\ C_n &= C_{n-1} (1+i) \end{aligned} \right\} \textit{subtract} :$$

$$C_{n+1} - C_n = C_n (1+i) - C_{n-1} (1+i)$$

$$\underbrace{C_{n+1} - C_n}_{I_{n+1}} = \underbrace{(C_n - C_{n-1})}_{I_n} (1+i) \Rightarrow I_{n+1} = I_n (1+i)$$

The Interests from each period grow geometrically and the ratio is

$$(1+i)$$

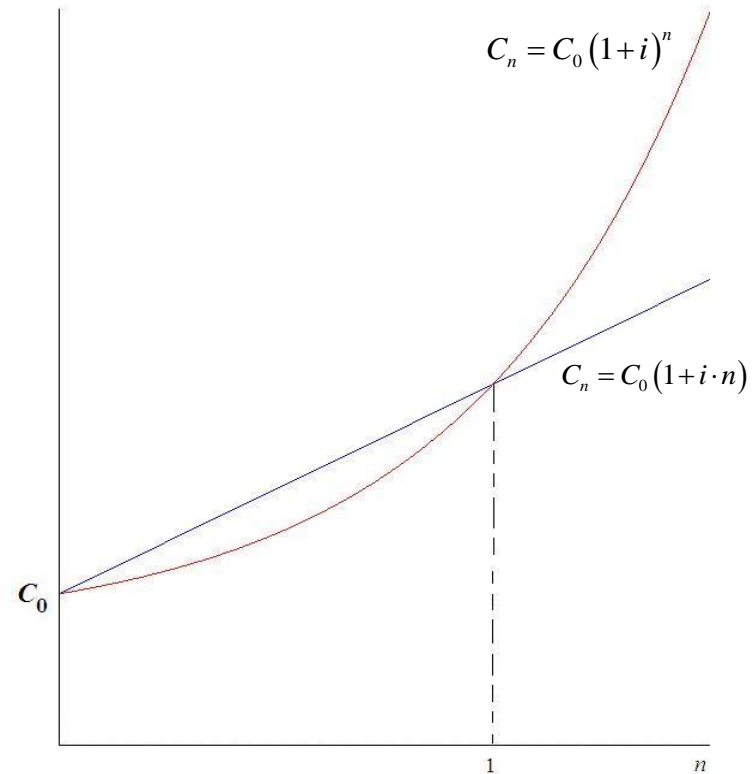
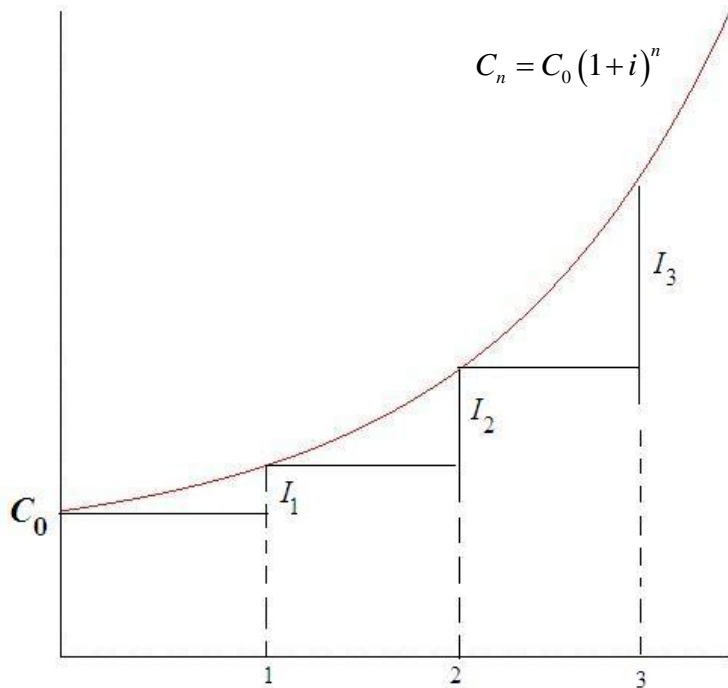
CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70

