

Computational Logic

Introduction to Logic Programming

Overview

1. Syntax: data
2. Manipulating data: Unification
3. Syntax: code
4. Semantics: meaning of programs
5. Executing logic programs

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Syntax: Terms (Variables, Constants, and Structures)

- **Variables:** start with uppercase character (or “_”), may include “_” and digits:
Examples: X, Im4u, A_little_garden, _, _x, _22
- **Constructor:** (or **functor**) lowercase first character, may include “_” and digits.
Also, some special characters. Quoted, any character:
Examples: a, dog, a_big_cat, x22, ‘Hungry man’, [], *, >
, Doesn’t matter’
- **Structures:** a constructor (the structure name) followed by a fixed number of arguments between parentheses:
Example: date(monday, Month, 1994)
Arguments can in turn be variables, constants and structures.
- **Constants:** structures without arguments (only name) and also numbers (with the usual decimal, float, and sign notations).
 - ◆ Numbers: 0, 999, -77, 5.23, 0.23e-5, 0.23E-5.

Syntax: Terms

- **Arity:** is the number of arguments of a structure. Constructors are represented as *name/arity* (e.g., date/3).
 - ◆ A constant can be seen as a structure with arity zero.
- Variables, constants, and structures as a whole are called **terms** (they are the terms of a first-order language): the *data structures* of a logic program.
- Examples:

Term	Type	Constructor
dad	constant	dad/0
time(min, sec)	structure	time/2

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Manipulating Data Structures (Unification)

- **Unification** is the only mechanism available in logic programs for manipulating data structures. It is used to:
 - ◆ Pass parameters.
 - ◆ Return values.
 - ◆ Access parts of structures.
 - ◆ Give values to variables.
- Unification is a procedure to solve equations on data structures.
 - ◆ As usual, it returns a minimal solution to the equation (or the equation system).
 - ◆ As many equation solving procedures it is based on isolating variables and then substituting them by their values.

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Unification

- **Unifying two terms A and B:** is asking if they can be made syntactically identical by giving (minimal) values to their variables.
 - ◆ I.e., find a solution θ to equation $A \equiv B$ (or, if impossible, *fail*).
 - ◆ Only variables can be given values!
 - ◆ Two structures can be made identical only by making their arguments identical.

E.g.:

A	B	θ	$A\theta$	$B\theta$
dog	dog	\emptyset	dog	dog
x	a	{x = a}	a	a
x	y	{x = y}	y	y

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Unification Algorithm

Let A and B be two terms:

1. $\theta = \emptyset, E = \{A = B\}$
2. while not $E = \emptyset$:
 - 2.1. delete an equation $T = S$ from E
 - 2.2. case T or S (or both) are (distinct) variables. Assuming T variable:
 - (occur check) if T occurs in the term $S \rightarrow$ halt with failure
 - substitute variable T by term S in all terms in θ
 - substitute variable T by term S in all terms in E
 - add $T = S$ to θ
- 2.3. case T and S are non-variable terms:
 - if their names or arities are different \rightarrow halt with failure
 - obtain the arguments $\{T_1, \dots, T_n\}$ of T and $\{S_1, \dots, S_n\}$ of S
 - add $\{T_1 = S_1, \dots, T_n = S_n\}$ to E
3. halt with θ being the m.g.u of A and B

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Unification Algorithm Examples (I)

- Unify: $A = p(x, x)$ and $B = p(f(z), f(w))$

θ	E	T	S
\emptyset	$\{p(x, x) = p(f(z), f(w))\}$	$p(x, x)$	$p(f(z), f(w))$
	$\{\}$	$x = f(z), x = f(w)$	x
$\{x = f(z)\}$	$\{f(z) = f(w)\}$	$f(z)$	$f(z)$
$\{x = f(z)\}$	$\{z = w\}$	z	$f(w)$
$\{x = f(w), z = w\}$	$\{\}$	w	

- Unify: $A = p(x, f(y))$ and $B = p(z, x)$

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Unification Algorithm Examples (II)

- Unify: $A = p(X, f(Y))$ and $B = p(a, g(b))$

$$\frac{\theta}{\begin{array}{c} E \\ \{ p(X, f(Y)) = p(a, g(b)) \} \\ \{ X = a, f(Y) = g(b) \} \\ \{ X = a \} \\ fail \end{array}} \quad \frac{T}{\begin{array}{c} T \\ \{ p(X, f(Y)) = p(a, g(b)) \} \\ \{ X = a, f(Y) = g(b) \} \\ \{ f(Y) = g(b) \} \\ f(Y) \\ g(b) \end{array}} \quad \frac{S}{\begin{array}{c} S \\ p(X, f(Y)) \\ p(a, g(b)) \\ a \\ f(Y) \\ g(b) \end{array}}$$

