



## SECTION III: PHENOMENOLOGY AND BIOPROCESS RUNNING: LESSON 14. – Scaling-up and Scaling-down

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**Francisco de Vitoria  
UFV Madrid**

# AIMS FOR TODAY'S LESSON

## BIORREACTOR SCALING-UP

**Definition**

**Starting point**

**Scaling-up or numbering-up?**

**Scaling Criterion**

## SCALING-UP and SCALING-DOWN

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## REFERENCES:

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- Doran, P.M. (2010), Bioprocess Engineering Principles, Academic Press (Londres).
- Shuler, M.L. y Kargi, F. (2002), Bioprocess Engineering, Prentice Hall, Upper Saddle River, NJ, EE.UU.

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**1.- BIOREACTOR SCALING-UP**

**2.- SCALING-UP AND SCALING-DOWN**

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# 1.- BIOREACTOR SCALING-UP

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## Bioreactor scaling-up

### SCALING-UP:

“Operation and starting-up of a **commercially-sized unit** whose design and operating procedures are based, in part, on experimentation and demonstration on a **smaller scale** of operation”

“Study of **problems associated with the transfer of experimental data** from laboratory and pilot-plant equipment to large scale industrial equipment.”

➔ It is the process consisting in achieving a fermentation unit operating

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## Bioreactor scaling-up

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### STARTING POINT:

Calculations and experiments carried out on a small scale.

### AIM:

Designing one or more large-scale production units.

### METHODOLOGY:

Progressive conversions from the starting scale to the **desired production.**

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## Bioreactor scaling-up

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### DIFFICULTIES:

- Scaling-up change **cannot be done directly.**
- It **doesn't consist in increasing the number of small-scale units.**
- **Inaccuracy** in the model.
- Process is affected by changes within **response times.**
- **Some surface phenomena** are not considered.
- Change within the **hydrodynamic regime.**
- **Interactions between phenomena** of mass, energy and momentum transport along the scaling up.

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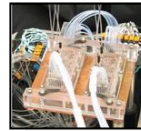
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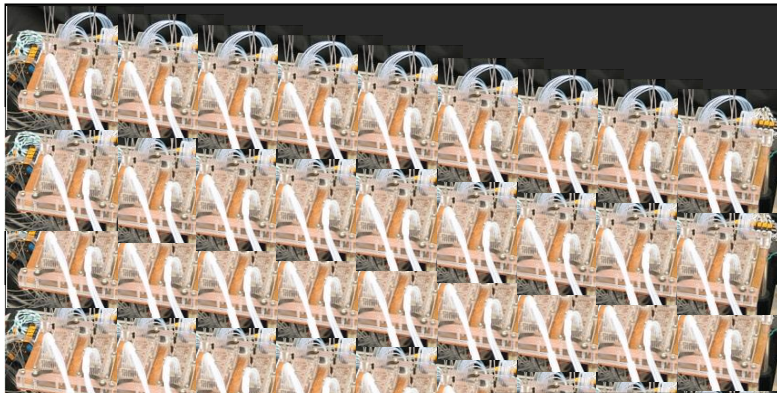
# Bioreactor scaling-up

## DIFFICULTIES:

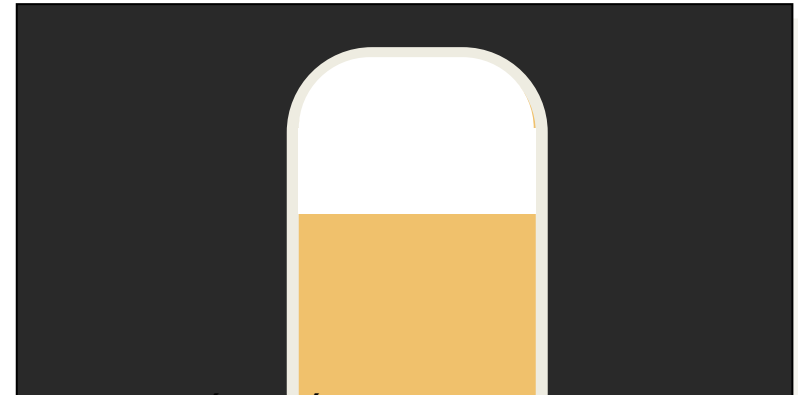
- A protocol developed in a miniature bioreactor should be used for the production of antibiotics.



Numbering up



Scaling up



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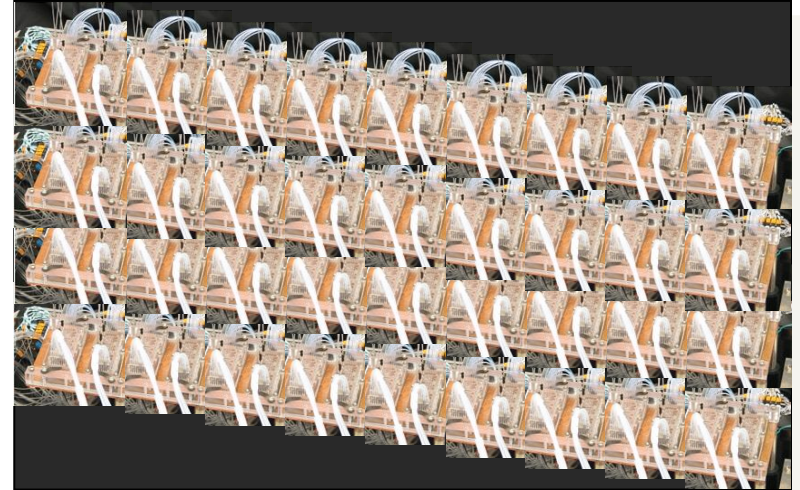
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## Numbering-up