Cartagena99

Financial mathematics

Compound Interest Graph



Final value

Cartagena99

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

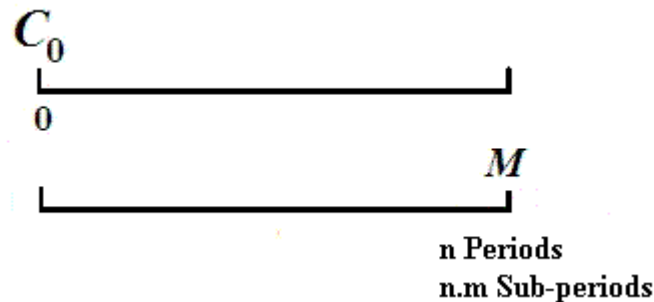
ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP: 689 45 44 70

Financiamientos matemáticos

EQUIVALENT INTEREST RATES IN COMPOUND

Equivalent Interest Rates

Two types of interest rates are said to be equivalent or indifferent using whichever chosen. They will produce the same final value, investing the same amount of money for the same period of time



$$i \Rightarrow M = C_0(1+i)^n$$

$$i_m \Rightarrow M = C_0(1+i_m)^{m \cdot n}$$

$$i \approx i_m \Rightarrow C_0(1+i)^n = C_0(1+i_m)^{m \cdot n} \Rightarrow 1+i = (1+i_m)^m$$

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
 LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
 CALL OR WHATSAPP:689 45 44 70

Cartagena99

Financial mathematics

EQUIVALENT INTEREST RATES IN COMPOUND CAPITALIZATION

Equivalent Interest Rates

Two types of interest rates are said to be equivalent or indifferent using whichever chosen. They will produce the same final value, investing the same amount of money for the same period of time

EQUIVALENT INTEREST RATES IN COMPOUNDING

In compound the equivalent interest rates are not related proportionally . The expression which connects both is:

$$(1+i) = (1+i_m)^m$$

$$\Rightarrow \begin{cases} i = (1+i_m)^m - 1 \\ i_m = (1+i)^{\frac{1}{m}} - 1 \end{cases}$$

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70

Cartagena99

Financial mathematics

ANNUAL PERCENTAGE RATES (APRs) and EFFECTIVE INTEREST RATES (EAIRs)

- Nominal Annual Interest Rate $j(m)$: Indicates that the interest is added to the capital to produce more interest
- m = indicates the number of times that the interest is added to the capital to produce more interest along the year ($m \leq 1$).
- For instance $m = 2$ means that the interest is added to the capital twice a year, that is, at the end of every semester.
-

$$j(m) = m \cdot i_m \qquad i_m = \frac{j(m)}{m}$$

Cartagena99

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70

Financial mathematics

NOMINAL ANNUAL INTEREST RATE (J_m). EFFECTIVE ANNUAL INTEREST RATE (i)

- Example :

A nominal interest rate of $j(2) = 0.1$ means that the interest is added to the capital at the end of every semester. For this reason, it is called nominal annual interest rate, compounding six monthly .

EAIR will be calculated this way:
$$i_2 = \frac{j(2)}{2} = \frac{0,1}{2} = 0,05 = 5\%$$

$$i = (1 + i_2)^2 - 1 = (1 + 0,05)^2 - 1 = 0,1025 = 10,25\%$$

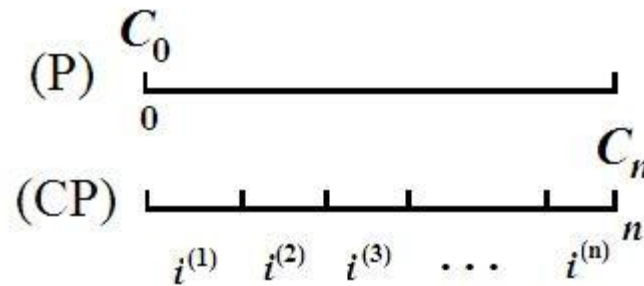
Cartagena99

Financial mathematics

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70

VARIBLE INTEREST RATE WITH COMPOUNDING



$i^{(1)}$ Effective Interest rate for the first period

$i^{(2)}$ Effective Interest rate for the second period

i^3 Effective Interest rate for the third period

i^n Effective Interest rate for the n period

$$C_n = C_0 (1 + i^{(1)}) (1 + i^{(2)}) (1 + i^{(3)}) \dots (1 + i^{(n)})$$

Cartagena99

CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE
LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS
CALL OR WHATSAPP:689 45 44 70