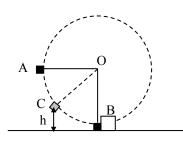


## **Physics Biomedical Engineering**

**Problem Sheet 5** 

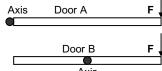
Dynamics of systems of particles

- Two bodies, masses 500 and 1000 kg, move at the same speed, 180 km/h. Determine their respective velocities after a frontal, inelastic collision Ans: 60 km/h
- 2. An artillery shell is fired forming an angle of 45°, initial speed 30 m/s. It explodes into two equal-mass fragments in the highest point of its trajectory. The first fragment continues in the direction of motion at velocity of 45 m/s. Determine what is the distance from firing point reached by the second fragment. Ans: 40,35 m from firing point
- A body of mass m is on a horizontal plane at rest. Another body collides elastically with it at velocity V and it deviates an angle  $\alpha$ . Calculate the velocities of both bodies after collision. Ans:  $|\vec{v_i}| = V \cdot \cos \alpha$  with angle  $\alpha$ ;  $|\vec{v}_2| = V \cdot sen\alpha$  with angle -(90° -  $\alpha$ )
- The simple pendulum of the figure has a mass  $m_1 = 20$  kg, and it is tied to a rope of length 1,5 m. We leave this mass to fall down from position A. When it reaches position B, it collides elastically with other mass  $m_2 = 25 \text{ kg}$ , initially at rest, no friction. Because of the collision, m<sub>1</sub> bounces back and reaches point C, at height h. Determine: a) Velocity of m<sub>1</sub> at point B before collision, and the tension of the rope at that precise instant. b) Velocities of m<sub>1</sub> and m<sub>2</sub> after collision. c) Kinetic energy Ek lost by m<sub>1</sub> during collision. d)



**Ans**: a) v = 5, 42 m/s; T = 588 N; b)  $v_1 = -0.60$  m/s;  $v_2 = 4.82$  m/s; c)  $\Delta Ek = -290.2$  J; h = 18.5 mm.

- Consider a pulley with mass 10 kg and radius 10 cm. Two masses,  $m_1 = 13$  kg and  $m_2 = 7$  kg, hang from an inextensible and weightless rope. Both masses at rest. Let  $g = 10 \text{ m/s}^2$  and the Moment of Inertia of the pulley ½ MR<sup>2</sup>. Determine: a) Linear acceleration of the bodies and angular acceleration of the pulley; b) Kinetic energy of each body and the pulley after 2 secs. Ans.: a) 2,4 m/s<sup>2</sup>, 24 rad/s<sup>2</sup>; b) 149,76 J, 80,64 J, 9,22 J
- The figure shows two identical doors seen from above. The same force F acts on the doors. The door A rotates around an axis located in its leftmost edge. The door B rotates around an axis located in its middle point. The door A rotates a given angle after 3 secs (initially at rest). How much time takes the door B to rotate the same angle?  $I_A = (1/3)Ml^2$ ,  $I_B = (1/12)Ml^2$ . Ans.: 2,12 s



- 7. A cylinder  $(I = 1/2 \cdot m \cdot R^2)$  rolls over a horizontal surface at speed v. Determine the work needed for stopping it **Ans.**: 3/4mv<sup>2</sup>.
- A solid sphere radius R and a solid cube are on top of a ramp, height H. The sphere rolls without slipping, the cube slides with no friction. The moment of inertia of the sphere is  $I = 2/5 \cdot M \cdot R^2$ . a) Calculate the velocities of the bodies when reaching the zero-level height. b) Determine which body arrives the first to the base of the ramp.

Ans:  $v_{sphere} = sqrt(10 g H/7)$ ;  $v_{cube} = sqrt(2gH)$  b) The cube arrives the first.

9. A person (mass 91kg) jumps into a moving boat (mass 510 kg) with another person already on board (mass 75 kg) Initial speed of the boat is 11 m/s. What is the speed of the boat after the jump? Ans: 9.52 m/s.



CLASES PARTICULARES, TUTORÍAS TÉCNICAS ONLINE LLAMA O ENVÍA WHATSAPP: 689 45 44 70

ONLINE PRIVATE LESSONS FOR SCIENCE STUDENTS CALL OR WHATSAPP:689 45 44 70