- Unify: $A = p(X, f(X))$ and $B = p(Z, Z)$

$$\frac{\theta}{\begin{array}{c} E \\ \{ p(X, f(X)) = p(Z, Z) \} \\ \{ X = Z, f(X) = Z \} \\ \{ X = Z \} \\ fail \end{array}} \quad \frac{T}{\begin{array}{c} T \\ \{ p(X, f(X)) = p(Z, Z) \} \\ \{ X = Z, f(X) = Z \} \\ \{ f(Z) = Z \} \\ f(Z) \\ Z \end{array}} \quad \frac{S}{\begin{array}{c} S \\ p(X, f(X)) \\ p(Z, Z) \\ X \\ Z \\ Z \end{array}}$$

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Syntax: Literals and Predicates (Procedures)

- **Literal:** a predicate name (like a functor) followed by a fixed number of arguments between parentheses:

Example: arrives(john, date(monday, Month, 1994))

- The arguments are *terms*.
- The number of arguments is the *arity* of the predicate.
- Full predicate names are denoted as *name/arity* (e.g., arrives/2).
- Literals and terms are syntactically identical!
- But, they are distinguished by context:
if dog(name(barry), color(black)) is a literal

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Syntax: Operators

- Functors and predicate names can be defined as prefix, postfix, or infix operators (just syntax!).
- Examples:

a + b	is the term	+ (a, b)	if + /2 declared infix
- b	is the term	- (b)	if - /1 declared prefix
a < b	is the term	< (a, b)	if < /2 declared infix
john father mary	is the term	father(john, mary)	if father /2 declared infix
- We assume that some such operator definitions are always preloaded, so that they can be always used.

Syntax: Clauses (Rules and Facts)

- Rule: an expression of the form:

```
p0(t1, t2, ..., tn0) :-  
    p1(t11, t21, ..., tn11),  
    ...  
    pm(t1m, t2m, ..., tnmm).
```

- ◆ $p_0(\dots)$ to $p_m(\dots)$ are **literals**.
- ◆ $p_0(\dots)$ is called the **head** of the rule.
- ◆ The p_i to the right of :- are called **goals** and form the **body** of the rule.
They are also called **procedure calls**.
- Literally, :- is called the **neck** of the rule

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Syntax: Clauses

Rules and facts are both called **clauses** (since they are clauses in first-order logic) and form the code of a logic program.

- Example:

```
meal(soup, beef, coffee).
meal(First, Second, Third) :-  
    appetizer(First),  
    main_dish(Second),  
    dessert(Third).
```

- :- stands for \leftarrow , i.e., logical implication (but written “backwards”).

Comma is conjunction.

- ◆ Therefore, the above rule stands for:

```
appetizer(First) \wedge main_dish(Second) \wedge dessert(Third) →
```

```
    meal(First, Second, Third)
```

- ◆ And thus, is a *Horn clause* of the form:

```
¬ appetizer(First) ∨ ¬ main_dish(Second) ∨ ¬ dessert(Third) ∨  
    meal(First, Second, Third)
```

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Syntax: Predicates and Programs

- **Predicate** (or *procedure definition*): a set of clauses whose heads have the same name and arity (the **predicate name**).

Examples:

```
pet(barry).                                animal(tim).
                                                animal(spot).
pet(X) :- animal(X), barks(X).           animal(hobbies).
```

Predicate `pet/1` has three clauses. Of those, one is a fact and two are rules.
Predicate `animal/1` has three clauses, all facts.

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Declarative Meaning of Facts and Rules

The declarative meaning is the corresponding one in first-order logic, according to certain conventions:

- **Facts:** state things that are true.
(Note that a fact “ p .” can be seen as the rule “ $p \leftarrow \text{true}$ ”)
Example: the fact $\boxed{\text{animal(spot)}}.$ can be read as “spot is an animal”.
- **Rules:** state implications that are true.
 - ◇ $p : - p_1, \dots, p_m.$ represents $p_1 \wedge \dots \wedge p_m \rightarrow p.$
 - ◇ Thus, a rule $p : - p_1, \dots, p_m.$ means
“if p_1 and ... and p_m are true, then p is true”

Example: the rule $\boxed{\text{pet}(X) : - \text{animal}(X), \text{barks}(X)}.$ can be read as “ X is a pet if it is an animal and it barks”.