- Parallel connection of the miniature bioreactors
- **Nature's principle**  
Unicellular → Multicellular  
Leaves → Tree → Forest
- **Advantages**  
No risks and compromises through scaling-up  
**„Process Intensification“:**  
good energy and material exchange  
(short diffusion distance)
- **Disadvantages**  
Individual process guidance and control for every single miniature reactor necessary



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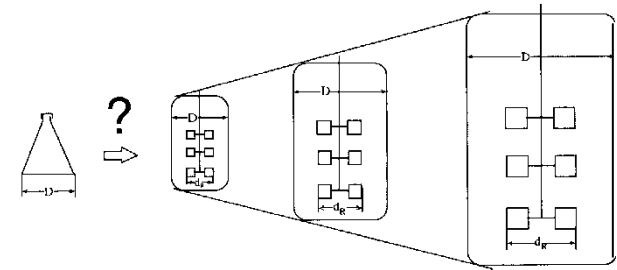
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## Scaling-up

- Scaling-up in practice
  - e.g. 100 ml shake flask → 3 L lab reactor, 100 L pilot plant → 3000 L production plant
- Bioprocesses are dependent on the scale
  - e.g. mixing time increases sharply with an increase in volume
- Aim of scaling-up
  - Similarity of geometrical and physical influence variables
- Which similarity criteria are relevant?
  - Mass transport ( $O_2$ ,  $CO_2$ )



Geometric similarity:  
Prerequisite for scale up

Quelle: Storhas, Bioverfahrensentwicklung, S. 189 ff, S 232 ff

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## Bioreactor scaling-up

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### HIGH COMPLEXITY:

#### EXAMPLE:

Broadly speaking, **height/diameter ratio** between **2:1** and **3:1**.

By **increasing the scale** and keeping this relationship constant, the **surface/volume ratio decreases rapidly**.

- The heat transfer with the exterior changes.
- The aeration and gas withdrawal requirements increase drastically.

**Parameters are affected non-linearly by an increase in size while maintaining the aspect ratio**

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## Bioreactor scaling-up

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### HIGH COMPLEXITY:

### ANALOGY:

A carpenter receives a client who wants to build a cubic box for a circus show. This client shows a wooden sample box presenting 25 cm each side.

He would like to build a 4 times bigger cube for a show.

Calculate dimensions, surface and volume for the structure to be built. If more than one solution is possible, do the calculations for everyone.

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## Bioreactor scaling-up

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“**A Four times bigger cube**” can be understood in many different ways, so that the solution for the problem could consist in:

- Increasing the **cube side four times**.
- Increasing **total volume four times**.
- Increasing **total area four times**. → However, interest in this situation is only explained if the expenses of material used need to be controlled.

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## Bioreactor scaling-up

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Anyway, equations putting into relationship side, surface and volume of the cubic structure are the following ones:

$$S = 6L^2 \quad [1]$$

$$V = L^3 \quad [2]$$

Where,

**L**, in the side of the cubic structure,

**S** is the total surface area of the structure and

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## Bioreactor scaling-up

### Initial situation

$$L_0 = 25 \text{ cm} = 0,25 \text{ m}$$

$$S_0 = 6 \cdot (0,25)^2 = 0,375 \text{ m}^2$$

$$V_0 = (0,25)^3 = 0,016 \text{ m}^3$$

### Increasing the **cube side four times**

$$L_1 = 4 \cdot 25 \text{ cm} = 100 \text{ cm} = \mathbf{1 \text{ m}}$$

$$S_1 = 6 \cdot 1^2 = \mathbf{6 \text{ m}^2}$$

$$V_1 = 1^3 = \mathbf{1 \text{ m}^3}$$

$$L_1/L_0 = 4$$

$$S_1/S_0 = 16 = 4^2$$

$$V_1/V_0 = 64 = 4^3$$

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## Bioreactor scaling-up

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$$V_0 = (0,25)^3 = 0,016 \text{ m}^3$$

### Increasing total volume four times

$$V_2 = 4 \cdot V_0 = 4 \cdot 0,016 = 0,0625 \text{ m}^3 \rightarrow L_2 = \sqrt[3]{V_0 \cdot 4} = \sqrt[3]{4} \cdot L_0 = 0.397 \text{ m}$$

$$L_2 = \mathbf{0,397 \text{ m}}$$

$$S_2 = 6 \cdot (0,397)^2 = \mathbf{0,945 \text{ m}^2}$$

$$V_2 = \mathbf{0,0625 \text{ m}^3}$$

$$L_2/L_0 = 1,587 = 4^{1/3}$$

$$S_2/S_0 = 2,520 = 4^{2/3}$$

$$V_2/V_0 = 4$$

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## Bioreactor scaling-up

### Initial situation

$$L_0 = 25 \text{ cm} = 0,25 \text{ m}$$

$$S_0 = 6 \cdot (0,25)^2 = 0,375 \text{ m}^2$$

$$V_0 = (0,25)^3 = 0,016 \text{ m}^3$$

### Increasinge total area four times

$$S_3 = 4 \cdot S_0 = 4 \cdot 0,375 = 1,5 \text{ m}^2 \rightarrow L_3 = \sqrt{\frac{S_0 \cdot 4}{6}} = \sqrt{\frac{6 \cdot L_0^2 \cdot 4}{6}} = 2 \cdot L_0 = 0,5 \text{ m}$$

$$L_2 = 0,5 \text{ m}$$

$$S_2 = 6 \cdot (0,5)^2 = 1,5 \text{ m}^2$$

$$V_2 = (0,5)^3 = 0,125 \text{ m}^3$$

$$L_2/L_0 = 2 = 4^{1/2}$$

$$S_2/S_0 = 4$$

$$V_2/V_0 = 8 = 4^{3/2}$$

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## Bioreactor scaling-up

TO SUM UP:

