

SURNAME:	NAME:	DNI:	GRADE:
COURSE: Random Signals (Señales Aleatorias)	DATE: 14/06/2018	GROUP:	

Final exam training  
Length: 3 hours

HOJA 1/2

## FINAL EXAM TRAINING

The following learning outcomes will be assessed in this exam:

**LO1** Analytically solve problems related to **probability theory and random variables**

**LO2** Analytically solve problems related to **random processes**

**LO3** Analytically solve problems related to **optimal filtering, detection and prediction of random signals**

**LO4** Analytically solve problems related to **information theory**

### LO1 LO2

1. Given two biomedical signals modeled as random processes  $X(t) = A\cos(\omega_0 t + \Phi/2)$  and  $Y(t) = AB\cos(\omega_0 t + \Phi/2)$ , where  $A$  and  $\omega_0$  are real constants and  $\Phi$  and  $B$  are **independent** random variables ( $\Phi \sim U(0, 4\pi)$ ,  $B \sim U(-1, 0)$ ).

- Check if  $X(t)$  and  $Y(t)$  are wide-sense stationary.
- Check if  $X(t)$  and  $Y(t)$  are jointly wide-sense stationary.
- Check if  $X(t)$  is ergodic in the mean and the autocorrelation.
- Given  $Z(t) = X(t) + N_2(t)$ , being  $N_2(t) = N_1(t) * h(t)$  with  $S_{N_1 N_1}(\omega) = N_0/2$  and  $H(\omega) = FT\{h(t)\} = 1, |\omega| < 1$ . Compute the SNR of  $Z(t)$

### LO1 LO4

2. Given a random variable  $X$  with the following symbols and probabilities:

	X0	X1	X2	X3	X4
P(X)	0.1	0.15	0.65	0.05	0.05

- Obtain a Huffman code and analyze the quality of the coding in terms of the mean code length with respect to the entropy.

### LO1 LO4

3. Given a family of communication channels defined by:

$$P(Y=0 | X=0) = a$$

$$P(Y=1 | X=0) = 1-a$$

$$P(Y=1 | X=1) = b$$

$$P(Y=2 | X=1) = 1-b$$

- Compute the channel capacity if  $a=b=1$ .
- Compute the channel capacity if  $a=b=1/2$ .



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Consider that all  $x(n)=0$  and  $r(n)=0$  if  $n<0$ .

**LO2 LO3**

5. Given a random process  $X(t)$  with cross-correlation

$$R_{XX}(-2) = 0.24649$$

$$R_{XX}(-1) = 0.24671$$

$$R_{XX}(0) = 0.27136$$

$$R_{XX}(1) = 0.24671$$

$$R_{XX}(2) = 0.24649$$

Use a 2-coefficient linear predictor to find  $S_{xx}(0)/S_{xx}(0.5)$



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