Declarative Meaning of Predicates and Programs

- **Predicates:** clauses in the same predicate

$p : - p_1, \dots, p_n$
 $p : - q_1, \dots, q_m$
...

provide different *alternatives* (for p).

Example: the rules

$\text{pet}(X) : - \text{animal}(X), \text{barks}(X).$
 $\text{pet}(X) : - \text{animal}(X), \text{meows}(X).$

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Queries

- **Query:** an expression of the form:

$$\boxed{?- \ p_1(t_1^1, \dots, t_{n_1}^1), \dots, p_n(t_1^n, \dots, t_{n_m}^n).}$$

(i.e., a clause without a head)
($?$ - stands also for \leftarrow).

- The p_i to the right of $?$ - are called **goals** (procedure calls).

- Sometimes, also the whole query is called a (complex) goal.

- A query is a clause to be deduced:

Example: $?\text{- pet}(X)$, i.e., “ $\neg \text{pet}(X)$ ” can be seen as “true $\leftarrow \text{pet}(X)$ ”, i.e., “ $\neg \text{pet}(X)$ ”

- A **query** represents a *question to the program*.

Examples:

$?\text{- pet}(\text{spot}).$
asks whether spot is a pet.
asks: “Is there an X which is a pet?”

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Execution

- Example of a **logic program**:

```
pet(X) :- animal(X), barks(X).
pet(X) :- animal(X), meows(X).
animal(tim).
animal(spot).
animal(hobbes).
roars(hobbes).
```

- **Execution:** given a program and a query, *executing the logic program is attempting to find an answer to the query*.

Example: given the program above and the query $?\text{- pet}(X)$.
the system will try to find a “solution” for X which makes $\text{pet}(X)$ true.

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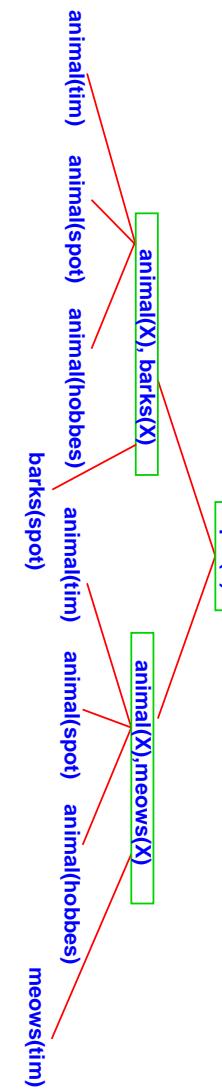
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The Search Tree

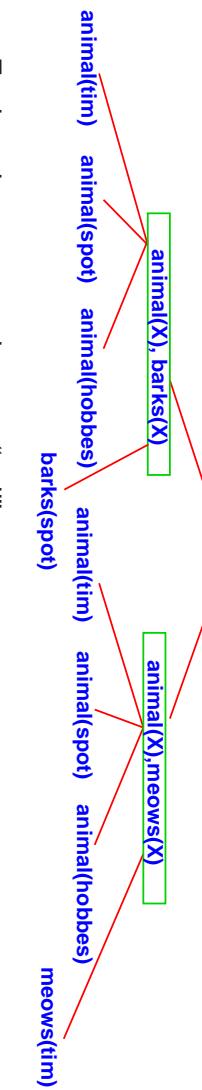
- A query + a logic program together specify a search tree.

Example: query `?- pet(X)` with the previous program generates this search tree
(the boxes represent the “and” parts [except leaves]):



- Different query → different tree.
- A particular execution strategy defines how the search tree will be explored during execution.
- Note: execution always finishes in the leaves (the facts).

Exploring the Search Tree



- Explore the tree top-down → “call”
- Explore the tree bottom-up → “deduce”
- Explore goals in boxes left-to-right or right-to-left

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Running Programs: Interaction with the System

- Practical systems implement a particular strategy (all Prolog systems implement the same one).
- The strategy is meant to explore the whole tree, but returns solutions one by one:
Example: (?- is the system prompt)

```
?- pet(X).
X = spot ? ;
yes
no
?-
```
- Prolog systems also allow to create executables that start with a given predefined query (which is usually `main/0` and/or `main/n`).
- Some systems allow to introduce queries in the text of the program, starting with `:-(` (remember: a rule without head). These are executed upon loading the file (or starting the executable).