	Relationship Side / Initial Side	Relationship Surface / Initial Surface	Relationship Volume / Initial Volume
Increasing side	4	4 <sup>2</sup>	4 <sup>3</sup>
Increasing surface	4 <sup>1/2</sup>	4	4 <sup>3/2</sup>
Increasing volume	4 <sup>1/3</sup>	4 <sup>2/3</sup>	4

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## Bioreactor scaling-up

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### HIGH COMPLEXITY:

#### ANALOGY:

Dimensions, total surface and volume do not keep a linear relation between each other, but potential instead, because of the geometry

→ Increasing each characteristics of the cube, does not affect the other ones in the same way.

It is necessary to **clearly define the scale change criterion** to

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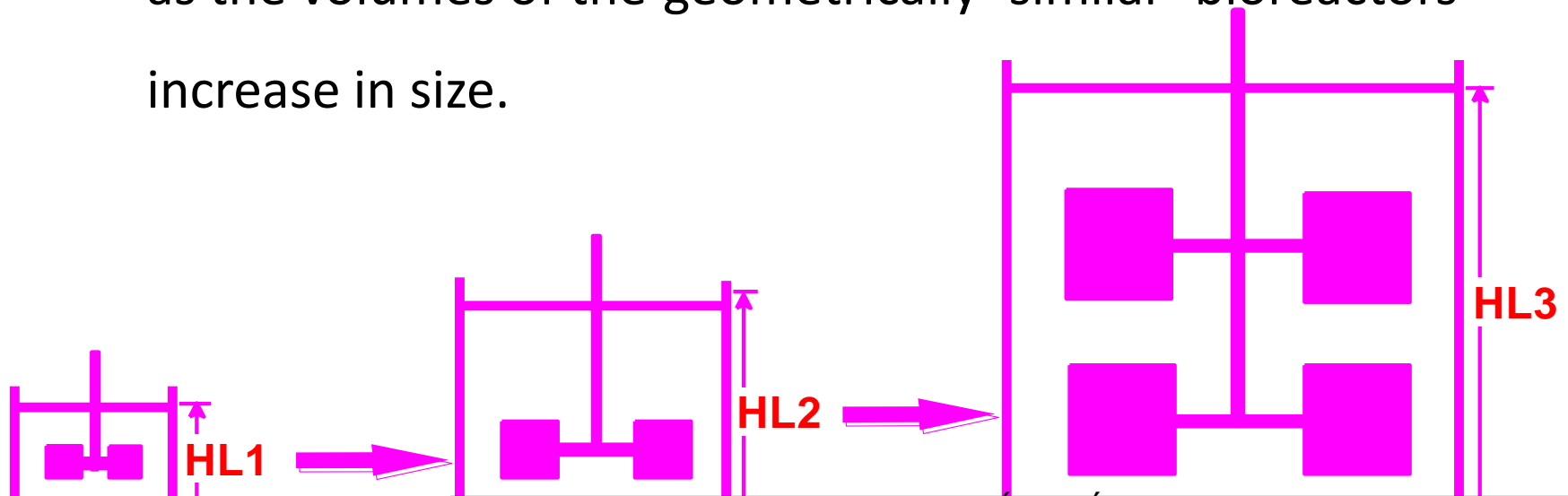
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## Scale-up Criterion

### IDEAL SCALING-UP CRITERION:

- That **parameter** which has the **same numerical value** as the volumes of the geometrically similar bioreactors increase in size.



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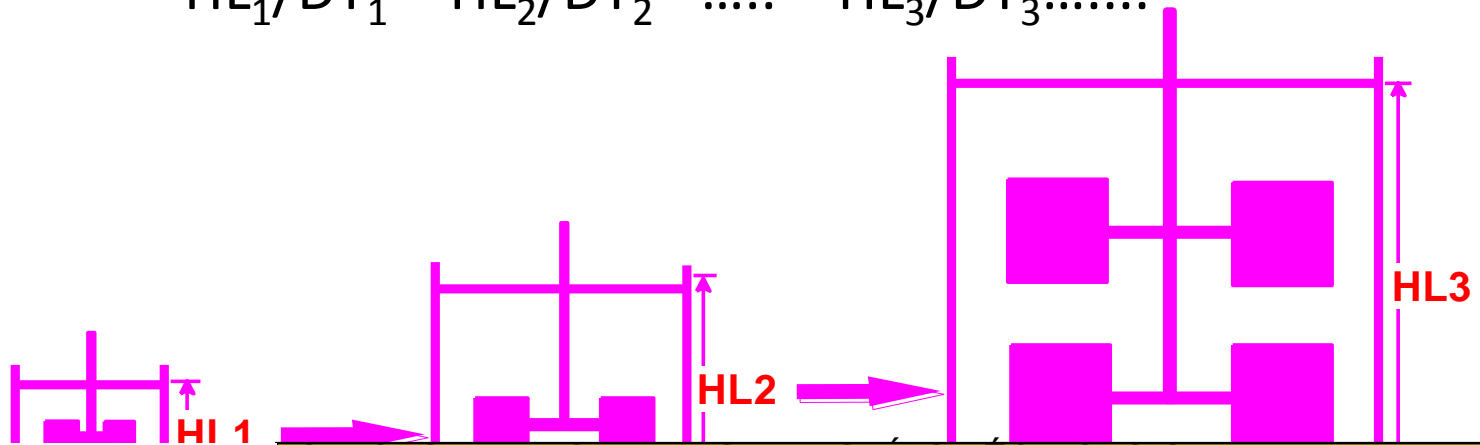
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## Scale-up Criterion