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Operational Meaning of Programs

- A logic program is operationally a set of *procedure definitions* (the predicates).
- A query `?- p` is an initial *procedure call*.
- A procedure definition with one *clause* `p :- p1, ..., pm.` means:
“to execute a call to `p` you have to *call* `p1` and ... and `pm`”
 - ◇ In principle, the order in which `p1`, ..., `pn` are called does not matter, but, in practical systems it is fixed.
- If several clauses (definitions) `p :- p1, ..., pn` means:
`p :- q1, ..., qm`
- “to execute a call to `p`, `call p1` and ... and `pn`, or, alternatively, `q1` and ... and `qm`,

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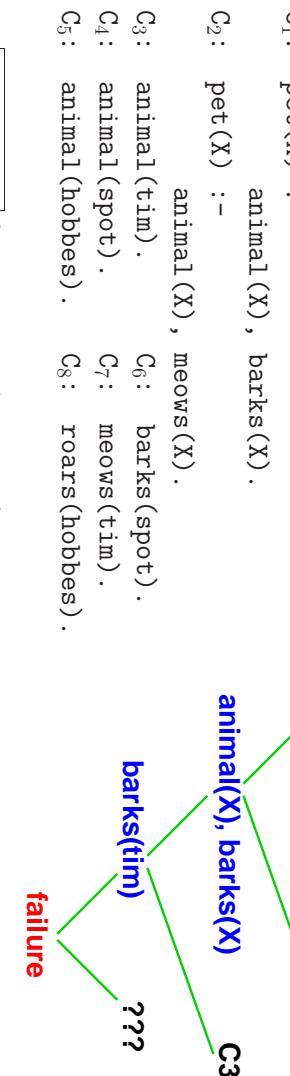
A (Schematic) Interpreter for Logic Programs (Prolog)

Let a logic program P and a query Q ,

1. Make a copy Q' of Q
2. Initialize the *resolvent* R to be $\{Q\}$
3. While R is nonempty do:
 - 3.1. Take the leftmost literal A in R
 - 3.2. Take the first clause $A' :- B_1, \dots, B_n$ (*renamed*) from P with A' same predicate as A
 - 3.2.1. If there is a solution θ to $A = A'$ (*unification*) continue
 - 3.2.2. Otherwise, take next clause and repeat
 - 3.2.3. If there are no more clauses, explore the last pending branch
 - 3.2.4. If there are no pending branches, output *failure*
 - 3.3. Replace A in R by B_1, \dots, B_n
 - 3.4. Apply θ to R and Q
4. Output solution μ to $Q = Q'$
5. Explore last pending branch for more solutions (upon request)

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Running Programs: Alternative Execution Paths



- $?- \text{pet}(X).$ (top-down, left-to-right)

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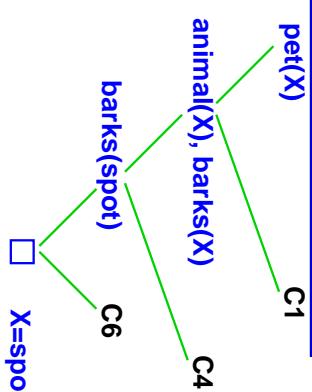
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Running Programs: Different Branches

```
C1: pet(X) :- animal(X), barks(X).
C2: pet(X) :- animal(X), meows(X).
C3: animal(tim).
C4: animal(spot).
C5: animal(hobbies).
```

```
C6: barks(spot).
C7: meows(tim).
C8: roars(hobbies).
```



- $?- \text{pet}(X)$. (top-down, left-to-right, different branch)

<i>Q</i>	<i>R</i>	Clause	θ
pet(X)	<u>pet(X)</u>	C_1^*	$\{ X=X_1 \}$
pet(X ₁)	<u>animal(X₁), barks(X₁)</u>	C_4^*	$\{ X_1=spot \}$
pet(spot)	<u>barks(spot)</u>	C_6	$\{ \}$
pet(spot)	<u>_</u>	$_$	$_$

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Backtracking (Prolog)