### IDEAL SCALING-UP CRITERION:

- First scale-up criterion is maintaining **Geometrical Similarity**:

$$HL_1/DT_1 = HL_2/DT_2 = \dots = HL_3/DT_3 \dots$$



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## Scale-up Criterion

### EXAMPLE:

For a given

- Medium Composition
- Temperature
- pH

We want to maximize the cell yield factor  $Y_{x/s}$ .

We start with a 10 L Laboratory scale bioreactor unit and we perform optimization experiments at different volumetric rates of oxygen supply, OTR.

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## Scale-up Criterion

### EXAMPLE:

Where:

$$\begin{aligned} \text{OTR} &= K_{La} (C_L^* - C_L) \\ &= (\text{moles O}_2)/(\text{L})(\text{hr}) \end{aligned}$$

$$\begin{aligned} Y_{x/s} &= \text{Cell to substrate yield} \\ &= (\text{g CDW yeast cells})/(\text{g glucose used}) \end{aligned}$$

Using the 10 L laboratory scale bioreactor we carry out experiments and we get the following hypothetical results shown in the following Figure.

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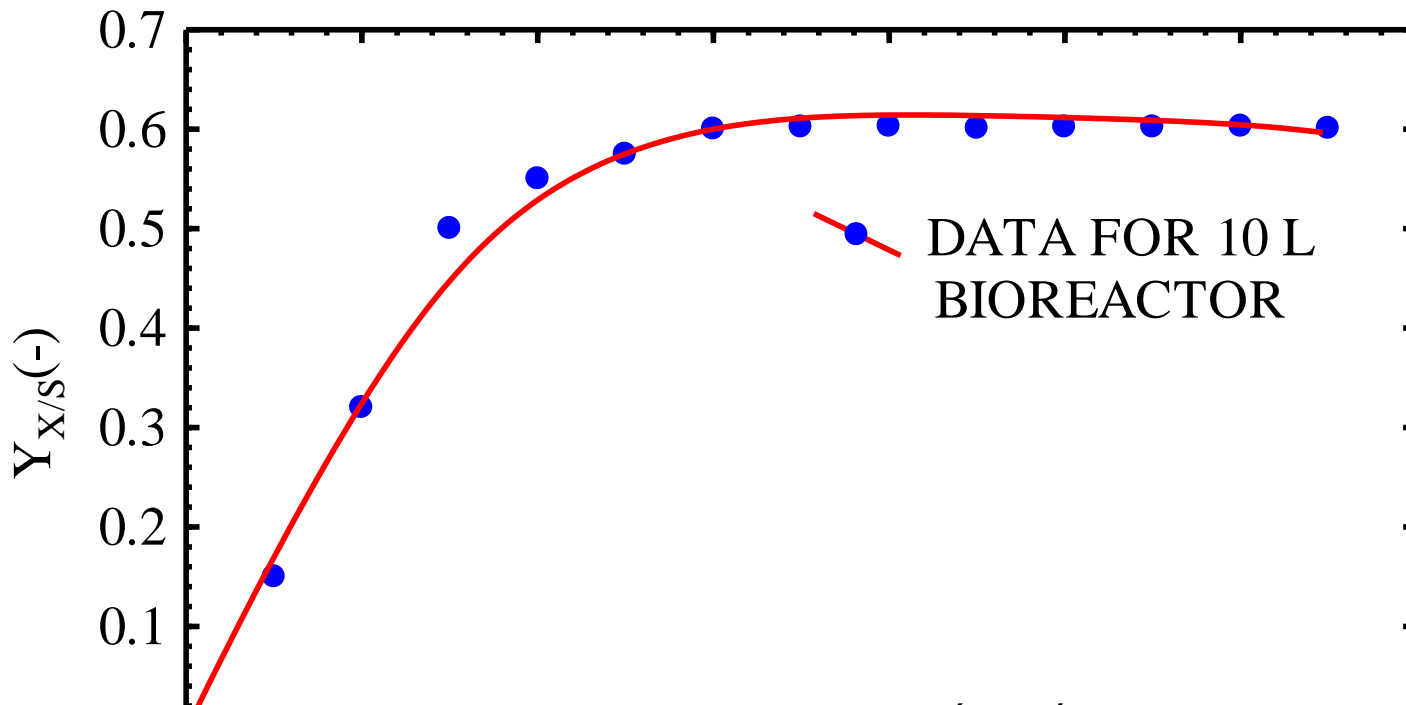
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# Scale-up Criterion

## EXAMPLE:



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## Scale-up Criterion

### EXAMPLE:

When we scale-up to 50,000 L bioreactor system, are we going to get the same  $Y_{X/S}$  vs. OTR relationship?

- It depends on **what scale-up criteria** we use.
- If the volumetric rate of oxygen transfer OTR were a true scale-up criterion, then the relationship between  $Y_{X/S}$  vs. OTR for the 10 L bioreactor **should be exactly the same** for any bioreactor size.
- if experiments were done with bioreactors of 10 L, 1,000 L, 10,000 L,

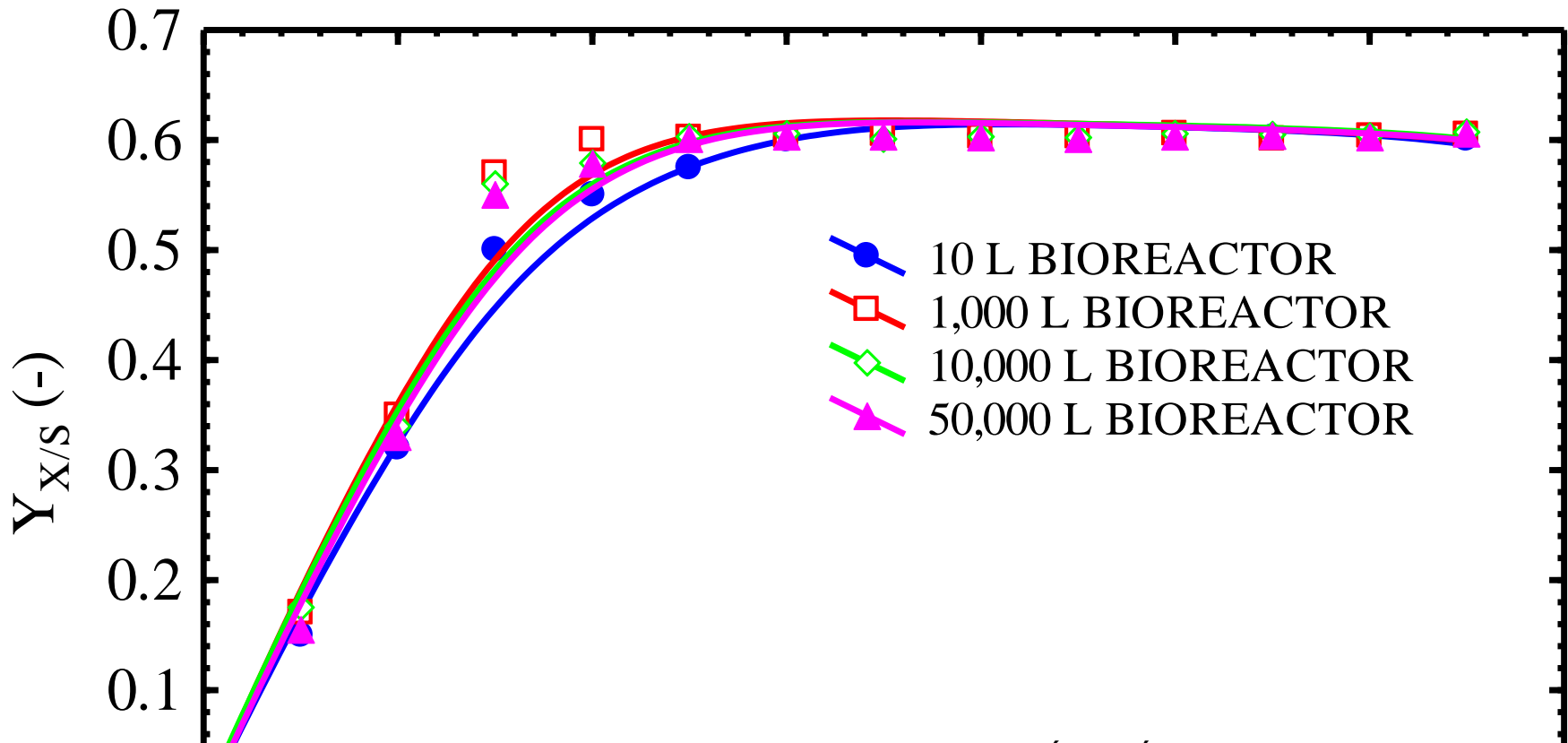
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### Scale-up Criterion



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$$R = K_L a (C_L^* - C_L)$$

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## Scale-up Criterion

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- In reality scale-up of laboratory and pilot-plant data to commercial size industrial bioreactors is **very difficult and complicated**.
- **No actual data or correlation** exist for scale-up.
- **Different people use different scale-up criteria** to design commercial size bioreactor systems.
- In industry there are a lot of **trade secrets** on scale-up of bioreactors, and **very few published** results exist in the literature.