- **Backtracking** is the way in which Prolog execution strategy explores different branches of the search tree.
- It is a kind of “backwards execution”.
- (Schematic) Algorithm:
 - “Explore the last pending branch” means:
 1. Take the last literal successfully executed
 2. Take the clause against which it was executed
 3. Take the unifier of the literal and the clause head
 4. Undo the unifications

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Running Programs: Complete Execution (All Solutions)

C_1 :	$\text{pet}(X) :- \text{animal}(X), \text{barks}(X).$
C_2 :	$\text{pet}(X) :- \text{animal}(X), \text{meows}(X).$
C_3 :	$\text{animal}(\text{tim}).$
C_4 :	$\text{animal}(\text{spot}).$
C_5 :	$\text{animal}(\text{hobbes}).$

- $?- \text{pet}(X).$ (top-down, left-to-right)

Q	R	Clause	θ	Choice-points
$\text{pet}(X)$	$\text{pet}(X)$	C_1^*	$\{ X=X_1 \}$	*
$\text{pet}(X_1)$	$\underline{\text{animal}(X_1)}, \text{barks}(X_1)$	C_3^*	$\{ X_1=\text{tim} \}$	*
$\text{pet}(\text{tim})$	$\underline{\text{barks}(\text{tim})}$???	failure	*
		deep backtracking		
$\text{pet}(X_1)$	$\text{animal}(X_1), \text{barks}(X_1)$	C_4^*	$\{ X_1=\text{spot} \}$	*
$\text{pet}(\text{spot})$	$\underline{\text{barks}(\text{spot})}$	C_6	$\{ \}$	
$\text{pet}(\text{spot})$	—	—	—	
;		triggers backtracking		
		continues...		

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Running Programs: Complete Execution (All Solutions)

C_1 :	$\text{pet}(X) :- \text{animal}(X), \text{barks}(X).$
C_2 :	$\text{pet}(X) :- \text{animal}(X), \text{meows}(X).$
C_3 :	$\text{animal}(\text{tim}).$
C_4 :	$\text{animal}(\text{spot}).$
C_5 :	$\text{animal}(\text{hobbes}).$

- $?- \text{pet}(X).$ (continued)

Q	R	Clause	θ	Choice-points
$\text{pet}(X_1)$	$\underline{\text{animal}(X_1)}, \text{barks}(X_1)$	C_5	$\{ X_1=\text{hobbes} \}$	
$\text{pet}(\text{hobbes})$	$\underline{\text{barks}(\text{hobbes})}$???	failure	*
$\text{pet}(Y)$	$\underline{\text{pet}(Y)}$			

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Running Programs: Complete Execution (All Solutions)

```

C1: pet(X) :- animal(X), barks(X).
C2: pet(X) :- animal(X), meows(X).
C3: animal(tim).
C4: animal(spot).
C5: animal(hobbes).

C6: barks(spot).
C7: meows(tim).
C8: roars(hobbes).

```

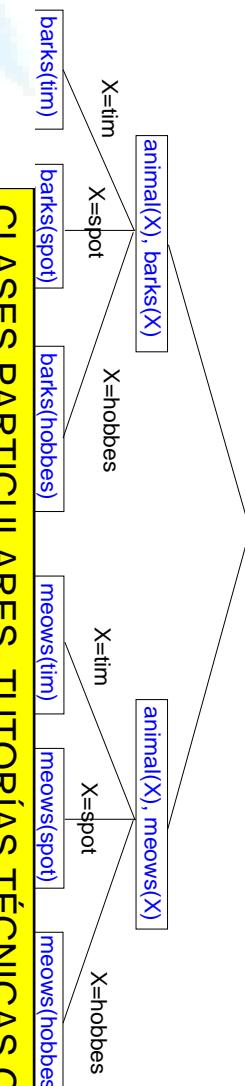
- ?- pet(X). (continued)

<i>Q</i>	<i>R</i>	Clause	θ	Choice-points
pet(X_2)	<u>animal(X_2), meows(X_2)</u>	C_4^*	{ $X_2=spot$ }	*
pet(spot)	<u>meows(spot)</u>	???	<i>failure</i>	*
pet(X_2)	<u>animal(X_2), meows(X_2)</u>	C_5	{ $X_2=hobbes$ }	
pet(hobbes)	<u>meows(hobbes)</u>	???	<i>failure</i>	
<i>failure</i>	deep backtracking			

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The Search Tree Revisited

- Different execution strategies explore the tree in a different way.
- A strategy is complete if it guarantees that it will find all existing solutions.
- Prolog does it top-down, left-to-right (i.e., depth-first).