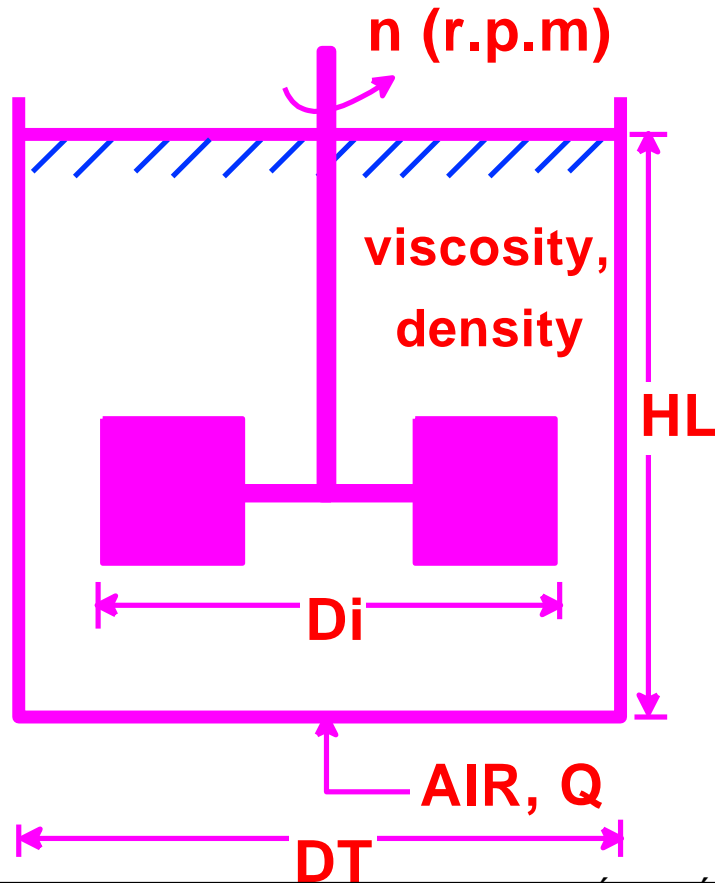
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## Scale-up Criterion



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## Scale-up Criterion

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- Scale-up criteria in general are a function of independent variables **N, Di, DT, HL, Qg,  $\mu$ ,  $\rho$** .
- Once a criteria is selected, then you make sure that the **numerical value of this scale-up criterion is the same** for the small and large size bioreactor.

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## Scale-up Criterion

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In general, the choice of scale-up criterion depends on two considerations:

### a) Nature of fermentation and culture morphology

- Aerobic / Anaerobic.
- Bacteria / Fungi / Mammalian Cells / Plant Cells.
- Exothermic character.
- Thermophilic organisms.
- Viscosity of culture.
- Newtonian fluid / Non-Newtonian fluid.

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## Scale-up Criterion

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In general, the choice of scale-up criterion depends on two considerations:

**b) What is being looked for to be maximized:**

- Yield of product or biomass
- Concentration of cells
- Concentration of the product
- Activity of the product.
- Productivity per unit volume of the bioreactor.

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## Scale-up Criterion

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- Different scale-up criteria have been used **depending on the type of fermentation** and the **objective of optimization**.
- The **first assumption is geometric similarity** between bioreactor vessels of different sizes.
- However, in **some scale-up cases geometric similarity is not preserved**. This makes scale-up much **more complex**.

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## Scale-up Criterion

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- $K_{La}$
- Power Per Unit Liquid Volume
- Tip Velocity of the Impeller
- Aeration Number
- Impeller Reynolds Number.

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## Scale-up Criterion (1) Volumetric Mass Transfer Coefficient

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$$(KLa)_1 = (KLa)_2$$

Where:

1 = small scale bioreactor

2 = large scale bioreactor

This criterion is usually applied to **aerobic systems** where **oxygen concentration is most important** and affects metabolism of the microbial cell.

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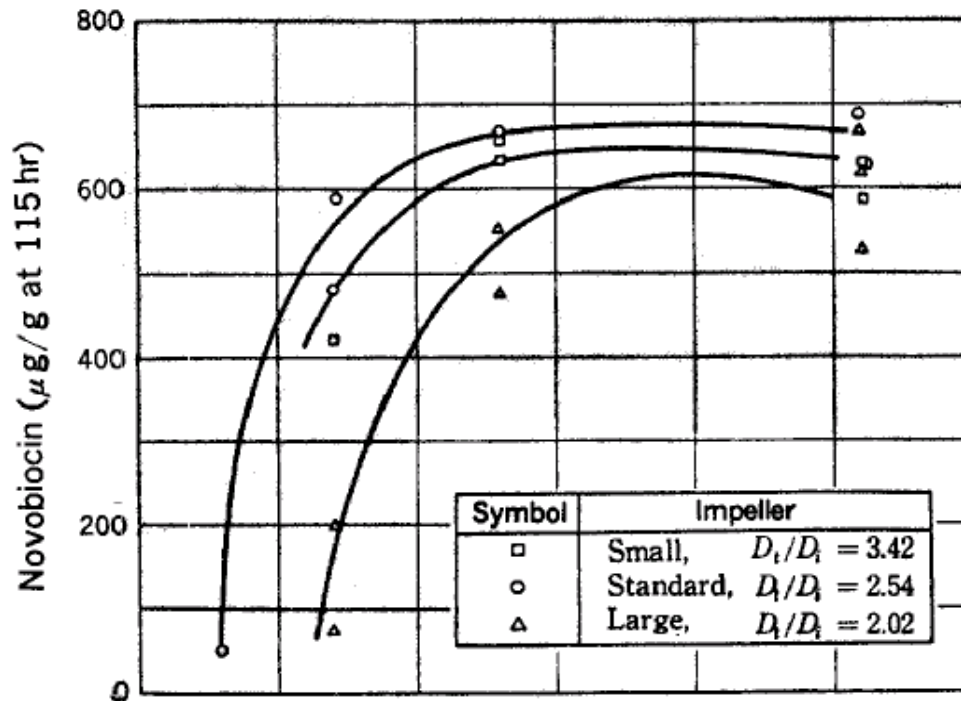
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## Scale-up Criterion (2) Power Per Unit Liquid Volume

$$(P/V_L)_1 = (P/V_L)_2$$



The majority of aerobic fermentor systems have been scaled-up on the  $K_L a$  basis and very few on the  $P/V_L$  basis.

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## Scale-up Criterion (3) Tip Velocity of the Impeller

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$$(N \cdot D)_1 = (N \cdot D)_2$$

This scale-up criterion is used for **shear sensitive fermentations** where a maximum shear rate is allowed to prevent possible irreversible shear damage to the cells growing inside the bioreactor.

In some cases where the **cells have a tendency to form dense flocks**, it is necessary to provide at least the minimum shear rate required to break-up these flocks.

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## Scale-up Criterion (4) Aeration Number

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$$(N_a)_1 = (N_a)_2$$

$$N_a = Q/(n D_i^3) = Q/[(n D_i)(D_i^2)]$$

In cases where expense on stirring is desive.

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## Scale-up Criterion (5) Impeller Reynolds Number

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$$(\text{Re})_1 = (\text{Re})_2$$

This criterion is used sometimes when the **heat transfer rate** from the fermentation broth to the cooling coils inside the bioreactor vessel is of paramount importance.

This is especially important for **thermophilic microorganisms**.

The **heat transfer coefficient** is a function of **impeller Reynolds number**

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## Scale-up Criterion

### EXAMPLE:

Oldshue worked out relationships between properties for scale-up from 80 L to 10,000 L bioreactor, which was not aerated but agitated with a six blade turbine impeller.

- Standard geometry vessel was used and geometric similarity was applied.
- Volumetric scale-up ratio =  $V_2/V_1 = 10,000/80 = 125$
- Impeller diameter scale-up ratio =  $Di_2/Di_1 = 5$

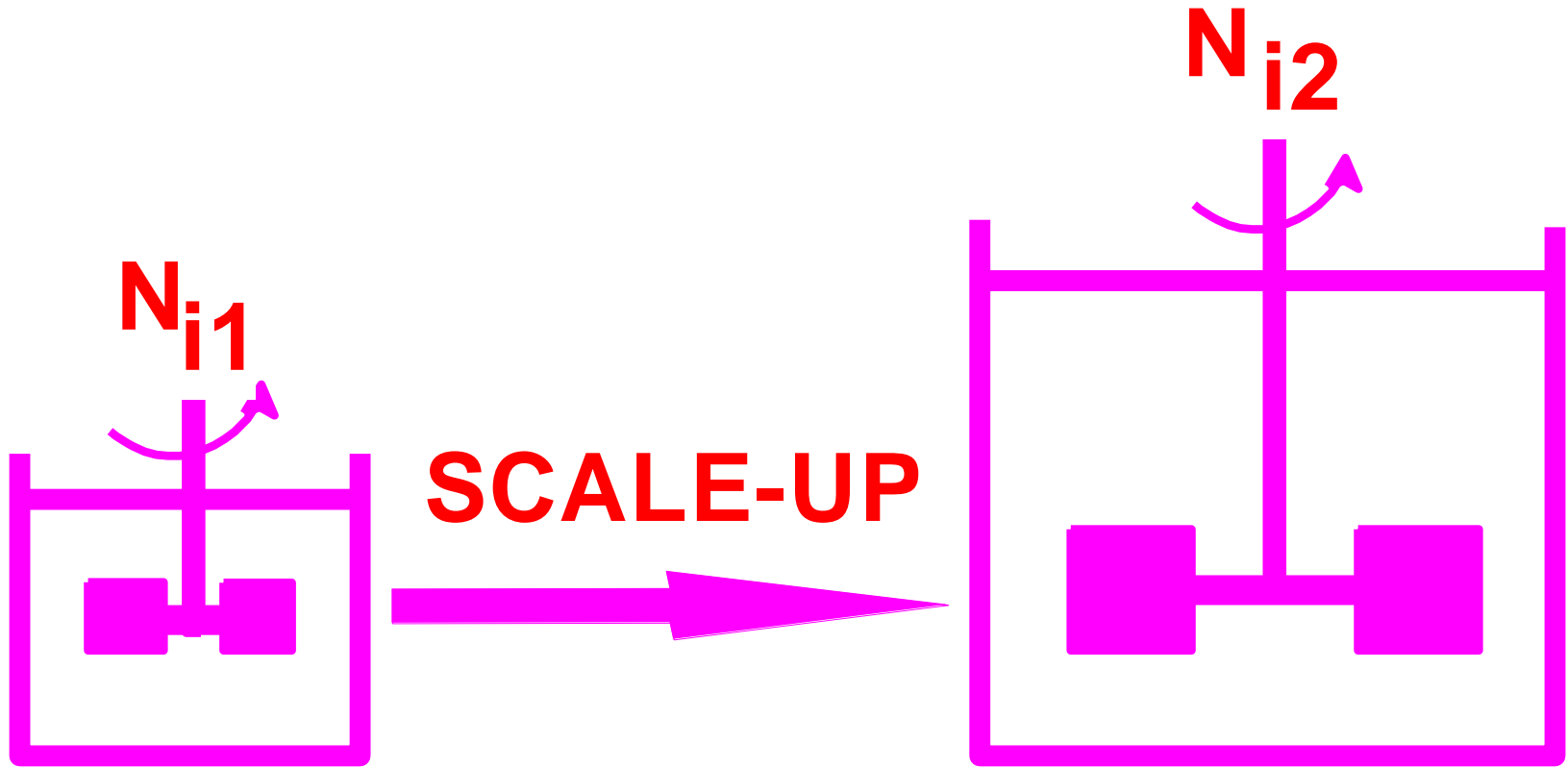
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# Scale-up Criterion