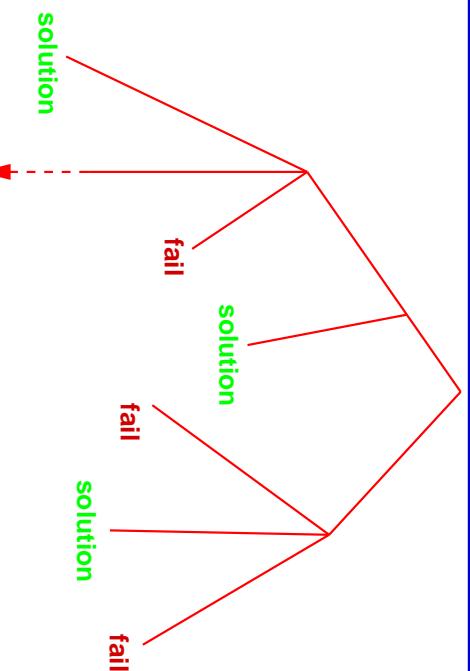
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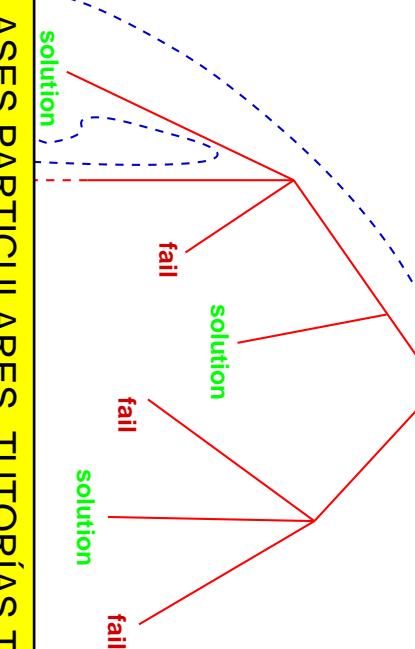


Characterization of the Search Tree

- All solutions are at *finite depth* in the tree.
- Failures can be at finite depth or, in some cases, be an infinite branch.



Depth-First Search



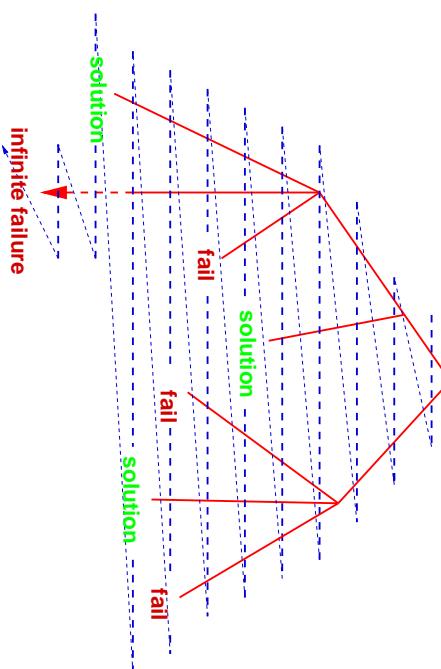
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Breadth-First Search

- But costly in terms of time and memory.
 - Used in some of our examples (via Ciao's bf package).



THE EXECUTION MECHANISM OF HEDGING

- At a *choice point*, take *first unifying clause* (i.e., the leftmost unexplored branch).
 - On failure, backtrack to the *next unexplored clause* of *last choice point*.

```
parent(C,G) :- parent(C,P), parent(P,G).
```

grandparent(charles,X)

```

parent(C,P) :- !, parent(C, charles).
parent(C,P) :- !, parent(C, philip).

parent(charles, P), parent(P, X) :- !, parent(charles, philip).
parent(charles, P), parent(P, X) :- !, parent(charles, philip).

parent(philip, X) :- !, parent(ana, X).
parent(philip, X) :- !, parent(george, X).

```

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Comparison with Conventional Languages

- Conventional languages and Prolog both implement (*forward*) continuations: the place to go after a procedure call succeeds. I.e., in:
`p(X, Y) :- q(X, Z), r(Z, Y).`
`q(X, Z) :-`

when the call to `q/2` finishes (with “success”), execution continues in the next procedure call (literal) in `p/2`, i.e., the call to `r/2` (the *forward continuation*).