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# (1) Scale-up Criterion:

$$(P/V_L)_1 = (P/V_L)_2$$

Property	80 L bioreactor	10,000L bioreactor
P (ungassed power)	1.0	125.00
$N_i$ (r.p.m)	1.0	0.34
$D_i$ (imp. diameter)	1.0	5.00
F (pumping rate)	1.0	42.50
$F/V_L$ (liquid circ. rate)	1.0	0.34
$N_i D_i$ (imp. tip speed)	1.0	1.70
$N_{Re}$ (Reynolds No.)	1.0	8.50

Note:  $N_2 = (N_1 D_1^2) / D_2$

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## (2) Scale-up Criterion: Same Liquid

$$\text{Circulation Rate } (F/V_L)_1 = (F/V_L)_2$$

Property	80 L Small scale	10,000L large scale
P (ungassed power)	1.0	3125.0
$P/V_L$	1.0	25.0
$N_i$ (r.p.m)	1.0	1.0
$D_i$ (imp. diameter)	1.0	5.0
F (pumping rate)	1.0	125.0
$N_i D_i$ (imp. tip speed)	1.0	5.0

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### (3) Scale-up Criterion:

Same Impeller Tip Velocity  $(N_i D_i)_1 = (N_i D_i)_2$

Property	80 L Small scale	10,000L Large scale
P	1.0	25.0
$P/V_L$	1.0	0.2
$N_i$	1.0	0.2
$D_i$	1.0	5.0
F	1.0	25.0
$F/V_T$	1.0	0.2

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# (4) Scale-up Criterion: Same Impeller

$$\text{Reynolds Number } (N_{Re})_1 = (N_{Re})_2$$

Property	80 L Small scale	10,000L Large scale
P	1.0	0.2
$P/V_L$	1.0	0.0016
$N_i$	1.0	0.04
D:	1.0	5.0
$F/V_L$	1.0	0.2

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## Bioreactor scaling-up

Parameter	Definition	Scale-Up Factor	Why is this Important?
<b>Mixing Time</b>	Amount of time it takes the bioreactor to create a homogeneous environment	$N_2 = N_1 (D_1 / D_2)^{1/4}$ N <sub>2</sub> agitation speed in scale-up N <sub>1</sub> agitation speed in scale-down D <sub>1</sub> impeller diameter of scale-down D <sub>2</sub> impeller diameter of scale-up	<ul style="list-style-type: none"> <li>•Want to ensure that the materials are well-mixed in a timely manner</li> </ul>
<b>Power Input per Volume (P/V)</b>	Amount of power transferred to a volume of cell culture through the agitator shaft and impellers	$P/V \approx N^3 / D^2$ P- power supplied V- Volume of Bioreactor N- Agitation Speed D- Impeller Diameter	<ul style="list-style-type: none"> <li>•Mammalian cells cannot handle a lot of power introduced into the culture media as it can cause small eddies that will shear the fragile cell membranes</li> </ul>
<b>Tip Speed</b>	Related to the shear rate	$N_2 = N_1 (D_1 / D_2)$ N <sub>2</sub> agitation speed in scale-up N <sub>1</sub> agitation speed in scale-down	<ul style="list-style-type: none"> <li>•High shear rates can cause the cell membrane to tear and the cells to die.</li> </ul>

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## Bioreactor scaling-up

Parameter	Definition	Scale-Up Factor	Why is this Important?
<b>Vessel Volumes per Minute (VVM)</b>	means the volume of gas flow (usually measured in slpm, standard liters per minute) per bioreactor volume per minute.	Volume of Gas Flow/time	<ul style="list-style-type: none"> <li>necessary to ensure that enough oxygen will be supplied to the cells</li> </ul>
<b>Superficial Gas Velocity (<math>V_s</math>)</b>	volume of gas per cross-sectional area of the vessel.	$V_s = Q_{\text{gas}}/A_v$ $V_s$ - superficial gas velocity $Q_{\text{gas}}$ - gas volumetric flow rate $A_v$ - inside cross-sectional area of vessel	<ul style="list-style-type: none"> <li>increasing <math>V_s</math> causes an increase in foam generation</li> </ul>



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# Bioreactor scaling-up



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**1.- BIOREACTOR SCALING-UP**

**2.- SCALING-UP AND SCALING-DOWN**

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## 2.- SCALING-UP AND SCALING-DOWN

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## SCALING-DOWN

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"Building a smaller experimental system that replicates the conditions existing on a current bigger one."

- **Imitate or reproduce** installations on a smaller scale.
- Parameters can be evaluated **more quickly**, and at lower cost.
- The **calculations** used when scaling-down **are the same** when scaling-up.

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**ANY QUESTION?**

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## SECTION III: PHENOMENOLOGY AND BIOPROCESS RUNNING: LESSON 14. – Scaling-up and Scaling-down

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