- In Prolog, when there are procedures with multiple definitions, there is also a *backward continuation*: the place to go to if there is a *failure*. I.e., in:

```
p(X, Y) :- q(X, Z), r(Z, Y).  
q(X, Z) :- ... .  
q(X, Z) :- ... .
```

if the call to `q/2` succeeds, it is as above, but if it fails at any point, execution continues (“backtracks”) at the second clause of `q/2` (the *backward continuation*).

- Again, the debugger (see later) can be useful to observe execution.

Ordering of Clauses and Goals

- Since the execution strategy of Prolog is fixed, the ordering in which the programmer writes clauses and goals is important.
- Ordering of clauses determines the order in which alternative paths are explored. Thus:
 - ◆ The order in which solutions are found.
 - ◆ The order in which failure occurs (and backtracking triggered).
 - ◆ The order in which infinite failure occurs (and the program flounders).
- Ordering of goals determines the order in which unification is performed. Thus:

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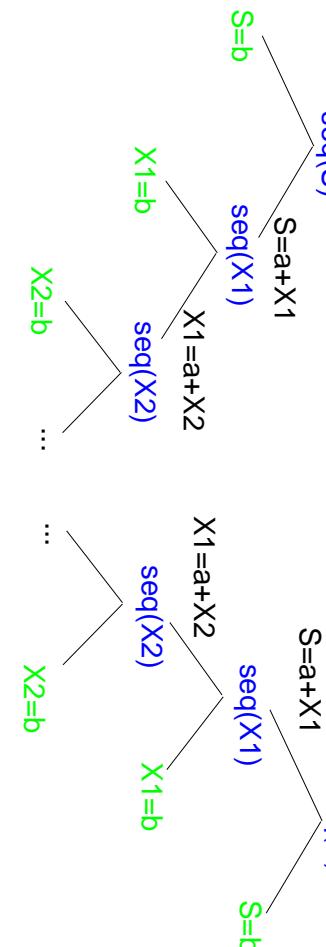
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Ordering of Clauses

```
seq(b) .  
seq(a+X) :- seq(X) .
```

```
seq(a+x) := seq(x) . seq(b).
```



- All infinite computation will no solutions (infinite failure)

6

singleton(X).
seq(X).

seq(X)

```
graph TD; A[seq(X1), singleton(a+X1)] --> B[seq(X1)]; A --> C[singleton(a+X1)]; B --> D[seq(b)]; B --> E[singleton(b)]; C --> F[S=b]; C --> G[S=a+X1]; G --> H[seq(S), singleton(S)]; G --> I[singleton(S), seq(S)];
```

The diagram illustrates the derivation of the sequent $\text{seq}(S), \text{singleton}(S)$ from the premise $\text{seq}(X_1), \text{singleton}(a+X_1)$. The proof tree branches into two main paths. One path leads to $\text{seq}(b)$ and $\text{singleton}(b)$, which are then combined into $S=b$. The other path leads to $S=a+X_1$, which is then combined with $\text{seq}(X_1)$ and $\text{singleton}(a+X_1)$ into $\text{seq}(S), \text{singleton}(S)$ and $\text{singleton}(S), \text{seq}(S)$.

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Execution Strategies

- **Search rule(s):** how are clauses/branches selected in the search tree (step 3.2 of the resolution algorithm).
- **Computation rule(s):** how are goals selected in the boxes of the search tree (step 3.1 of the resolution algorithm).
- Prolog execution strategy:
 - ◇ Computation rule: left-to-right (as written)
 - ◇ Search rule: top-down (as written)

Summary

- A logic program declares known information in the form of rules (implications) and facts.
- Executing a logic program is deducing new information.
- A logic program can be executed in any way which is equivalent to deducing the query from the program.
- Different execution strategies have different consequences on the computation of programs.
- Prolog is a logic programming language which uses a particular strategy (and does beyond logic because of its predefined predicates).

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Exercise

- Write a predicate `jefe/2` which lists who is boss of whom (a list of facts). It reads:
`jefe(X,Y)` iff `X` is direct boss of `Y`.
- Write a predicate `curritos/2` which lists pairs of people who have the same direct boss (should not be a list of facts). It reads:
`curritos(X,Y)` iff `X` and `Y` have a common direct boss.
- Write a predicate `jefazo/2` (no facts) which reads:
`jefazo(X,Y)` iff `X` is above `Y` in the chain of “who is boss of whom”.

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